

Started on	Thursday, 19 October 2023, 7:14 AM
State	Finished
Completed on	Thursday, 19 October 2023, 7:44 AM
Time taken	30 mins
Marks	14.00/15.00
Grade	9.33 out of 10.00 (93%)
Feedback	Congratulations on your performance! 🏆

Question 1

Complete

Mark 1.00 out of 1.00

How many one-to-one functions from a set of 2 elements to a set of 5 elements?

Answer:

Question 2

Complete

Mark 1.00 out of 1.00

How many positive integers not exceeding 100 and are divisible by neither 6 nor 9?

Select one:

- ☐ a. 88
- ☒ b. 78
- ☐ c. None of the other choice is correct.
- ☐ d. 68
- ☐ e. 58

Question 3

Complete

Mark 1.00 out of 1.00

Suppose $\gcd(m, n) = 7^3 \cdot 11^{12}$ and $\text{lcm}(m, n) = 2^4 \cdot 7^5 \cdot 11^{13} \cdot 13^4$. Choose correct statements:

(i) $m=7^5 \cdot 11^{12} \cdot 13^4$ and $n = 2^4 \cdot 7^3 \cdot 11^{13}$

(ii) $m=2^4 \cdot 7^5 \cdot 11^{13} \cdot 13^2$ and $n = 7^3 \cdot 11^{12} \cdot 13^2$

Select one:

- ☐ a. None of the other choices is correct
- ☒ b. (i)
- ☐ c. Both (i), (ii).
- ☐ d. (ii)

Question **4**

Complete

Mark 1.00 out of 1.00

Find the output of:

Greedy Change-Making Algorithm

Input: 1068 cents

Output: The number of coins of each type: Quarters (25 cents), Dimes (10 cents), Nickles (5 cents), Pennies (1 cent)

Select one:

- ☒ a. 42 , 1 , 1 , 3
- ☐ b. 42 , 1 , 0 , 8
- ☐ c. None of the other choices is correct
- ☐ d. 41 , 4 , 0 , 3
- ☐ e. 43 , 0 , 1 , 2

Question **5**

Complete

Mark 1.00 out of 1.00

How many solutions are there to the equation

$$x_1 + x_2 + x_3 = 12,$$

where x_1, x_2, x_3 are nonnegative integers such that $x_2 \leq 3$ and $x_3 \leq 3$?

Select one:

- ☐ a. None of the other choices is correct
- ☒ b. 16
- ☐ c. 24
- ☐ d. 20
- ☐ e. 12

Question **6**

Complete

Mark 1.00 out of 1.00

Find a recursive definition for

$$S(n) = n^2 - 1, \ n = 1, 2, 3, \dots$$

Select one:

- ☒ a. $S(1) = 0; S(n + 1) = S(n) + 2n + 1$ for $n \geq 1$
- ☐ b. $S(1) = 0; S(n + 1) = S(n) + n^2 + 2n + 1$ for $n \geq 1$
- ☐ c. None of the other choices is correct
- ☐ d. $S(1) = 0; S(n + 1) = S(n) + n^2$ for $n \geq 1$
- ☐ e. $S(1) = 0; S(n + 1) = S(n) + 2$ for $n \geq 1$

Question **7**

Complete

Mark 1.00 out of 1.00

How many divisions are needed when using Euclidean algorithm to find the greatest common divisor of $a = 846$ and $b = 238$?

Answer:

Question **8**

Complete

Mark 1.00 out of 1.00

procedure **XYZ**(a_1, \dots, a_n : integers)
 $k := 0$
 for $i := 1$ to n do
 if $a_i \bmod 2 = 0$ then $k := k + a_i$
Find output value of k if input is 1, 2, 3, 7, 8, 6, 9, 12, 11.

Select one:

- ☒ a. 28
- ☐ b. None of the other choices is correct
- ☐ c. 30
- ☐ d. 32
- ☐ e. 26

Question **9**

Complete

Mark 1.00 out of 1.00

21, 34, 55 are pairwise relatively prime.

Select one:

- ☒ True
- ☐ False

Question 10

Complete

Mark 1.00 out of 1.00

Which of the following algorithms are recursive?

- (i) procedure **XYZ**(n , P : integers)
 $s := 0$;
 for $j := 1$ to n
 $s := s + j^2$;
 return n
- (ii) procedure **ABC**(n , P : integer)
 if $n = 1$ then $ABC(1) := 1$;
 else $ABC(n) := ABC(n - 1) + n^2$;

Select one:

- ☐ a. None of them
- ☐ b. Both of them
- ☐ c. (i)
- ☒ d. (ii)

Question 11

Complete

Mark 1.00 out of 1.00

Rearrange the steps in the correct order of a proof by induction of the proposition

$1 + 3 + 5 + \cdots + (2n - 1) = n^2,$

for n positive integer.

Assume that the proposition is true for $n = k$.
Then the proposition is also true for $n = k + 1$ since
 $1 + 3 + 5 + \cdots + (2(k + 1) - 1) = 1 + 3 + 5 + \cdots + (2k - 1) + (2k + 1) = k^2 + 2k + 1 = (k + 1)^2$.
The proposition is true for $n = 1$ since $1 = 1^2$.
By induction, the proposition is true for all n positive integer.

Step 2

Step 3

Step 1

Step 4

Question 12

Complete

Mark 1.00 out of 1.00

Find the smallest integer n such that $f(x) = O(x^n)$.

2^x	Does not exist
$2x^3 \ln(x)$	4
$(x^3 - x^2 + x - 1)^3$	9

Question **13**

Complete

Mark 0.00 out of 1.00

A young pair of rabbits (one of each sex) is placed on an island. A pair of rabbits does not breed until they are 2 month old. After they are 2 month old they will produce 3 pairs of rabbits each month. Find the number of pairs of rabbits after 5 months.

Answer: 55

Question **14**

Complete

Mark 1.00 out of 1.00

How many bit strings of length seven either begin with two 0s or end with three 1s?

Select one:

- ☒ a. 44
- ☐ b. 48
- ☐ c. 52
- ☐ d. 40
- ☐ e. None of the other choices is correct

Question **15**

Complete

Mark 1.00 out of 1.00

Given

$$f(n) = 2.f(\sqrt{n})^2 + 1, f(2) = 1.$$

Find $f(16)$.

Answer: 19