Let Y^{n-1}

Solution of equation $\Phi(x, u, p) = 0$

Let Y^{n-1} be a surface in V^n and φ function on Y^{n-1}

We have to find function u such that

$$\Phi(x, u, p) = 0, u|_{V} = \varphi$$

'Solution

Characteristic vector field is

$$\mathbf{X} = -\frac{\partial \Phi}{\partial p_m} \frac{\partial}{\partial_m} + \left(\frac{\partial \Phi}{\partial x^m} + p_m \frac{\partial \Phi}{\partial y} \right) \frac{\partial}{\partial} + p_r \frac{\partial \Phi}{\partial p_r} \frac{\partial}{\partial u}$$

This vector field is

- i) tangent to the surface M
- ii) it vanishes contact form
- iii) it is symplectoorthogonal to 2n-1 dimensional plane P=intersection of tangent and contact plane.

Hence applied to initial manifold it gives the