Duistermont- Heckman localisation formula and locar of vector fields. 12 October 2013 \$0 about Fivo years ago (summer 2012) Darha Belavin explained how to calculate an integral $Z(t) = \int e^{t} d_{K} W$ (0.1) (w-1 form, dx = d+ lx). He exp showed first the Mischlegral doer not depend on t, then showed Hole it is localised at zeros of vector field K:

Z(H ~ \frac{1}{\text{Vdet}} \frac{3E}{3x} \ksize. (0.2) It is Eypical localisation formula. Thried to revive there calculation, that On one hand they are leading to Düislermeet - Keckmen formule in more less general case.

On the other hand we may discus at is interesting to analyze geometrical meaning of answer.

S1. localisation

Two words about Devistermat-Heckmen formule

(DHL)-formule.

Let M-le compact manifold

(M²ⁿ, D) le compact jumple ctic menifold

Let H be an Hamiltonian, such that the vector field is a compact vector field (i.e. it generates compact sulgroup & the in the group of differmorphisms) (we suppose that K(X) are not-degenerate This is famour Dissermet-Heckman formula We will consider here a special but very illuminating case of this formula. etude [See in more defail the next

We comider now the following set up: Let whe 1-form on M (dim M32m) Such that $\Omega = dw$ definer symplectic structure. (of course condition $\Omega = dw$ is in contradiction with comportness of $M: SI^m \neq 0$, but we ignore now this. Egwe suppose that M is not compact Let K le a veclor field such thet Lxw=dwsk+d(wsk/20 Then It is evident that K is Hamiltonian redor field of H= WIK ILIK= du IK=-dlusK=-dH. $\frac{\partial V}{\partial x} = \frac{\partial v}{\partial x} =$ We see that

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Calculation of Seidkie. Consider Stitch W. Idk = Lk / Z(H= Je itch W. Idk = Lk) Show Hot ZHI does not depend on t.

dZH = i J dx w e = -= i fdk (we it dk we) = id(twe it dk w) = 0 m (under some kechnical conditions); (21) [Slk w = 0 since form kew her rank \(\in 2n - 1) \) We see that ZH does not depend on to Hence we call calculate ZH at too. Seitdre seit(ItH) = du=D, wIK=H, (Lru=9) Calculate uning stationer y phone method: $dH = d(wJK) = -dwJK \qquad (2.3)$ Locus of dH = locus of K

32 H/= 3 2 CW/K/= 2 (OfpK)= (dewskl=-dwsk) (Hexil=0 for Kexd=0) Hence Note: 3K is their operator at publishmentalei [K, 4]. We see that answer does not depend on

OHL formula (In particular HIX:1=0).

On the other hand this formula emphissizer the role of vector field K: It states that Seit (dwt lkw) Sc Je July Sk X. Kulo depends only on Kat lovers in the care if w is an "askitrary" K-invariant 1-form (of course du is not-degenerale) This weful to study DHL formule in its supersymmetric manifestation.

1. A. Nersessian. "Antibrackets and theyral."

(Lee 2. A. Schwarz, O. Zalorowsky "Supersymmetry and localization" JETP Lett, 58,1(1953)-EMP (1995 or 1996) 12 X 9.012 (Dee for détail next étude)