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CS-225: Discrete Structures in CS

Homework 8, Part 2

Exercise Set 9.5: #7.b((ii), (iii)), #12, #16.(a, b)

Exercise Set 9.6: #4, #13, #18

Set 9.5:

$$7. \text{ b) ii. } \binom{13}{7} - \binom{7}{7} \equiv \frac{13!}{7!(6!)} - \frac{7!}{7!(0!)} = \frac{13 \times 11 \times 9 \times 8}{6} - 1 = 1,715 \text{ [ans]}$$

$$\text{iii. } \binom{6}{6} \binom{7}{1} + \binom{6}{5} \binom{7}{2} + \binom{6}{4} \binom{7}{3} \equiv (1 \times 7) + (6 \times 21) + (15 \times 45) = 808 \text{ [ans]}$$

$$12. \binom{101}{2} \approx \frac{101!}{2!(99!)} = \frac{101 \times 100}{2} = 101 \times 50 = 5,050, \text{ then we divide by 2 because statistically half of these values have an even sum, which is what we are to show.}$$

[ans] 2525

16.

$$\text{a) } \binom{40}{5} = \frac{40!}{5!(35!)} = 39 \times 38 \times 37 \times 36 \times 35 = 658,008 \text{ possible combinations of 5 out of 40}$$

$$\text{b) Previous answer} - \binom{37}{5}$$

$$\frac{37!}{5!(32!)} = 37 \times 36 \times 35 \times 34 \times 33 = 373,626$$

$$\text{[ans]} 658,008 - 373,626 = 284,382 \text{ samples will contain at least one defective chip}$$

Set 9.6:

4.

$$\text{a) } \binom{30+8-1}{30} = \binom{37}{30} = \frac{37!}{30!(7!)} = 37 \times 36 \times 35 \times 34 \times 33 \times 32 \times 31 = 10,295,472$$

$$\text{b) } \binom{26+8-1}{26} = \binom{33}{26} = \frac{33!}{26!(7!)} = 33 \times 32 \times 31 \times 30 \times 29 \times 28 \times 27 = 4,272,048$$

$$\text{c) Subtract solution b from solution a: } 10,295,472 - 4,272,048 = 6,023,424$$

$$13. \binom{24+4-1}{24} = \binom{27}{24} = \frac{27!}{24!(3!)} = \frac{27 \times 26 \times 25}{3!}$$

18.

$$\text{a) } \binom{30+120-1}{30} = \frac{149!}{30!119!} = \frac{149 \times 148 \times 147 \times \dots \times 120}{30!}$$

b)