

FP-Aufgaben 07

Aufgabe 1

$$g :: (\text{Num } a, \text{Eq } a) \Rightarrow [a] \rightarrow a \rightarrow [a] \rightarrow a$$

Aufgabe 2

call-by-value

$$\begin{aligned} & (\lambda n \rightarrow \text{mult } n \ n) (1+2) \\ &= \text{mult } (1+2) (1+2) \\ &= \text{mult } 3 \ (1+2) \\ &= \text{mult } 3 \ 3 \\ &= 3 * 3 = (*) 3 \ 3 = 9 \end{aligned}$$

call-by-name

$$\begin{aligned} & (\lambda n \rightarrow \text{mult } n \ n) (1+2) \\ &= \text{mult } (1+2) (1+2) \\ &= (\text{mult } (1+2)) (1+2) \\ &= (\lambda n \rightarrow (1+2) * n) (1+2) \\ &= (1+2) * (1+2) \\ &= (*) (1+2) (1+2) \\ &= (*) 3 \ 3 = 9 \end{aligned}$$

call-by-need

$$\begin{aligned} & (\lambda n \rightarrow \text{mult } n \ n) (1+2) \\ &= (\lambda n \rightarrow \text{mult } n \ n) 3 \\ &= \text{mult } 3 \ 3 \\ &= 3 * 3 = 9 \end{aligned}$$

Aufgabe 3

$$\begin{aligned}
& (\text{add } 2 \ 3) \\
&= (\text{add } 2) \ 3 \\
&= (\lambda x \rightarrow \text{inc} (\text{add} (\text{dec } 2) \ x)) \ 3 \\
&= \text{inc} (\text{add} (\text{dec } 2) \ 3) \\
&= (\text{add} (\text{dec } 2) \ 3) + 1 \\
&= (\text{add} (2-1) \ 3) + 1 \\
&= (\text{add } 1 \ 3) + 1 \\
&= ((\text{add } 1) \ 3) + 1 \\
&= ((\lambda x \rightarrow \text{inc} (\text{add} (\text{dec } 1) \ x)) \ 3) + 1 \\
&= \text{inc} (\text{add} (\text{dec } 1) \ 3) + 1 \\
&= ((\text{add} (\text{dec } 1) \ 3) + 1) + 1 = (\text{add} (1+1) \ 3) + 1 + 1 \\
&= (\text{add } 0 \ 3) + 1 + 1 \\
&= 3 + 1 + 1 = \cancel{3+1+1} \ (+) \ ((+) \ 3 \ 1) \ 1 = \cancel{5} \ (+) \ 4 \ 1 = 5
\end{aligned}$$

$$\begin{aligned}
& (\text{add}' \ 2 \ 3) \\
&= (\text{add}' \ 2) \ 3 \\
&= (\lambda m \rightarrow \text{add}' (\text{dec } 2) (\text{inc } m)) \ 3 \\
&= \text{add}' (\text{dec } 2) (\text{inc } 3) \\
&= \text{add}' (2-1) (3+1) \\
&= \text{add}' \ 1 \ 4 \\
&= (\text{add}' \ 1) \ 4 \\
&= (\lambda m \rightarrow \text{add}' (\text{dec } 1) (\text{inc } m)) \ 4 \\
&= \text{add}' (\text{dec } 1) (\text{inc } 4) \\
&= \text{add}' (1-1) (4+1) \\
&= \text{add}' \ 0 \ 5 \\
&= 5
\end{aligned}$$