

I will define metaplectic in a way similar to spinor group.

Consider the vector space $V \oplus V^*$ with canonical symplectic form $< , >$.

Let $\hat{a} = \hat{a}_{\mathbf{X}}$ be a linear operator which is canonically assigned to the vector \mathbf{R} , such that

$$[\hat{a}_{\mathbf{X}}, \hat{a}_{\mathbf{Y}}] = < \mathbf{x}, \mathbf{Y} > . \quad (1)$$

We consider transformations on the space of functions on V such that for an arbitrary $\mathbf{X} \in V \oplus V^*$,

$$S^{-1} a_{\mathbf{X}} S = a_{F(\mathbf{X})} \quad (2)$$

One can see that for an arbitrary vectors $\mathbf{X}, \mathbf{Y} \in V \oplus V^*$,

$$< \mathbf{X}, \mathbf{Y} > = \langle F(\mathbf{X}), F(\mathbf{Y}) \rangle .$$

Thus we define the group of transformations of space of the functions on V , metaplectic group, and its epimorphism on symplectic group.

Now instead V consider the space C^n , and assign to every vector \mathbf{X} , the matrix $M_{\mathbf{X}} = X^m \gamma_m$.

We have instead equation (1) the following relation:

$$[M_{\mathbf{X}}, M_{\mathbf{Y}}]_+ = 2 < \mathbf{x}, \mathbf{Y} > . \quad (1a)$$

where $[,]_+$ is the anticommutator, and $< , >$ now is the scalar product.

Now instead equation (2) we come to consider transformations O on the space matrices such that for an arbitrary $\mathbf{X} \in C^n$

$$O^{-1} M_{\mathbf{X}} O = M_{F(\mathbf{X})} \quad (2a)$$

One can see that for an arbitrary vectors \mathbf{X}, \mathbf{Y} ,

$$< \mathbf{X}, \mathbf{Y} > = \langle F(\mathbf{X}), F(\mathbf{Y}) \rangle .$$

Thus we define the group of spinor transformations and its epimorphism on orthogonal group.