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## Soft Computing Techniques (Assignment 2)

Design a fuzzy control system for Washing Machine. inorder to determine the Wash Time.

### I) Input Variables.

① Dirt (on clothes): High dirt ( $D_3$ ), Medium Dirt ( $D_2$ )  
Low dirt ( $D_1$ )

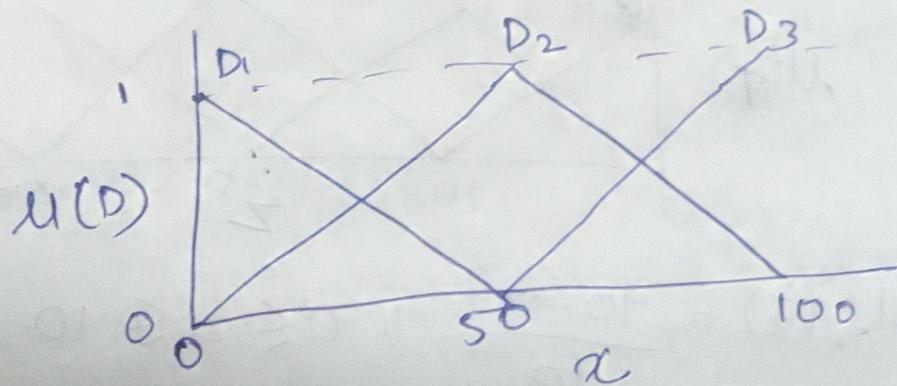
② Grease (on clothes): High Grease ( $G_3$ ), Medium Grease ( $G_2$ )  
Low Grease ( $G_1$ )

### II) Output Variables:

Wash Time: Very High ( $T_5$ ), ~~medium~~ High ( $T_4$ )  
Medium ( $T_3$ ), short ( $T_2$ ),  
Very short ( $T_1$ ).

### III) Defining membership function for i/p variable

#### i) For dirt:

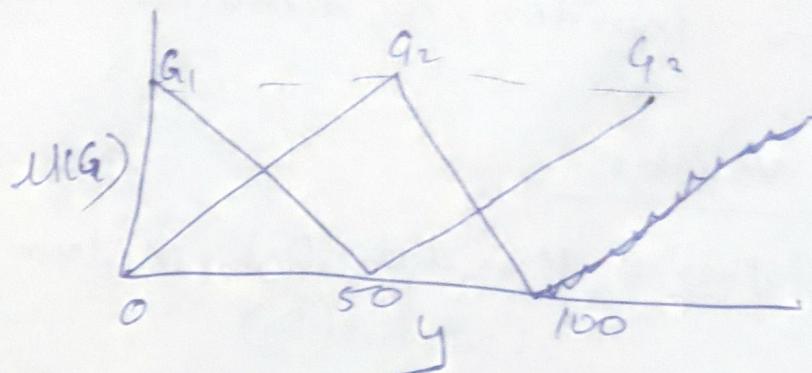


$$i) \mu_{D_1}(x) = \frac{50-x}{50}, \quad 0 \leq x \leq 50$$

$$ii) \mu_{D_2}(x) = \begin{cases} \frac{x}{50}, & 0 \leq x \leq 50 \\ \frac{100-x}{50}, & 50 \leq x \leq 100 \end{cases}$$

$$\text{iii) } \mu_{G_3}(x) = \frac{x-50}{50}, \quad 50 \leq x \leq 100$$

② For greese.

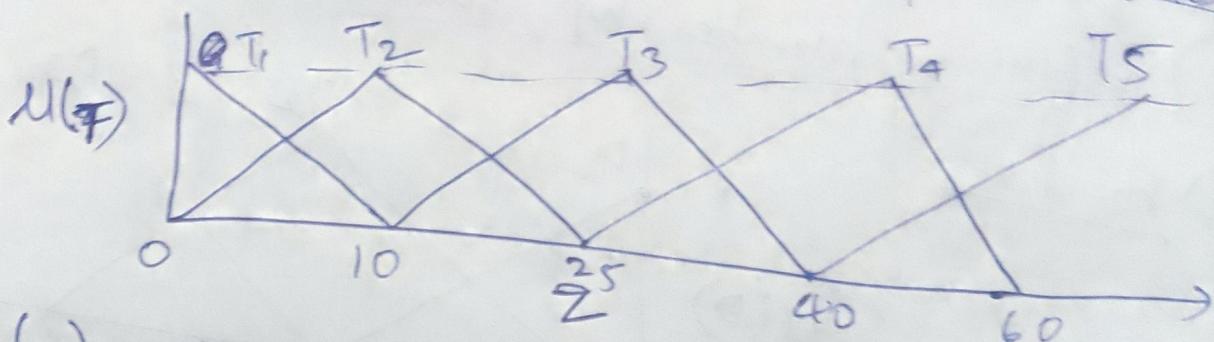


$$\text{iv) } \mu_{G_1}(y) = \frac{50-y}{50}, \quad 0 \leq y \leq 50$$

$$\begin{aligned} \text{v) } \mu_{G_2}(y) &= \frac{y}{50}, \quad 0 \leq y \leq 50 \\ &= \frac{100-y}{50}, \quad 50 \leq y \leq 100 \end{aligned}$$

$$\text{vi) } \mu_{G_3}(y) = \frac{y-50}{50}, \quad 50 \leq y \leq 100$$

#### IV Defining Membership function for o/p variables



$$\text{i) } \mu_{T_1}(z) = \frac{10-z}{10}, \quad 0 \leq z \leq 10$$

$$\begin{aligned} \text{ii) } \mu_{T_2}(z) &= \frac{z}{10}, \quad 0 \leq z \leq 10 \\ &= \frac{25-z}{15}, \quad 10 \leq z \leq 25 \end{aligned}$$

Wash time

$$\text{iii) } \mu_{T_3}(z) = \frac{z-10}{15} \quad 10 \leq z \leq 25$$

$$= \frac{40-z}{15} \quad 25 \leq z \leq 40$$

$$\text{iv) } \mu_{T_4}(z) = \frac{z-25}{15} \quad 25 \leq z \leq 40$$

$$= \frac{60-z}{20} \quad 40 \leq z \leq 60$$

$$\text{v) } \mu_{T_5}(z) = \frac{z-40}{20}, \quad 40 \leq z \leq 60$$

## IV) Control Rules for our Fuzzy controller

	$G_1$	$G_2$	$G_3$
$D_1$	$T_1$	$T_3$	$T_4$
$D_2$	$T_2$	$T_3$	$T_4$
$D_3$	$T_5$	$T_4$	$T_5$

i. Rules can be define as

i) If Dirt is  $D_1$  and Grease is  $G_1$ , then Wash Time is  $T_1$

ii) If Dirt is  $D_1$  and Grease is  $G_2$  then Wash Time is  $T_3$

iii) If Dirt is  $D_1$  and Grease is  $G_3$  then Wash Time is  $T_4$

iv) If Dirt is  $D_2$  and Grease is  $G_1$  then Wash Time is  $T_2$ .

- v) If dirt is  $D_2$  and Grease is  $G_2$  then  
 Wash Time is  $T_3$
- vi) If dirt is  $D_2$  and Grease is  $G_3$  then  
 Wash Time is  $T_4$
- vii) If dirt is  $D_3$  and Grease is  $G_1$  then  
 Wash Time is  $T_3$
- viii) If dirt is  $D_3$  and Grease is  $G_2$  then  
 Wash Time is  $T_4$
- ix) If dirt is  $D_3$  and Grease is  $G_3$  then  
 Wash Time is  $T_5$

### VI) Test Cases (Examples)

1) Assume Dirt is 60% & Grease is 70%.

Sol<sup>n</sup> &  $\Rightarrow$  Converting Crisp to Fuzzy value. (Fuzzification)  
 Here since Dirt  $\Rightarrow 60\%$ .

& Grease  $\Rightarrow 70\%$ .

there are 2 ~~are~~ ~~100~~ membership function applicable.

$$\text{and } \mu_{D_2}(x) = \frac{100-x}{50} = \frac{100-60}{50} = \frac{40}{50} = 0.8$$

$$\mu_{D_3}(x) = \frac{x-50}{50} = \frac{60-50}{50} = \frac{10}{50} = 0.2$$

$$\text{and } \mu_{G_2}(y) = \frac{100-y}{50} = \frac{100-70}{50} = \frac{30}{50} = 0.6$$

$$\mu_{G_3}(y) = \frac{y-50}{50} = \frac{70-50}{50} = \frac{20}{50} = 0.4$$

0.1 Linn membership value of  $T_3$  is 10  
 Now converting the membership values to linguistic term.

0.8  $\Rightarrow$  Medium Dirt  $\Rightarrow D_2$

0.2  $\Rightarrow$  High Dirt  $\Rightarrow D_3$

0.6  $\Rightarrow$  Medium Grease  $\Rightarrow G_2$

0.4  $\Rightarrow$  High Grease  $= G_3$

Evaluation all possibilities for Defuzzification using Mean Max method

	$D_2$	$G_2$	$\text{Min}(D_2, G_2) = \text{Min}(0.8, 0.6) = 0.6$
i)	$D_2$	$G_3$	$\text{Min}(D_2, G_3) = \text{Min}(0.8, 0.4) = 0.4$
ii)	$D_3$	$G_2$	$\text{Min}(0.2, 0.6) = 0.2$
iii)	$D_3$	$G_3$	$\text{Min}(0.2, 0.4) = 0.2$

$$\therefore \text{Max}(0.6, 0.4, 0.2, 0.2) = \underline{\underline{0.6}}$$

$\therefore$  Here we will select  $D_2 \& G_2$

for evaluation

We have define rule  $\forall$  for  $D_2 \& G_2$  evaluation.

$\therefore$  If dirt is  $D_2$  & grease is  $G_2$  then wash time is  $T_3$

Evaluation membership value of  $T_3$  to

find wash time

$$U_{T_3}(z) = \frac{z-10}{15} \quad \& \quad U_3(z) = \frac{40-z}{15}$$

$$0.6 = \frac{z-10}{15} \quad \& \quad 0.6 = \frac{40-z}{15}$$

$$(0.6 \times 15) + 10 = z \quad \& \quad (0.6 \times 15) + 2 = z$$

$$\therefore \boxed{z=19} \quad \& \quad \boxed{z=31}$$

Here we can take average of these two val.

$$\therefore z^* = \frac{19+31}{2} = 25 \text{ min}$$

$$\therefore \boxed{T_3 = 25 \text{ min}}$$

Hence the time required is 25 min.

Graphically

