

# A method to extract peaks in chromosome conformation capture data

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# Motivation

- 1 Large amount of biological data can be produced in each experiment.
- 2 Multiple hypotheses are being conducted on it.
- 3 There is a growing need for methods to control the error rate of multiple hypotheses tests.
- 4 One would like to avoid type I error while performing multiple tests.
- 5 Traditional methods which reduce the probability of at least one type I error in multiple tests, were shown to be too restrictive.
- 6 New method of controlling the error called positive false discovery rate (pFDR) was developed.
- 7 We want to apply this method to find significant looping events in the chromosomes using chromosome capture (CC) data.

# Background

- 1 CC experiment capture millions of encounter events between different parts of the chromosome.

- 2

## Mathematical derivation

Conducting  $m$  hypothesis tests, using p-values,  $P$ , as our test statistics.

We fix a rejection region  $\gamma$ , and we reject the null hypothesis  $H$  is  $P \leq \gamma$ . ( $\gamma > 0$ )

Let  $V$  be the number of type I errors, out of  $R$  total rejections.

The pFDR is defined as:

$$pFDR = E \left( \frac{V}{R} | R > 0 \right)$$

We assume that the null hypothesis  $H$  is true ( $H = 0$ ) with an a priori probability  $\pi_0$  and false ( $H = 1$ ) with probability  $\pi_1$ . We write (Storey 2001, Theorem 1)

$$pFDR = \frac{\pi_0 Pr(P \leq \gamma | H = 0)}{Pr(P \leq \gamma)}$$

By the Bayes rule

$$pFDR = Pr(H = 0 | P \leq \gamma)$$

Under the null hypothesis, the p-values are uniformly distributed.

$$pFDR = \frac{\pi_0 \gamma}{Pr(P \leq \gamma)}$$

## Mathematical derivation

We now need an estimate of  $\pi_0$  and  $Pr(P \leq \gamma)$ .

Let  $R$  be the total rejected hypotheses, and  $W$  the total accepted hypotheses.

$$\hat{\pi}_0 = \frac{\#(P_i > \lambda)}{(1 - \lambda)m} = \frac{W(\lambda)}{(1 - \lambda)m} \quad 0 \leq \lambda < 1$$

We treat  $\lambda$  as fixed in the following.

$$\hat{Pr}(P \leq \gamma) = \frac{R(\gamma)}{m}$$

Plugging in these estimates and remembering that the pFDR is a conditional probability measure, we have

$$p\hat{FDR}_\lambda(\gamma) = \frac{W(\lambda)\gamma}{(1 - \lambda)R(\gamma)(1 - (1 - \gamma)^m)}$$

The equivalent of the p-values for this statistics is called the q-value.

q-values are the minimum pFDR that can occur when rejecting a statistics with  $t$  value.