

# Lab 2 (Statistics)

- If the mean of five observations  $x$ ,  $x + 4$ ,  $x + 6$ ,  $x + 8$  and  $x + 12$  is 16, find the value of  $x$ .
- The mean of 40 numbers was found to be 38. Later on, it was detected that a number 56 was misread as 36. Find the correct mean of given numbers.

## Normal Distribution

- $X$  is a normally distributed variable with mean  $\mu = 30$  and standard deviation  $\sigma = 4$ . Find
  - a)  $P(x < 40)$
  - b)  $P(x > 21)$
  - c)  $P(30 < x < 35)$
- A radar unit is used to measure speeds of cars on a motorway. The speeds are normally distributed with a mean of 90 km/hr and a standard deviation of 10 km/hr.

What is the probability that a car picked at random is travelling at more than 100 km/hr?

- For a certain type of computers, the length of time between charges of the battery is normally distributed with a mean of 50 hours and a standard deviation of 15 hours. John owns one of these computers and wants to know the probability that the length of time will be between 50 and 70 hours.
- Entry to a certain University is determined by a national test. The scores on this test are normally distributed with a mean of 500 and a standard deviation of 100. Tom wants to be admitted to this university and he knows that he must score better than at least 70% of the students who took the test. Tom takes the test and scores 585. Will he be admitted to this university?

- The length of similar components produced by a company are approximated by a normal distribution model with a mean of 5 cm and a standard deviation of 0.02 cm. If a component is chosen at random
  - a) what is the probability that the length of this component is between 4.98 and 5.02 cm?
  - b) what is the probability that the length of this component is between 4.96 and 5.04 cm?

- The length of life of an instrument produced by a machine has a normal distribution with a mean of 12 months and standard deviation of 2 months. Find the probability that an instrument produced by this machine will last
  - a) less than 7 months.
  - b) between 7 and 12 months.

- The time taken to assemble a car in a certain plant is a random variable having a normal distribution of 20 hours and a standard deviation of 2 hours. What is the probability that a car can be assembled at this plant in a period of time
  - a) less than 19.5 hours?
  - b) between 20 and 22 hours?

- A large group of students took a test in Physics and the final grades have a mean of 70 and a standard deviation of 10. If we can approximate the distribution of these grades by a normal distribution, what percent of the students
  - a) scored higher than 80?
  - b) should pass the test ( $\text{grades} \geq 60$ )?
  - c) should fail the test ( $\text{grades} < 60$ )?



- The annual salaries of employees in a large company are approximately normally distributed with a mean of \$50,000 and a standard deviation of \$20,000.
  - a) What percent of people earn less than \$40,000?
  - b) What percent of people earn between \$45,000 and \$65,000?
  - c) What percent of people earn more than \$70,000?

- A customer calling a call center spends an average of 45 minutes on hold during the peak season, with a standard deviation of 12 minutes. Suppose these times are normally distributed. Find the probability that the customer will be on hold for each interval of times:
  - a) More than 54 minutes.
  - b) Less than 24 minutes.
  - c) Between 24 and 54 minutes.
  - d) More than 39 minutes.