CS 5033 - RL Project Report

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1. Introduction

For our RL project this semester, we want to build an RL agent that can easily beat the CartPole game.

CartPole v1 is a game environment provided in the Gym package from OpenAI. In this environment, there is a pole, attached to a cart (hence the name CartPole). The cart moves along a frictionless track. Force is applied in the left and right direction of the cart. The goal of the game is to keep the pole upright for as long as possible. For each step taken, a +1 reward is given, including the termination step. The maximum points achievable in the game is 475. There are a few conditions that, if met, will end the game.

First, if the pole angle is greater than 12 degrees, the game ends.

Second, if the cart position is greater than 2.4 (or the center of the cart reaches either end of the display), the game ends.

Finally, if episode length is greater than 500, the game ends.

For the criteria related to the CartPole environment, the agent will play the game for a 10000 episodes, and in each episode, the last 100 steps will have their rewards recorded (if the number of steps is less than 100, then the average will be over however many steps was taken for that episode) in order to generate an average. If any of the failing conditions is met, a penalty of -10 is given, otherwise, a reward of +1 is given.

2. Background

2.1. Reinforcement Learning

The goal of reinforcement learning (RL) is not simply to play a game. Rather, the driving force is to create systems that can be adaptive in the real world (?).

The essence of RL is learning through interaction and reward-driven behavior. The RL agent interacts with the environment and the results of its actions; it can then adjust its behavior in response to the reward(s) received (?)

This trial-and-error behavior can be considered the root of RL.

Reinforcement learning has been used in many applications such as process control, dispatch management, robot control,

game competition, etc. (?). In this project, we will explore using reinforcement learning to play the CartPole game, using 2 algorithm: SARSA and Q-Learning.

2.2. SARSA

SARSA is an on-policy temporal difference learning algorithm (?).

It is a popular reinforcement learning algorithm. At each time step, the agent selects an action according to its policy, observes the next state and reward, and updates the estimated value of the current state-action pair using a learning rate and discount factor. The algorithm maintains a Q-value function that estimates the expected future rewards for each state-action pair. The agent selects an action using an exploration-exploitation strategy and takes the selected action in the environment.

The update equation for SARSA learning is:

$$Q(s,a) \leftarrow Q(s,a) + \alpha * (R + \gamma * Q(s',a') - Q(s,a))$$

where α is the learning rate, and γ is the discount factor for future reward. For any given state-action pair, a new state-action value is obtained with a small correction to the old state-action value (?)

The behavior of using the next state and action to update the current state and action value gives rise to the name SARSA (State, Action, Reward, [next] State, [next] Action).

2.3. Q-Learning

Q-learning is a reinforcement learning algorithm that enables an agent to learn an optimal policy by observing and updating the estimated value of state-action pairs.

The agent selects an action and observes the next state and reward. Q-Learning is a very similar algorithm to SARSA learning. However, Q-learning uses an off-policy learning approach, updating the Q-value function using the maximum expected future reward (?).

The update equation for Q-Learning is:

$$Q(s, a) \leftarrow Q(s, a) + \alpha * (R + \gamma * max_{a'}Q(s', a') - Q(s, a))$$

Notice that the update equation always uses the maximum Q value to update the current state, action value.

3. Hypotheses

For this project, we will be testing 2 hypotheses:

Hypothesis 1: We epxect the Q Learning algorithm to perform better overall than the SARSA algorithm over 10000 episodes.

Hypothesis 2: For both algorithms, we expect exponential decay of ϵ to perform the best, as in, have the highest average reward over 10000 episodes.

Both Airi and Khoi's experiments will be performed in accordance to these hypotheses.

4. Experiments Done

4.1. Preliminary Test

This section serves as a baseline. Here, the game is played randomly, without using any training algorithm. Here are the results:

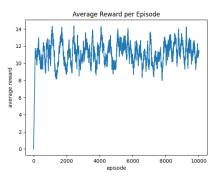


Figure 1. Baseline Testing Results

Looking at the graph, we can see that the average reward are very low.

4.2. Airi's Experiments - Q-Learning

4.3. Khoi's Experiments - SARSA Learning

For SARSA Learning, Khoi is also implementing an ϵ greedy method. For his setup, the hyperparameters are: $\epsilon=0.5$; $\gamma=0.9$; and $\alpha=0.5$

Additionally, Khoi is also implementing three differement decaying methods for the ϵ hyperparameter. These methods will be explained further in the **General Analysis** section, with **Hypothesis 2**.

For one run of 10000 episodes, with ϵ kept static at 0.5, here are his current results. Note that due to the random nature of taking actions, each run will produce a different graph.

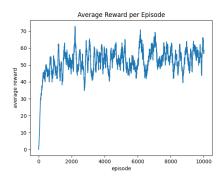


Figure 2. SARSA Results Over 10000 Episodes, Static ϵ

Looking at the graph, we can see that the average rewards reached a plateau of approximately 60 after about 1000 to 1500 episodes, this shows that the agent is indeed being trained to take more optimal actions as the number of episodes increased. Compared to the baseline results, the average reward are much higher.

5. General Analysis

5.1. Hypothesis 1

This comparison is done between Khoi's SARSA algorithm, and Airi's Q-Learning algorithm. Below is the graph of average reward for each algorithm, with ϵ kept static at 0.5

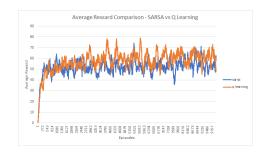


Figure 3. Comparison of SARSA and Q Learning

Looking at the figures, we can see that Q-Learning perform slightly better than SARSA, as the average reward stayed at a higher range for longer. Moreover, Q-Learning has an average reward of 57.44 while SARSA's average is only 52.41.

5.2. Hypothesis 2

We explored three different methods of ϵ decay. First, ϵ is kept static at a value of 0.5. Second, ϵ followed the decaying function of $\epsilon = 0.5 * \frac{1}{no.ofepisodes}$. Finally, ϵ follows the exponential decaying function of $\epsilon = 0.5 * \frac{1}{e^{-0.001*no.ofepisodes}}$

For SARSA, comparing the three methods of ϵ decay, yields the following results:

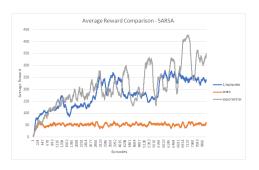


Figure 4. Average Reward of SARSA, Comparing DIfferent ϵ Decay

Additionally, the mean and standard deviation for each method are as follows:

Method	Mean	Standard Deviation
Static	52.41	7.089
1/Episodes	116.56	45.775
Exponential	192.32	68.383

Table 1. Mean of Average Reward and Standard Deviation

As these results show, for the SARSA algorithm, exponential decay of ϵ performed the best.

Next, for Q Learning, the comparison graph is as follows:

6. Methods Comparison and Related Work Review

Swagat Kumar implemented a Deep Q Netword approach to this problem in 2020. Their DQN result is shown below:

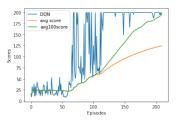


Figure 5. Performance of Kumar's DQN. Avg100score is the average of the last 100 episodes

It should be noted that Kumar used v0 of the CartPole environment, which has a much lower maximum reward threshold of 195. As such, their model were able to solve the problem in only 200 episodes (?). Moreover, in the paper,

Kumar also stated that DQN is much faster compared to the usual Q-Learning approach, which solved the problem in 300 episodes.

We expect the same result would apply to our v1 environment, if we were to implement a Deep Q Network approach.

Another comparison is from (?). Here, Wang showed that SARSA performs slightly better than Q-Learning, taking less time to train, as shown in this figure taken from the paper. From this figure, the Time factor will be taken into consideration.

 Table 5

 Result of 50 runs for each RL algorithm in Example 3.

 Methods
 Trial
 Std.
 Time
 α
 γ

 Q-learning
 649.88
 151.88
 48.83
 0.1
 0.99

 Sarsa algorithm
 558.92
 198.84
 40.21
 0.1
 0.99

 SA-Q-learning
 559.90
 189.16
 33.09
 0.1
 0.99

Figure 6. Performance of Wang's Algorithms

Compared to our implementation of SARSA and Q-Learning, where we have the average running time to go through 10000 episodes for Q Learning is 192.343 seconds, while SARSA takes 180.925 seconds to perform the same task. So, our results matched that of Wang's, if running time is the only consideration. However, because of the difference in metrics, we considered Q Learning to be the better algorithm for our case.

7. Conclusion and Future Work

Throughout the course of this project, we were able to implement a SARSA and a Q-Learning algorithm that successfully played the CartPole game. As hypothesized, exponential decay of ϵ yielded the largest average reward. We also compared our methods' performance with existing metrics and found that it has explainable differences to related works.

In the future, we wished to be able to save our modesl to memory, and be able to recall them in a fresh environment without having to go through the training steps again. Moreover, we also wanted to implement eligibility traces with backwards $\mathrm{TD}(\lambda)$ to see how it compares. Moreover, we would also like to implement some sort of custom reward functions, as opposed to a fixed -10 or +1 reward, to see if learning time would improve.

Finally, aside from this CartPole environment we used, there exists the Pendulum environment within the same Gym package with similar properties. We think this will provide an interesting challenge and comparison to solve.