

# CURRICULUM VITAE

## 1. PERSONAL RECORD.

Full name: **Dr. Hovhannes Khudaverdyan**

(in most of scientific articles after 2000 H. M.Khudaverdian, before 2000: O.M.Khudaverdian)

Nationality: British, Armenian

Date and place of birth: 28 May 1955, Yerevan (Armenia)

Marital status: Married with two adult sons.

Place of residence: 33 Highfield Road, Prestwich, Manchester M25 3AQ.

Languages: Armenian and Russian mother tongues, English fluent, French competent

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## 2. EDUCATION AND QUALIFICATIONS.

**Ph.D. in Theoretical and Mathematical Physics. 1982**

Thesis: *Multiplicative and Additive Functionals; their Role in Quantum Field Theory*

Advisor: Professor A.S. Schwarz.

Referees: Professor V.I. Ogievetsky, Professor Yu.I. Manin

1978–1981 *Postgraduate student*

Department of Theoretical Nuclear Physics

Moscow Physical Engineering Institute (MPEI).

**M.S. in Physics (with Honors). 1978.**

Thesis: On Anomalies in Quantum Field Theory.

Advisor: Professor A.S. Schwarz.

1975–1978 Department of Theoretical Nuclear Physics

Moscow Physical Engineering Institute.

1972–1975 Department of Physics

Yerevan State University.

### 3. PROFESSIONAL EXPERIENCE.

#### Current position:

Since August 2005 Senior Lecturer in Pure Mathematics, University of Manchester

#### Previous positions:

- 2001—2005    Lecturer in Pure Mathematics, UMIST  
                  (University of Manchester from 2004)
- 1996—2005    Senior Researcher,  
                  Laboratory of Computing Technique and Automation  
                  Joint Institute for Nuclear Research (Dubna, Russia)
- Since 1985    Senior Researcher, Department of Theoretical Physics  
                  Yerevan State University (Yerevan, Armenia)
- 1981—1985    Junior Researcher, Laboratory of Theoretical Physics  
                  Yerevan Physics Institute (Yerevan, Armenia)

#### Invited guest positions:

- January 2012    Guest Professor in I.H.E.S. (Paris)
- Autumn 2011    Guest Professor Max-Planck-Institut für Mathematik (Bonn)
- 2000            Academic Visitor, UMIST
- Autumn 1999    Guest Professor Max-Planck-Institut für Mathematik (Bonn)
- Autumn 1994    Professor of Mathematics, Advanced Institute of Basic Sciences  
                  (Zanjan, Iran)
- 10.1988–08. 1989    Visiting Researcher, Department of Theoretical Physics  
                  Geneva University (Geneva, Switzerland)

#### Research grants:

- October 2010 and February 2012;  
    LMS (scheme 2) grants            supporting a visitor to UK
- October 2007 and July 2008    Royal Society grants for conferences
- 2000-2001                    EPSRC
- 1996–1998,                  INTAS-RFFI: European Union and  
  Russian Foundation for Basic Research
- 1993–1995                  International Science Foundation

**Invited talks (after 2000):**

November 2011	Geometry Seminar in Liege University (Belgium)
	Mathematica Physics Seminar in Max-Planck-Institut (Bonn)
January 2010	Analysis and Geometry Seminar in Newcastle University
December 2009	Mathematics Seminar in Valenciennes University (France)
December 2009	Mathematical Physics Seminar in Lille University (France)
October 2009	Geometry and Topology Seminar in Aberdeen University
May 2008	Mathematical Physics Seminar in Bordeaux University (France)
April 2008	W.Brauer Special topology seminar in Princeton University (USA)
January 2008	S.P. Novikov Geometry and Topology Seminar, V.A. Steklov Mathematical Institute (Moscow)
November 2007	Applied Mathematics Seminar in Brunel University
January 2007	All-Moscow seminar "Globus"
December 2006	Geometry seminar in Independent University
January 2006	Geometry Seminar in Edinburgh University
September 2004	I.R.Shafarevitch Algebra Seminar, Steklov Institute (Moscow)
February 2004	Seminar on Mathematical Physics, University of Loughborough
December 2003	Analysis/Geometry Seminar, King's College
October 2003,	Bristol Pure Mathematics Seminar
October 2003,	Liverpool Pure Mathematics Colloquium
September 2003	I.V. Tamm Department of Theoretical Physics, Moscow
April 2003,	Geometry of differential equations Seminar, Moscow, IU
July 2002	International Workshop Quantum Gravity and Superstrings, Dubna
November 2001,	Geometry with Brackets and Quantization, Warwick
December 2000	Geometry and Theoretical Physics Seminar, King's College London
November 2000	N. Hitchin Geometry and Analysis Seminar, Oxford University
November 2000	Departmental Colloquium, Sheffield University
July 2000	International Workshop on Quantization, Warwick
April 2000	Mathematical Physics Seminar, Loughborough University
February 2000	I.V. Tamm Department of Theoretical Physics,

**Meetings (after 2000):**

Lecturer on the School for young researchers attached to the XXXI and Workshops on Geometry in Physics. Bialowieza, Poland, July 2012  
XXII, XXV, XXVII and XXX and Workshops on Geometry in Physics. Bialowieza, Poland, July 2003, July 2006, July 2008 and July 2011 *Plenary talks*. (Opening plenary talk on the last Workshop)

International workshops "Supersymmetry in Integrable Systems - SIS'10"  
August 24-28, 2010, Yerevan, Armenia, August 01-04 Hannover, Germany  
*Invited talks*

Third International Conference on Geometry and Quantization GEOQUANT  
at the University of Luxembourg. September 7 - 11, 2009. *Invited talk*.

International workshops "Supersymmetry and Quantum Symmetries. Dubna,  
Russia, July 2009, July 2007, and July 2005. *Invited talks*.

XVIII International Colloquium "Integrable Systems and Quantum Symmetries" Prague, Czech Republic, June 18—20, 2009. *Invited Talk*.

One-day Geometry workshop Lyon—Manchester—Loughborough in Loughborough University. March 13, 2009. *Invited talk*.

Conference "Conformal Field Theory and Integrability", Nor-Amberd, Armenia, October 2007. *Plenary talk*

"Integrable Day" in Loughborough University November 2006. *Invited talk*

10-th International Conference Symmetry Methods in Physics. Yerevan, 13–20 August, 2003. *Talk presented*.

International workshop "Quantum Gravity and Superstrings". Dubna, Russia, 11—18 July, 2002. *Plenary Talk*.

LMS Northern Meeting and international workshop "Quantization, deformations, and new homological and categorical methods in mathematical physics". Manchester, 7-13 July 2001. *Invited talk*

**Reviewing:** Mathematical Reviews (1994–1996), Zentralblatt (2000—2003)

**Refereeing:** Lett.Math.Phys and Journal of Math. Physics.

**Editorial work:** member of editorial board of the Armenian Journal of Mathematics (since 2008).

## 4. RESEARCH ACTIVITY.

**Main area of research interests:** Mathematical problems of Quantum Field Theory, in particular geometry of supermanifolds

**Ph.D. thesis:**

My Ph.D. thesis was devoted to the following questions:

1. Investigation of objects which can be integrated over supersurfaces in superspace – generalization of differential forms on superspace [1,2,3,4,6].
2. Constructing of Poincaré-Cartan integral invariants for even symplectic structure on superspace [5] and analysis of normal forms of real surfaces in complex superspace [7]; these investigations were applied to problems of supergravity.

An exposition of the results of my thesis was published in [8].

**Geometry of odd bracket:** In 1986 I started the investigation of the geometry of supermanifolds endowed with odd symplectic structure and its application to quantum field theory. This geometry is natural framework of Batalin-Vilkovisky formalism. I was the first to give the invariant definition of the the BV "delta-operator" (see [14], also [12,13]). Since 1987 I

continued these investigations with my postgraduate student A.P. Nersessian [10—20]. In particular we give an interpretation of the Master Equation as the nilpotency condition and related BV formalism with integration theory on (super)manifolds.

For odd symplectic superspace a certain divergence-like operator and a non-trivial analogue of the Poincaré-Cartan integral invariant – a density that depends on second derivatives, – were constructed in [11,23]. These objects have no analogues in even symplectic geometry. They can be considered as superanalogues of the mean curvature of hypersurfaces.

In 1999 I defined a new canonical  $\Delta$ -operator on semidensities. This gives explicit geometrical picture on Batalin-Vilkovisky quantum and classical master-equation and fulfills the gap in the previous considerations. Then I performed a complete studying of the relations between semidenstities in  $(p,p)$ -dimensional symplectic supermanifolds and differential forms on  $(p,0)$ -dimensional Lagrangian supersurfaces [25,27,29,31].

**Geometry associated with differential operators:** Encouraging by results related with  $\Delta$ -operator on semidensity in a collaboration with T.Voronov I studied odd Laplacians on an supermanifold with odd Poisson structure. We obtained results which disclose deep relations between standard Riemannian and odd Poisson geometry [29]. Then we describe geometry of second order differential operators on an arbitrary manifold [30]. In particular we studied the pencil of second order operators acting on the space of densities of arbitrary weight, studied the peculiar role of semidensity and classify second-order odd differential operators on supermanifold [32,33].

Last two years I recommence the studying of operator pencil [43.] We began to analyze geometry of differential operators of arbitrary orders acting on algebra of densities. This work I do with my PhD student Adam Biggs.

**Generalization of Campbell-Hausdorff formulae:** I introduced a special class of algebras (so called  $CH$ -algebras), obtained a generalized Campbell-Hausdorff formula for them and applied it to the problem of connectivity of Feynman graphs in field theory [18] and statistical physics. Recent development has shown that this construction can be useful with the connection to homotopy algebras and their generalization.

**Linear algebra in supercase** With T.Voronov we studied Cayley-Hamilton like identities for linear operators in superspace. In particular we obtained new formulae expressing Berezinians (superdeterminant) of supermatrix as a rational function of supertraces [34, 35] and studied the meaning of numerator and denominator of this fraction in terms of resultant of polynomials. We obtained beautiful relations between recurrent sequences and traces of wedged products for linear operators in superspace. This can help to explain some peculiar properties of integration theory on supermanifolds.

**$p$ -homomorphisms** With T. Voronov we introduced the notion of  $p|q$ -symmetrical product of commutative algebras and  $p|q$ -homomorphisms [36,

38]. These constructions are on one hand natural generalisations of symmetric product of commutative algebras and Buchstaber-Rees  $p$ -homomorphisms and on the other hand are intimately related with invariants of linear operators in superspace. In particular using our approach we give the conceptually short proof of the main theorem about  $p$ -homomorphisms [42]<sup>1</sup>.

**Complexes related with calculus of variations. Cohomology in Physics:** In the papers [21,24] with my student D.A. Sahakyan I calculated the cohomological hierarchy in the space of Lagrangians which are defined on a given configuration space and which are weakly invariant w.r.t. a given symmetry algebra. These methods can be successfully used for the investigation of constrained systems and particularly in the BV formalism from the point of view of homological algebra [22,24]. In the paper [28] with Th.Th. Voronov we studied some geometrical aspects of jets geometry and investigated relations between different variational complexes.

**Other research:** I studied anomalies in field theory using the technique of Seeley coefficients (M.S. thesis, see also [9]).

### My projects.

I am planning to do the following:

1. Using formulae constructed for Berezinians in my previous work I plan to consider generalisation of tubes formula for hypersurfaces in superspace: The generating function of volume of tube will be a rational function (in the usual case it is polynomial). I will try to attack the problem of characteristic classes of supersurfaces analysing this rational function. There are mysterious relations between  $\zeta$ -function for arithmetic surfaces in algebraic number theory and characteristic functions for Berezinians in linear superalgebra. I am trying to analyse these relations and reveal the meaning of Frobenius map in terms of supermathematics. I did some preliminary work in [37].

2. To study the famous relations between Casimir operators for symplectic and orthogonal groups using technique of characteristic functions and parity reversing functors developed in my papers [34,35].

3. Encouraged by the works of Duval, Ovsienko and Lecompte (full symbols of differential operators equivariant with respect to projective transformations) and using the technique of operator pencils acting on algebra of

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<sup>1</sup>Buchstaber-Rees  $p$ -homomorphisms are linear maps which obey the special recurrent relations. Buchstaber and Rees proved the Theorem that for commutative associative algebras with unit  $A$  and  $B$  over real or complex numbers under some technical assumptions on  $B$ , there is a one-to-one correspondence between the algebra homomorphisms  $S^p A \rightarrow B$  and the  $p$ -homomorphisms  $A \rightarrow B$ . Here  $S^n A \subset A^{\otimes n}$  is the symmetric power of  $A$ . In particular, when  $A = C(X)$  for a compact Hausdorff space  $X$  and  $B = \mathbf{R}$ , this gives the following extension of the classical theorem of Gelfand & Kolmogorov (1939): for any  $n$ , the symmetric power  $\text{Sym}^n X = X \times \dots \times X$  is canonically embedded into the linear space  $C(X)^*$  so that the image of the embedding is the set of all  $n$ -homomorphisms  $C(X) \rightarrow \mathbf{R}$ . The proof of this remarkable result in Buchstaber & Rees (2002) is a tour de force of combinatorial ingenuity.)

densities (my previous works on BV formalism with T.Voronov) I put and study the problem of  $G$ -lifting the operators acting on space of densities of given weight to the operator pencils acting on whole algebra of densities. We study the cases where  $G$  is a subgroup of projective (or conformal) or volume preserving, or whole group all diffeomorphisms.

## 5. TEACHING.

During my life from 1978 till now I taught different courses in Moscow, Yerevan and Manchester in Mathematical and Theoretical Physics and in Mathematics: Electrodynamics, Quantum Mechanics, Differential Geometry, Applications of Differential Geometry in Theoretical Physics, Group Theory, Homological methods in Physics, Galois Theory, Elements of Functional analysis e.t.c. Now I teach the new course "Introduction in Geometry" for second years students and this year I will teach also the new course "Riemannian Geometry"

### **Supervision of research students:**

Last 7 years I share my PHD students with Ted Voronov. I supervised these years 6 PhD students. Four of them already finished their thesis.

One of my former PhD students (Armen Nersessian) nowadays is the leading researcher in mathematical physics in Yerevan, Armenia.

I regularly supervised projects of undergraduate and master students in Galois Theory and Differential Geometry.

I was four times internal examiner and once the external examiner (Aberdeen 2010) in PHD oral examinations.

I make regularly projects with foundation year students.

## 6. Social Activity.

1. From 2001 I am helping on the regular basis in organising weekly sessions of Manchester Geometry Seminar

2. From 2003 till 2006 I was responsible for organising staff development process in our Department.

3. From 2007 till 2010 I was a member of promotion committee in the School of Mathematics.

4. I am actively interesting in the process of mathematical education of children in UK. I prepared the talk "Euler Theorem for polyhedra" which I gave many years during interview days for sixthformers. In March 2005 I participated in the conference "Where will the next generation of UK mathematicians come from?"

In February 2008 and April 2012 I had lectures for general audience: "Tubes formula",

5. Now I am fire marshal in our School.

## 7. PUBLICATIONS.

1. A.V. Gayduk, O.M. Khudaverdian, A.S. Schwarz. *Multiplicative Functionals on Curves, Additive Functionals on Surfaces; their significance in QFT*. In Proceedings: "Group Theor. Methods in Physics", vol. 2, p. 201-205, Zvenigorod 1979.
2. O.M. Khudaverdian, A.S. Schwarz. *A Few Comments on the String Representation of Gauge Fields*. Phys. Lett. v. 91B (1980), p. 107-110.
3. O.M. Khudaverdian, A.S. Schwarz. *Additive and Multiplicative Functionals*. Preprint ITEP-3-1980.
4. O.M. Khudaverdian, A.S. Schwarz. *Multiplicative Functionals and Gauge fields*. Theor. Math. Phys. (in Russian), v. 46 (1981) p. 187-198 (transl. into English: p. 124-132).
5. O.M. Khudaverdian, A.S. Schwarz, Yu.S. Tyupkin. *Integral invariants for Supercanonical Transformations*. Lett. Math. Phys., v. 5 (1981), p. 517-522.
6. A.V. Gayduk, O.M. Khudaverdian, A.S. Schwarz. *Integration over Surfaces in Superspace*. Theor. Math. Phys. (in Russian), v. 52 (1982), p. 375-383 (transl. into English: p. 862-868).
7. O.M. Khudaverdian, A.S. Schwarz. *Normal Gauge in Supergravity*. Theor. Math. Phys., v. 57 (1983), p. 354-362 (transl. into English: p. 1189-1195).
8. O.M. Khudaverdian, A.V. Rosly, A.S. Schwarz. *Supergravity and Complex Geometry*. In book: News of Science and Technics. Modern Problems of Mathematics. v. 9, 1986, p. 247-284 (in Russian) (transl. into English: "Encyclopedia of Modern Mathematics", Springer-Verlag).
9. O.M. Khudaverdian, R.L. Mkrtchian, L.A. Zurabian. *On the Axial Anomalies in External Tensor Fields*. Theor. Math. Phys. v. 71 (1987) p. 393-401.
10. O.M. Khudaverdian, A.P. Nersessian. *Formulation of Hamiltonian Mechanics with Even and Odd Poisson Bracket*. Preprint EFT 1031-81(87), Yerevan (1987).
11. O.M. Khudaverdian, R.L. Mkrtchian. *Integral Invariants of Buttin Bracket*. Lett. Math. Phys. v. 18 (1989), p. 229-231 (Preprint EFI-918-69-86- Yerevan (1986)).
12. O.M. Khudaverdian, A.P. Nersessian. *Superspaces with Odd and Even Canonical Two-Forms and the Strange Superalgebra*. Izv. Acad. Nauk Arm. SSR, v. 24, No. 6, (1989) p. 288-294 (transl. into English: Soviet Journal of Contemp. Phys., v. 24 No.6, p. 22-27).
13. O.M. Khudaverdian, A.P. Nersessian. *The Supergeneralization of  $CP(N)$  as Reduced Phase Space of Super-Hamiltonian Systems*. Izv. Acad.



Nauk Arm. SSR, v. 25, No. 6, (1990) p. 330-337 (transl. into English: Soviet Journal of Contemp. Phys., v. 25 No.6.)

14. O.M. Khudaverdian. *Geometry of Superspace with Even and Odd Brackets*. J. Math. Phys. v. 32 (1991) p. 1934-1937 (Preprint of the Geneva University, UGVA-DPT 1989/05-613).

15. O.M. Khudaverdian, A.P. Nersessian. *Canonical Poisson Brackets of Different Grading and Strange Superalgebras*. J. Math. Phys. v. 32 (1991) p. 1938-1941 (Preprint of the Geneva University, UGVA-DPT 1989/05-614).

16. O.M. Khudaverdian, A.P. Nersessian. *Even and Odd Symplectic and Kählerian Structures on Projective Superspaces*. J. Math. Phys. v. 34 (1993), p. 5533-5548.

17. O.M. Khudaverdian, A.P. Nersessian. *On Geometry of Batalin-Vilkovisky Formalism*. Mod. Phys. Lett. A, v. 8 (1993), No. 25, p. 2377-2385.

18. O.M. Khudaverdian. *Algebras with Operator and Campbell-Hausdorff Formula*. Lett. Math. Phys., v. 35 (1995), pp.27-38.

19. O.M. Khudaverdian. *Batalin-Vilkovisky Formalism and Odd Symplectic Geometry*. In: Proceedings of International Workshop "Geometry and Integrable Systems", P.N.Pyatov and S.N.Solodukhin, eds. World Scientific Publishing Co., 1996, p. 144-181.

20. O.M. Khudaverdian, A.P. Nersessian. *Batalin-Vilkovisky Formalism and Integration Theory on Manifolds*. J. Math. Phys., v. 37 (1996), p. 3713-3724.

21. O.M. Khudaverdian, D.A. Sahakyan. *Cohomological Aspects of Noether Theorem for Lagrangians of Classical Mechanics*. Proceedings of the conference "Secondary calculus and Cohomological Physics", Moscow, 1997, in Electronic Proceedings of EMIS, <http://www.emis.proceedings/SCCP97>

22. O.M. Khudaverdian. *Algebraic and Geometric Aspects of Constrained Systems*. In survey: "Collaboration JINR-YSU (1992-1997)", JINR E-98-12, Dubna (1998).

23. O.M. Khudaverdian. *Odd Invariant Semidensity and Divergence-like Operators on Odd Symplectic Superspace*. Comm. Math. Phys., v. 198 (1998), p. 591-606.

24. O.M. Khudaverdian, D.A. Sahakyan. *Double Complexes and Cohomological Hierarchy in the Space of Weakly Invariant Lagrangians of Mechanics*. Acta Applicandae Mathematicae., v. 56 (2/3), (1999), p. 181-215.

25. O.M. Khudaverdian. *Delta-Operator on Semidensities and Integral Invariants in the Batalin-Vilkovisky Geometry*. Preprint of Max-Planck-Institut für Mathematik, MPI-135 (1999), Bonn.

26. O.M. Khudaverdian. *Evolution of oscillator wave function and Fourier transformation*. In: “Symmetries and Integrable Systems”, collected papers. A.N. Sissakian, ed., Dubna, 2000, p. 269–272.
27. H.M. Khudaverdian, T.Voronov *On complexes related with calculus of variations.*, J. Geom. Phys. 44 (2-3) (2002), 221-250
28. H.M. Khudaverdian *Laplacians in odd symplectic geometry*.— In *Quantization, Poisson Brackets and Beyond*, Theodore Voronov, ed., Contemp. Math., Vol. 315, Amer. Math. Soc., Providence, RI, 2002, pp. 199-212.
29. H.M. Khudaverdian, T.Voronov *On Odd Laplace operators..* Lett. Math. Phys. 62 (2002), 127-142
30. H.M. Khudaverdian, T.Voronov *Geometry of differential operators, and odd Laplace operators.* Russian Math. Surveys 58 (2003)
31. H.M. Khudaverdian. *Semidensities on odd symplectic supermanifold.*, Comm. Math. Phys., v. 247 (2004), pp. 353-390
32. H.M. Khudaverdian, T.Voronov *On odd Laplace operators. II.* In book: *Geometry, Topology and Mathematical Physics. S. P. Novikov’s seminar: 2002 - 2003*, V. M. Buchstaber, I. M. Krichever, eds., Amer. Math. Soc. Transl. (2), Vol. 212, 2004, pp.179–205
33. H.M. Khudaverdian, T.Voronov *Geometry of differential operators, odd Laplacians, and homotopy algebras* Journal of Nonlinear Math. Phys. **11**, Supplement (2004), pp. 217–227. arXiv:math.DG/0402292
34. H.M. Khudaverdian, T.Voronov. *New facts about Berezinians.* In book: *Supersymmetries and Quantum Symmetries 2005*. Proceedings of International Workshop, Joint Institute of Nuclear Research, Dubna, 27-31 July 2005, E. Ivanov and B. Zupnik, eds., Dubna, 2006, 393-398, arXiv:math-ph/0512031.
35. H.M. Khudaverdian, T.Voronov. *Berezinians, Exterior Powers and Recurrent Sequences.*— Lett. Math. Phys. (Berezin memorial volume), 74 (2005), 201-228 (arXiv:math.DG/0309188)
36. H.M. Khudaverdian, T.Voronov. *On generalized symmetric powers and a generalization of Kolmogorov-Gelfand-Buchstaber-Rees theory.* Russian Mathematical Survey 2007, arXiv:math.RA/0612072.
37. H.M. Khudaverdian. *Tube formula, Berezinians and Dwork formula.* Journal of Geometry and Symmetry in Physics, v10, 2007, pp.29–40, arXiv:math.DG/0402292
38. H.M. Khudaverdian, T.Voronov. *Operators on superspaces and generalizations of the Gelfand-Kolmogorov theorem.* In: XXVI Workshop on Geometric Methods in Physics. Bialowieza, Poland, 1 - 7 July 2007. AIP Conference Proceedings 956, Melville, New York, 2007, p. 149-155. arXiv:0709.4402 [math-ph].

39. H.M. Khudaverdian, T.Voronov. *Differential forms and odd symplectic geometry*. Amer. Math. Soc. Transl (2) Vol 224, 2008 pp.159—171
40. H.M. Khudaverdian, T.Voronov. *Higher Poisson brackets and differential forms*. In: Geometric Methods in Physics. AIP Conference Proceedings 1079, American Institute of Physics, Melville, New York, 2009, 203-215. arXiv:0808.3406v2 [math-ph].
41. A. Borovik, O.M. Khudaverdian. *Merkator projection, logarithm and...*(in Russian) Matematikoeskoe Prosvechenie no. 14 (2010), 58–82.
42. H.M. Khudaverdian, T.Voronov. *On a short proof of Buchstaber—Rees Theorem*. Phil. Trans. R. Soc. A. (2011).
43. H.M. Khudaverdian, T.Voronov. *Second order operators on the algebra of densities and a groupoid of connections* MAX Planck Institut fur Mathematik. Preprint 2011 (73) (math-archive—. arXiv:1112.5379 []). It is published in the book: “Astrophysics, Gravitation and Quantum Physics”. *A volume in honour of academician Edvard Chubaryan. Editor A.A. Saharian, Yerevan State University Publishing House, Yerevan, 2012. ISBN 978-5-8084-1579-9. Number of pages 294. (The pages of this paper are 171-205.)*