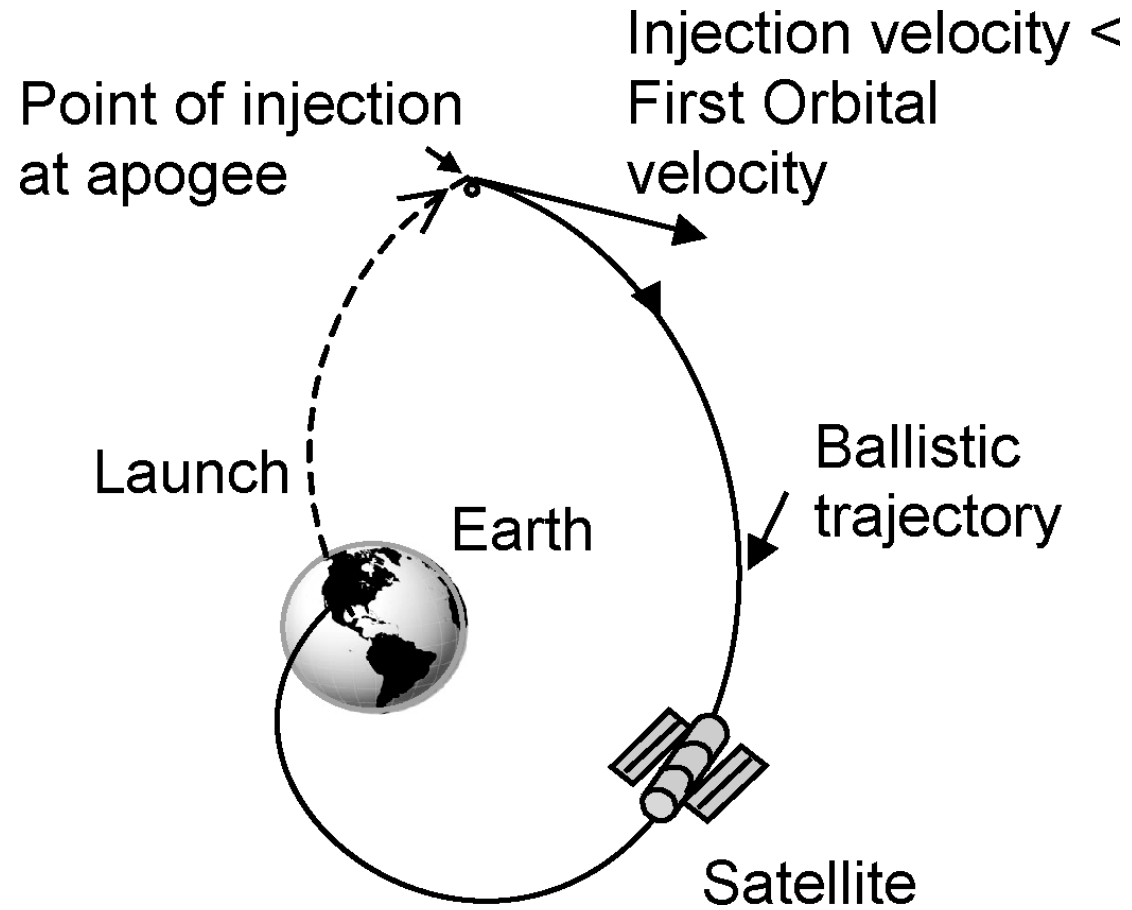


Launch and Maneuvers

SPACE
INFORMATICS

Satellite Injection Velocity

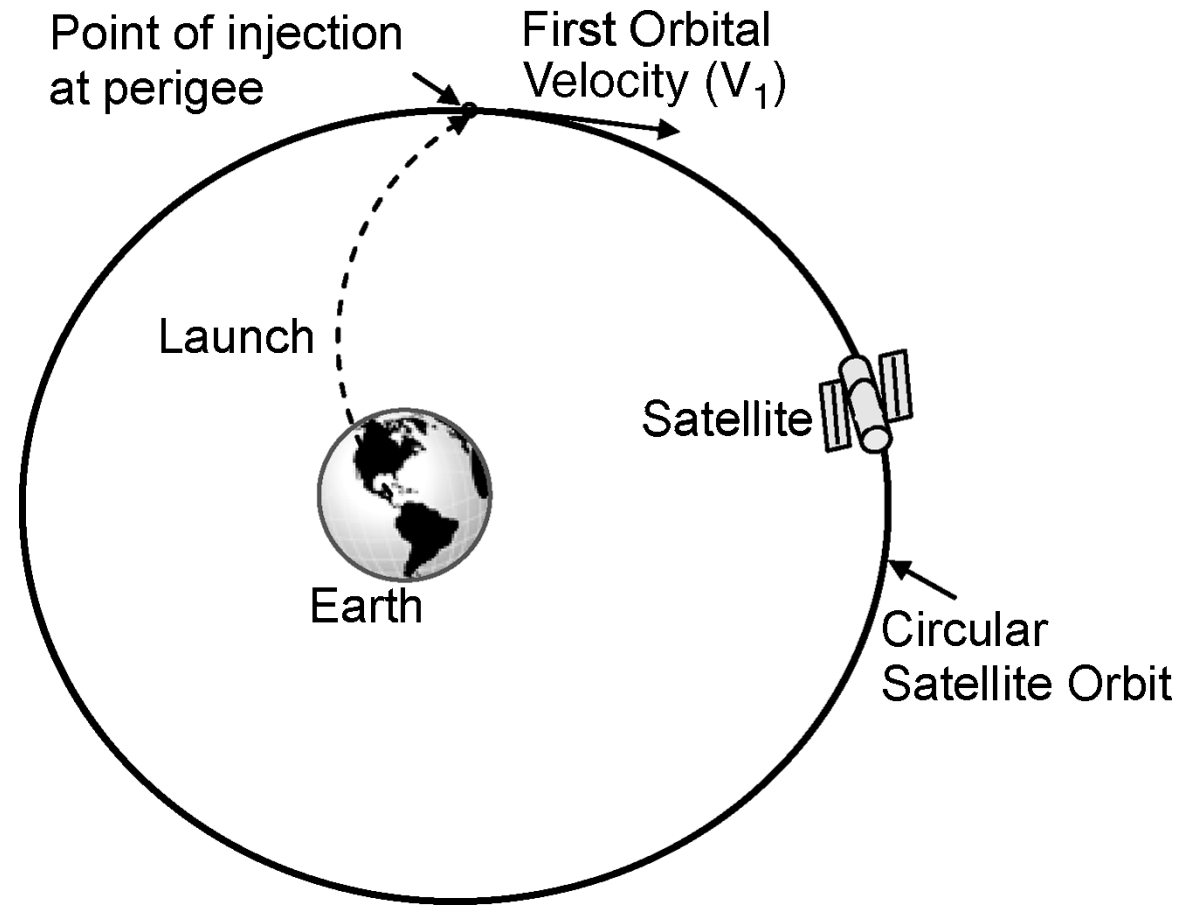
Injection Velocity – Low Speed



Satellite injection at a slow speed

Satellite Injection Velocity

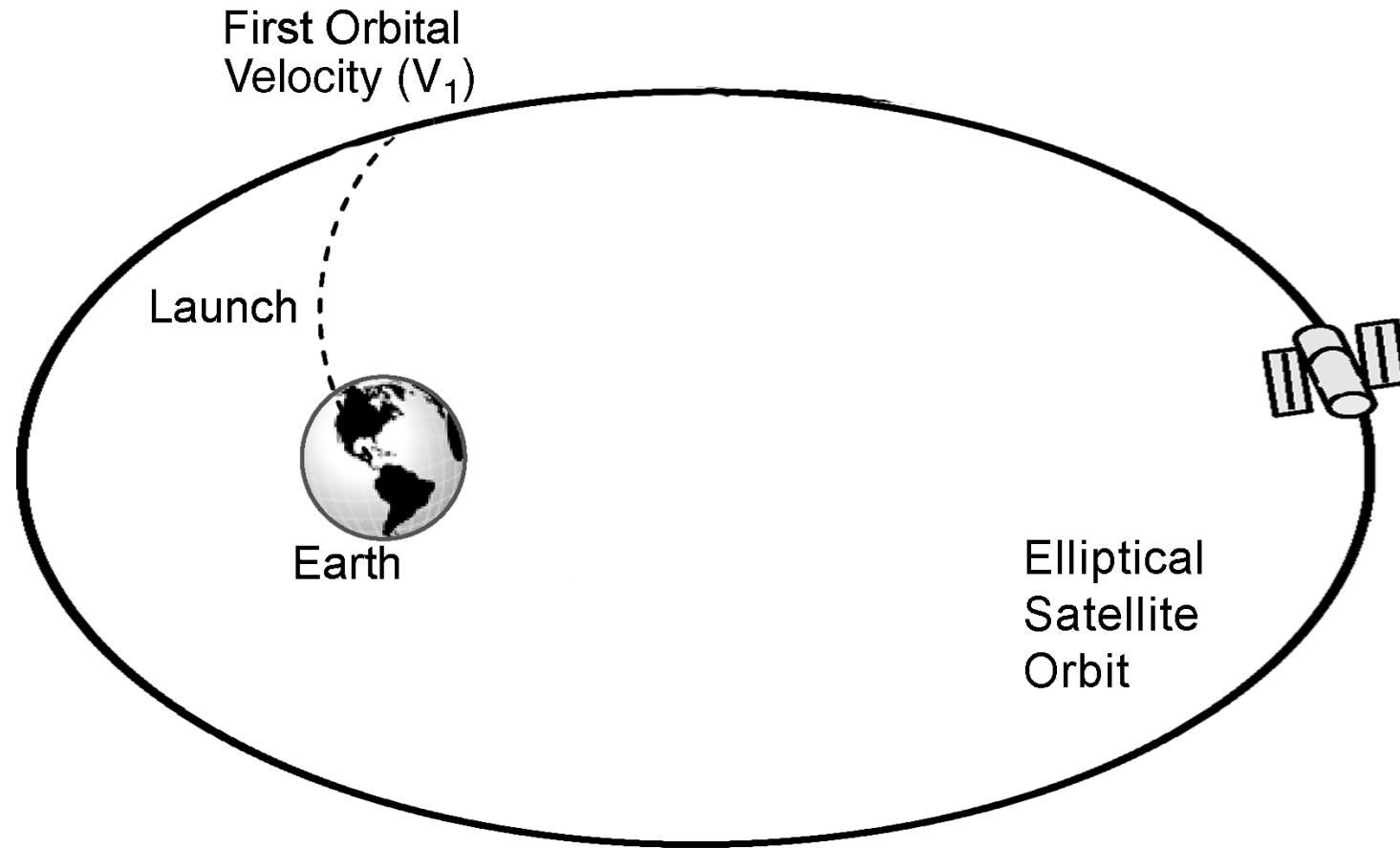
Injection Velocity – Medium Speed



Satellite injection at a medium speed

Satellite Injection Velocity

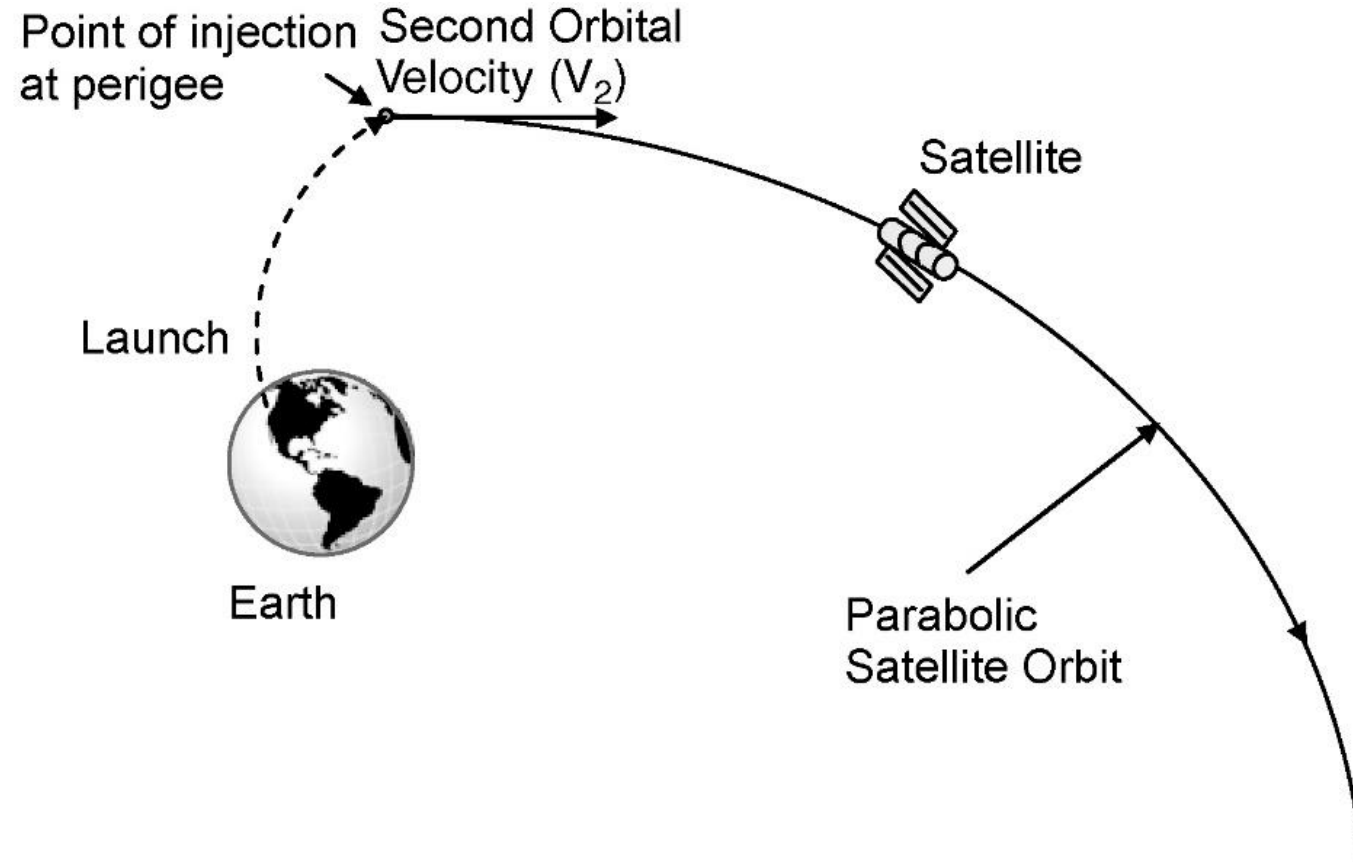
Injection Velocity – High Speed



Satellite injection at a high speed

Satellite Injection Velocity

Injection Velocity – Very High Speed



Satellite injection at a very high speed

Satellite Injection Velocity

Orbit Velocity

We have said that **velocity** in an **elliptical orbit** with apogee and perigee distances of r_a and r_p and semi-major axis $a = (r_p + r_a)/2$ is

$$v(r) = \sqrt{\frac{2\mu}{r} - \frac{\mu}{a}} = \sqrt{\frac{2\mu}{r} - \frac{2\mu}{r_p + r_a}}$$

Notably, in a **circular orbit** with radius $R = r_p = r_a$

$$v(r) = \sqrt{\frac{\mu}{R}}$$

$$(*) \mu = 3.986013 \times 10^5 \text{ km}^3/\text{s}^2$$

Satellite Injection Velocity

Formally Speaking

- If the injection velocity at height r is
 - $v < \sqrt{\mu/r}$, the satellite follows a **ballistic** trajectory and falls
 - $v = \sqrt{\mu/r}$, the satellite stays in a **circular** orbit of radius r
 - $v > \sqrt{\mu/r}$ but $v < \sqrt{2\mu/r}$, we have an **elliptical** orbit ($e \in (0; 1)$)
 - $v = \sqrt{2\mu/r}$, the satellite follows a **parabola** ($e = 1$)
 - The apogee becomes ∞
 - This is the Earth's **escape** velocity
 - $v > \sqrt{2\mu/r}$, the trajectory is **hyperbolic**

Satellite Injection Velocity

Try this on STK



- Use **Astrogator** in **STK** to:
 - Create a new satellite with **Astrogator** as the propagator
 - Set initial state in **Earth Inertial Cartesian Coordinates** (6678 km, 0, 0)
 - Apply velocity in z axis only (V_z) and explore velocity ranges considering the following inflexion points:

$$\begin{aligned} \blacksquare v_{z1} &= \sqrt{\frac{\mu}{r}} = \sqrt{\frac{3.986013 \times 10^5}{6678}} = 7.72 \text{ km/s} \\ \blacksquare v_{z1} &= \sqrt{\frac{2\mu}{r}} = \sqrt{\frac{2 \times 3.986013 \times 10^5}{6678}} = 10.93 \text{ km/s} \end{aligned}$$

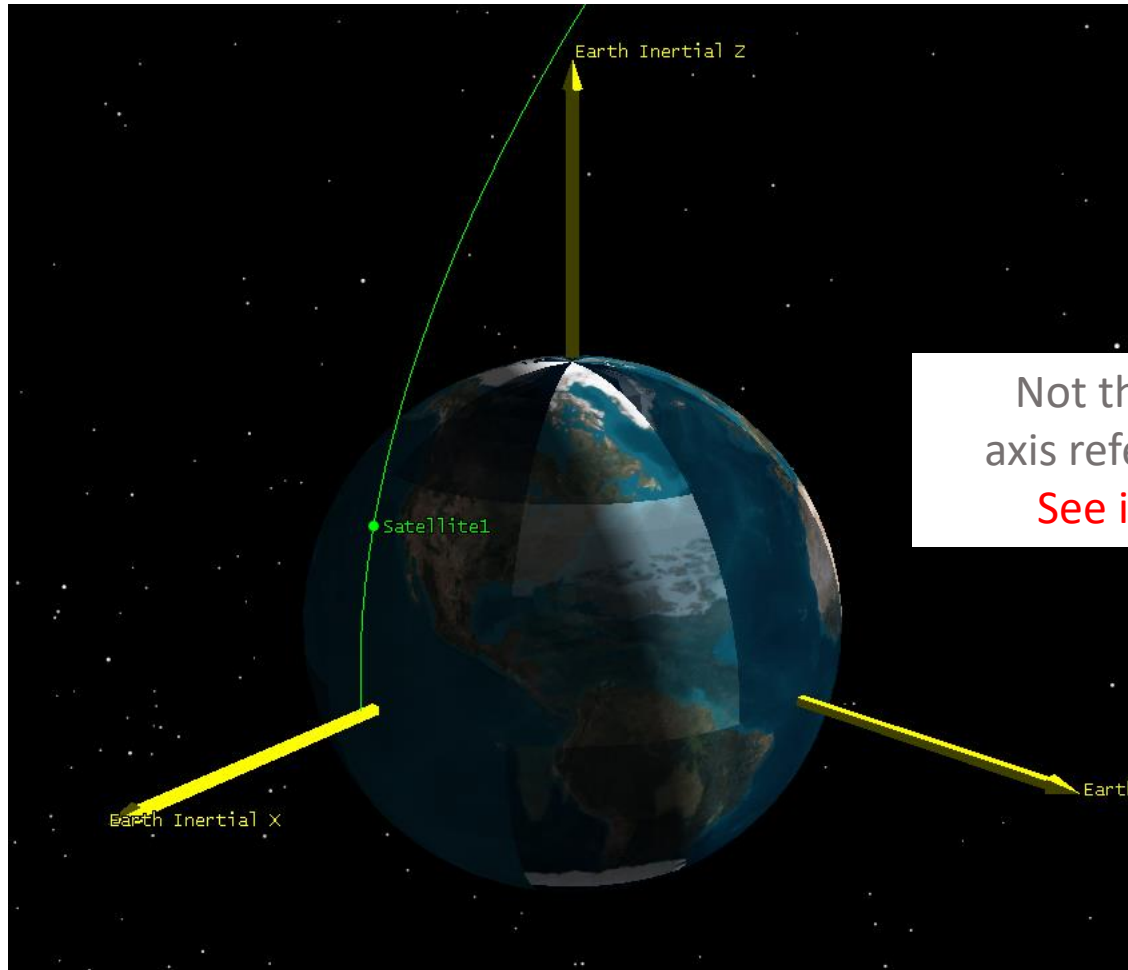
- → show in STK (Stk_Initial_Velocity.vdf)

6,371 + 307 km

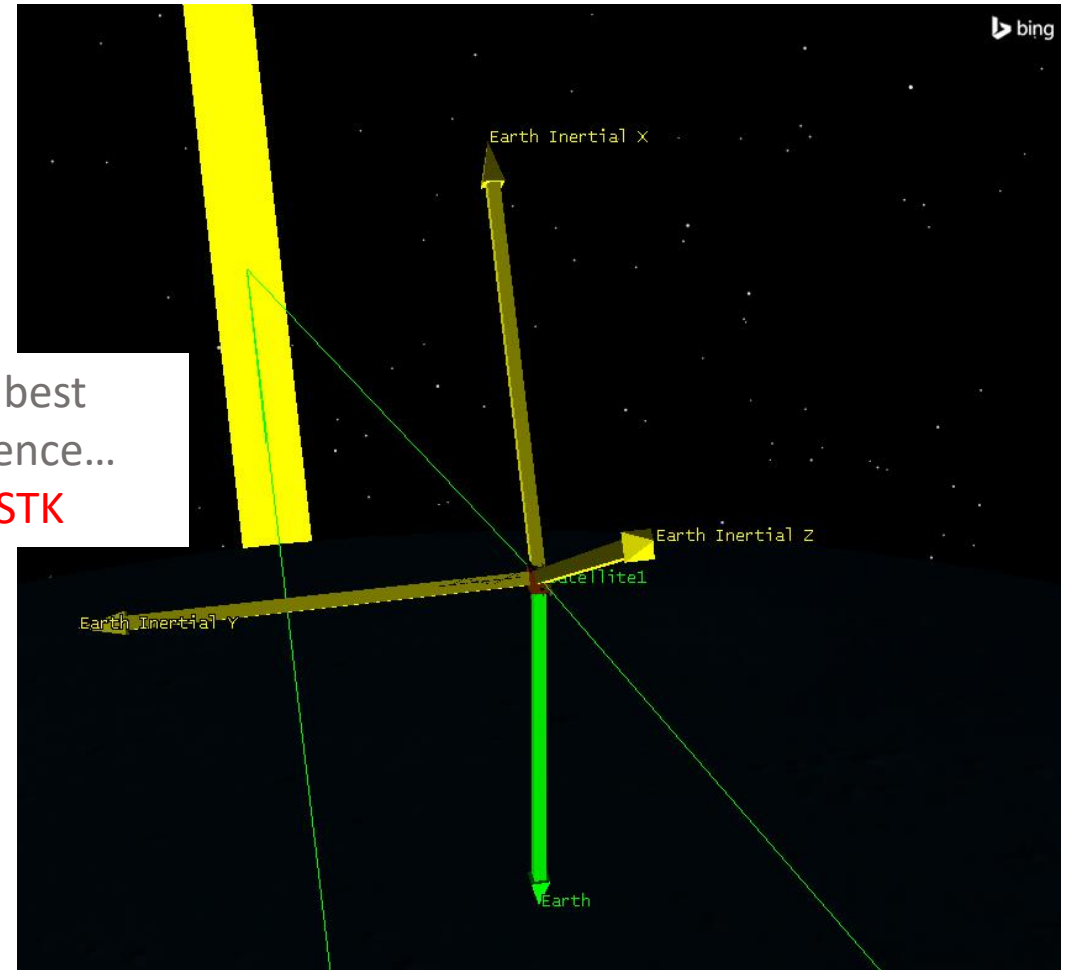
Coord.System:	Earth Inertial
Coordinate Type:	Cartesian
Orbit Epoch:	19 Aug 2019 10:00:00.000 UTCG
X Component:	6678.14 km
Y Component:	0 km
Z Component:	0 km
Vx Component:	0 km/sec
Vy Component:	0 km/sec
Vz Component:	10.93 km/sec

Satellite Injection Velocity

Try this on STK



Not the best
axis reference...
See in STK



Satellite Injection Velocity

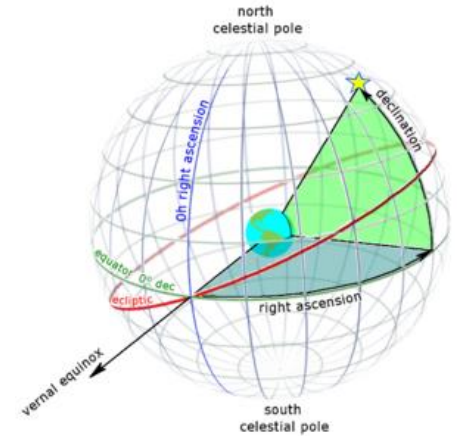
Cosmic Velocities

- $v_1 = \sqrt{\mu/r}$ is known as the **first cosmic velocity**
 - The required velocity not to fall to Earth
- $v_2 = \sqrt{2\mu/r}$ is known as the **second cosmic velocity**
 - The required velocity to escape from Earth
- $v_3 = \sqrt{2GM/R}$ is known as the **third cosmic velocity**
 - The required velocity to escape from the Solar System
 - Where M is the mass of the central object (e.g., Sun)
 - And R is the distance from the center of the celestial body to the point of escape (e.g., distance from the Sun to the object trying to escape its gravitational pull)
- The **fourth cosmic velocity**: galaxy escape velocity...

Satellite Injection Velocity

Cosmic Velocities – Solar System Escape

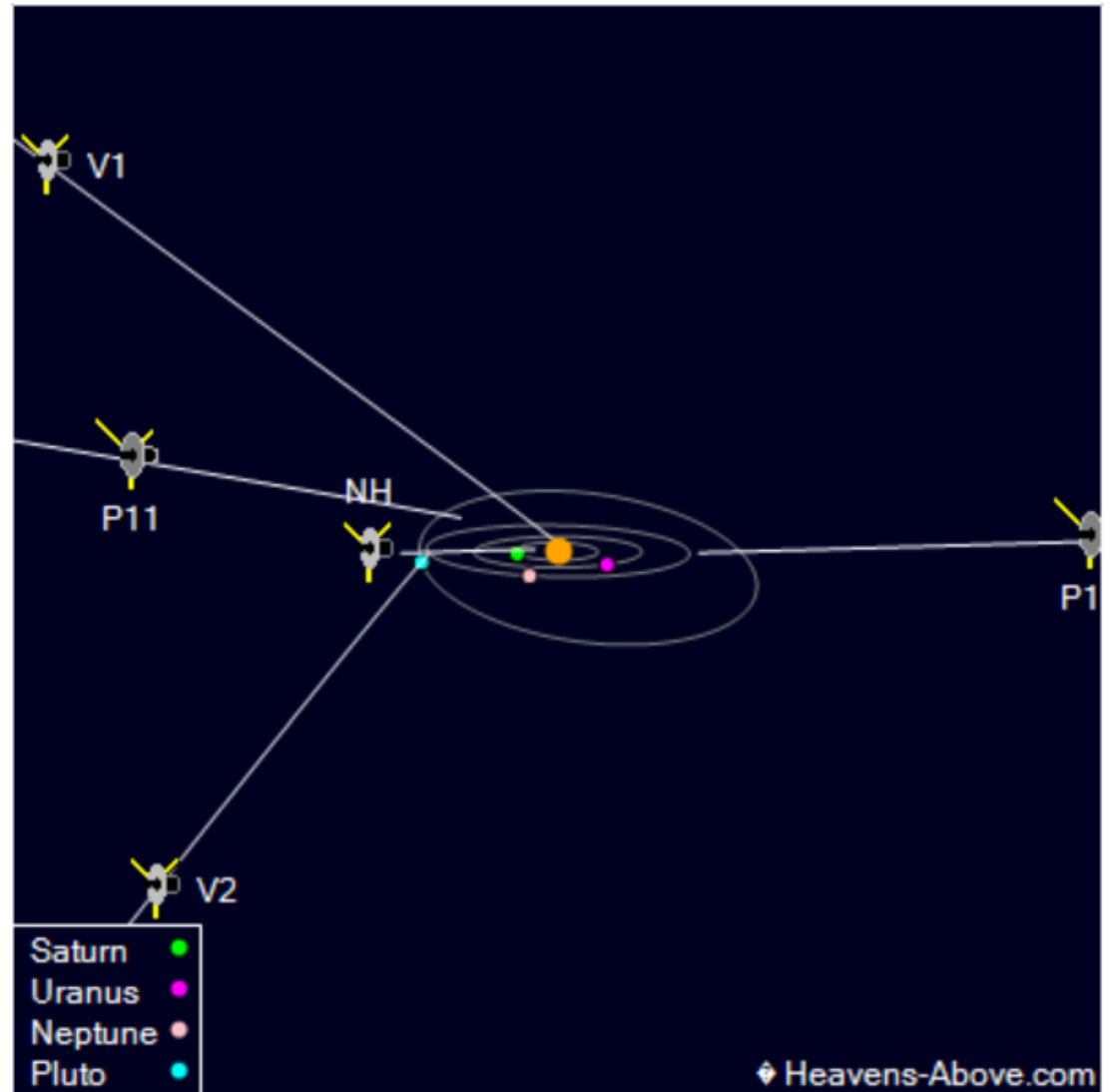
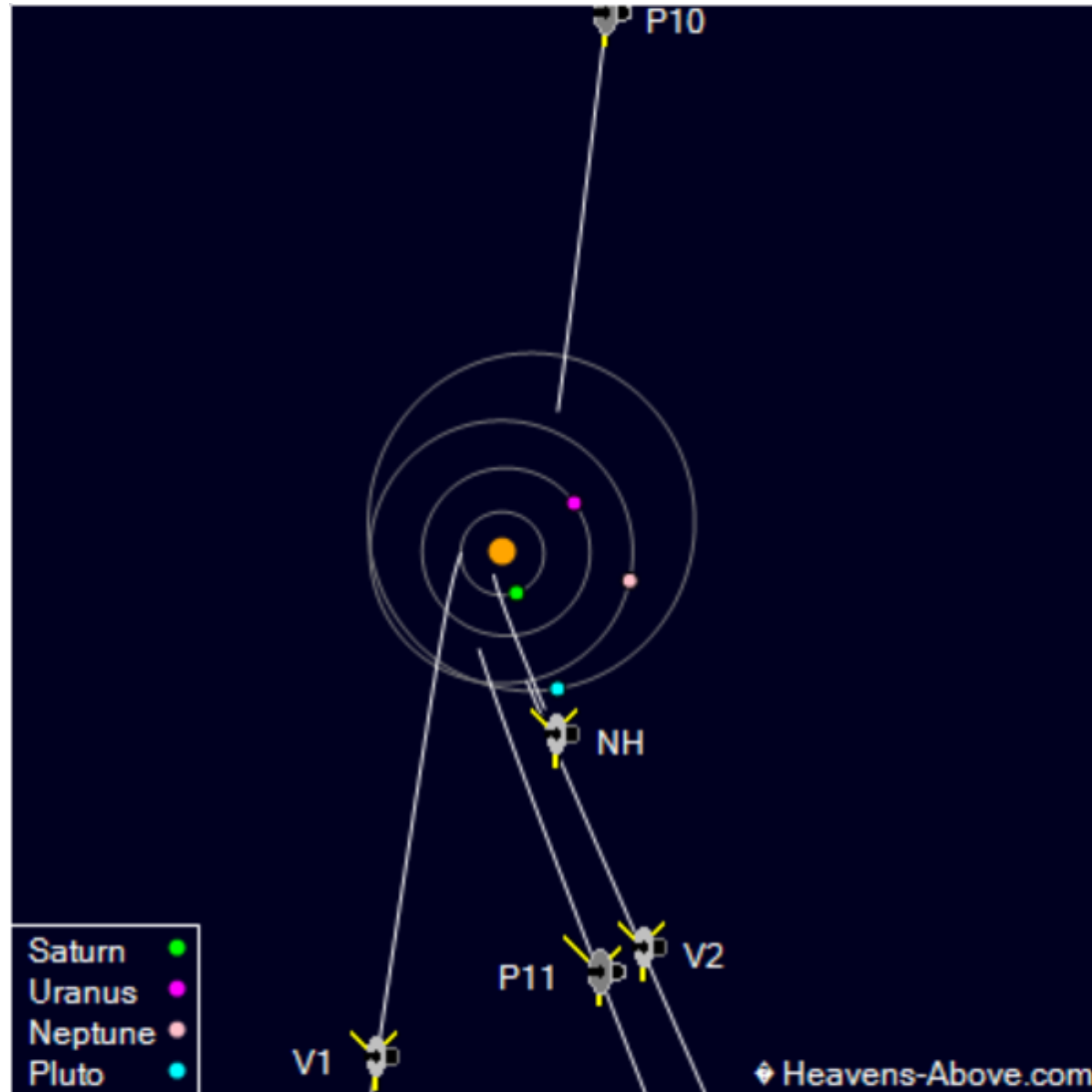
- **Five** spacecraft are leaving the Solar System
- Voyager 1: about **70,000 years** to reach the nearest star



	Pioneer 10	Pioneer 11	Voyager 2	Voyager 1	New Horizons
Distance from Sun (AU)	124.318	102.890	121.665	146.820	45.303
Speed relative to Sun (km/s)	11.938	11.231	15.330	16.970	14.007
Speed relative to Sun (AU/year)	2.518	2.369	3.234	3.580	2.955
Ecliptic latitude	3°	14°	-37°	35°	2°
Declination	26° 0'	-8° 50'	-58° 24'	12° 15'	-20° 35'
Right ascension	5 ^h 13 ^m	18 ^h 49 ^m	19 ^h 59 ^m	17 ^h 12 ^m	19 ^h 5 ^m
Constellation	Taurus	Scutum	Pavo	Ophiuchus	Sagittarius
Distance from Earth (AU)	124.347	102.475	121.242	146.844	44.826
One-way light time (hours)	17.24	14.20	16.81	20.35	6.21
Brightness of Sun from spacecraft (Magnitude)	-16.2	-16.6	-16.3	-15.9	-18.4
Spacecraft still functioning?	no	no	yes	yes	yes
Launch date	1972-Mar-03	1973-Apr-06	1977-Aug-20	1977-Sep-05	2006-Jan-19

Satellite Injection Velocity

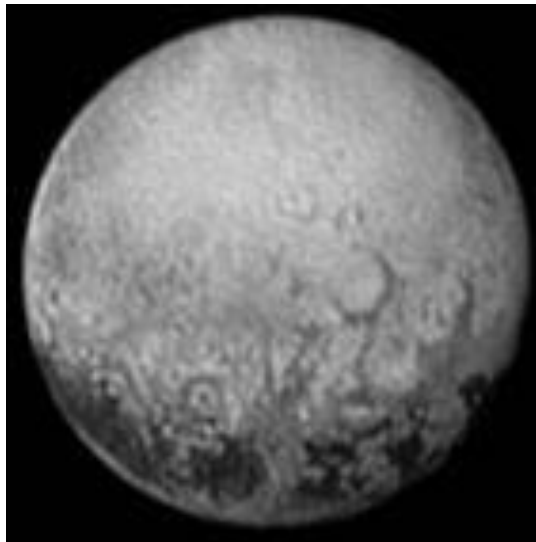
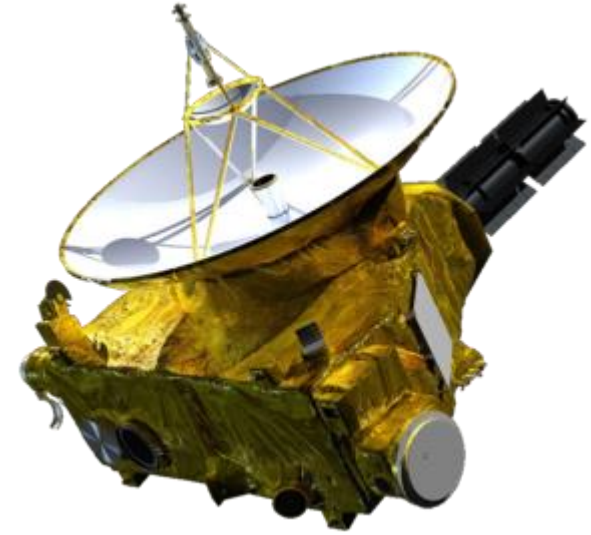
Cosmic Velocities – Solar System Escape



Satellite Injection Velocity

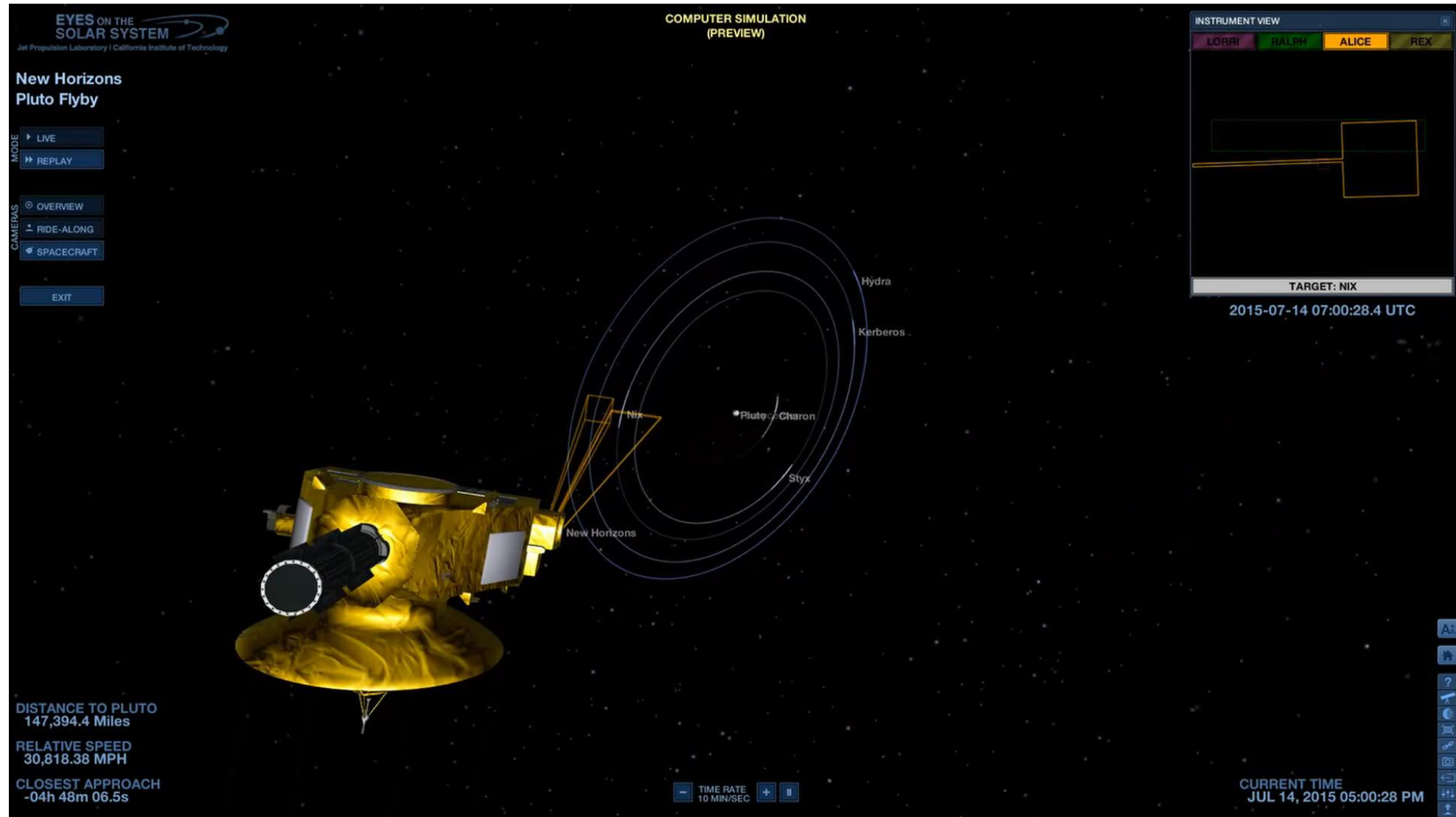
Cosmic Velocities – Solar System Escape

- **New Horizon**
- Launch mass: 478 kg – $2.2 \times 2.1 \times 2.7$ m
- The first spacecraft to explore Pluto
 - Finest images from the dwarf planet
 - Now headed to Kuiper belt



Satellite Injection Velocity

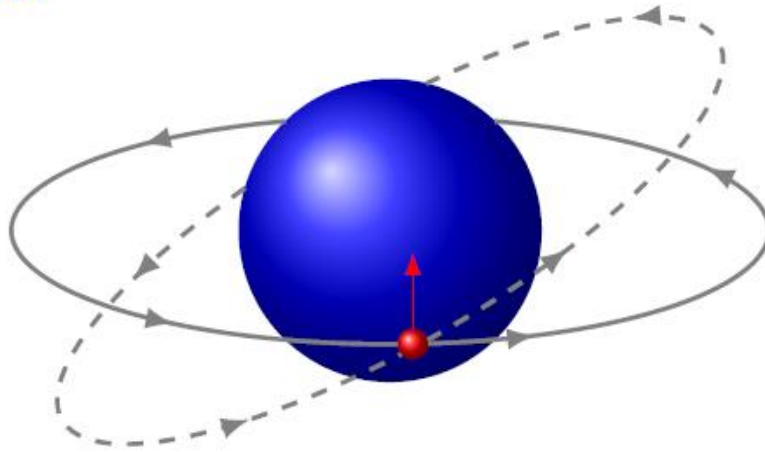
Cosmic Velocities – Solar System Escape



Maneuvers

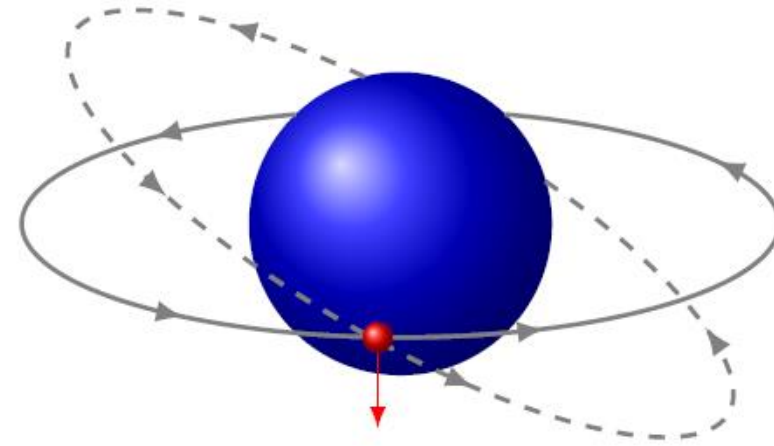
Normal and Anti-Normal Burns

Normal



Acceleration with 90° to the orbital plane.

Anti-Normal



Acceleration with -90° to the orbital plane.

Properties

- It can be used to change *inclination* (if the maneuver is performed in the ascending/descending nodes) as well as to perform *RAAN* angle changes (if the maneuver is performed in the north/south extreme of the orbit).

Maneuvers

Normal and Anti-Normal Burns

- A small change Δi to the inclination angle i of a **circular orbit** can be affected externally by applying a thrust Δv to the velocity vector V at an angle of $90^\circ + \Delta i / 2$ to the direction of the satellite

$$\Delta v = 2V \sin\left(\frac{\Delta i}{2}\right)$$

Maneuvers

Normal and Anti-Normal Burns – Simple Inclination Change

- Use **Astrogator** in **STK** to:
 - Create a new satellite with **Astrogator** as propagator
 - Set initial state in **Earth Inertial Cartesian Coordinates** (6678 km, 0, 0)
 - Apply velocity in z axis only (V_z) of 7.72 km/s
 - Propagate until ascending node
 - Set maneuver to **Thrust Vector** in **VNC (Earth)** coordinates
 - Configure impulse to change $\Delta i = 10^\circ$
 - Magnitude $\Delta v = ?$
 - Angle at $90^\circ + \Delta i / 2 = 95^\circ$
 - $\Delta_x = ?$
 - $\Delta_y = ?$
 - → show in STK (Stk_Inclination_change.vdf)

6,371 + 307 km



Maneuvers

Normal and Anti-Normal Burns – Simple Inclination Change

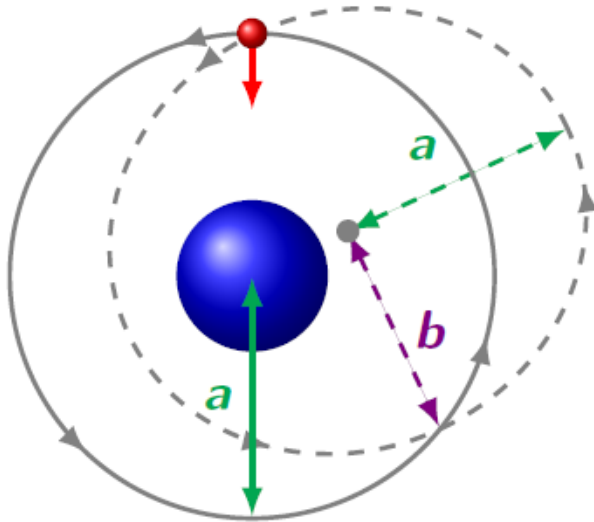
- Use **Astrogator** in **STK** to:
 - Create a new satellite with **Astrogator** as propagator
 - Set initial state in **Earth Inertial Cartesian Coordinates** (6678 km, 0, 0)
 - Apply velocity in z axis only (V_z) of 7.72 km/s
 - Propagate until ascending node
 - Set maneuver to **Thrust Vector** in **VNC (Earth)** coordinates
 - Configure impulse to change $\Delta i = 10^\circ$
 - Magnitude $\Delta v = 2\sqrt{\mu/r} \sin(\Delta i/2) = 2 \times 7.726 \times 0.0871 = 1.345 \text{ km/s}$
 - Angle at $90^\circ + \Delta i/2 = 95^\circ$
 - $\Delta_x = \cos(95^\circ) \times \Delta v = -0.0871 \times 1.345 = -0.1172 \text{ km/s}$
 - $\Delta_y = \sin(95^\circ) \times \Delta v = 0.9961 \times 1.345 = 1.3398 \text{ km/s}$
- → show in STK (Stk_Inclination_change.vdf)

6,371 + 307 km

Maneuvers

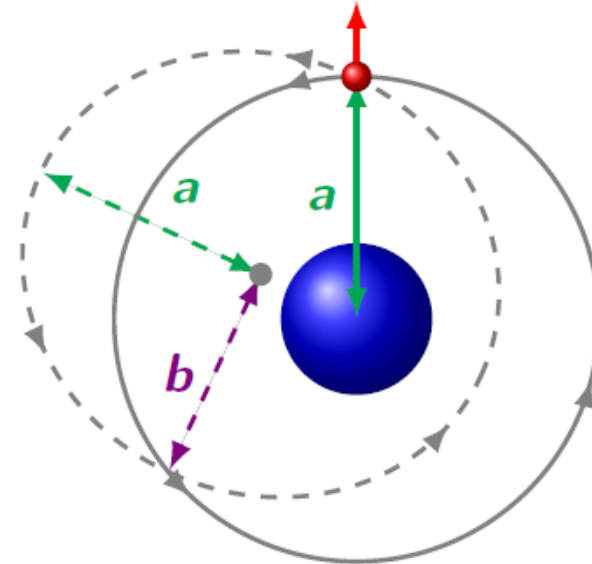
Radial Burns

Radial-In



Acceleration **towards** the center of the orbit.

Radial-Out



Acceleration **away from** the center of the orbit.

Properties

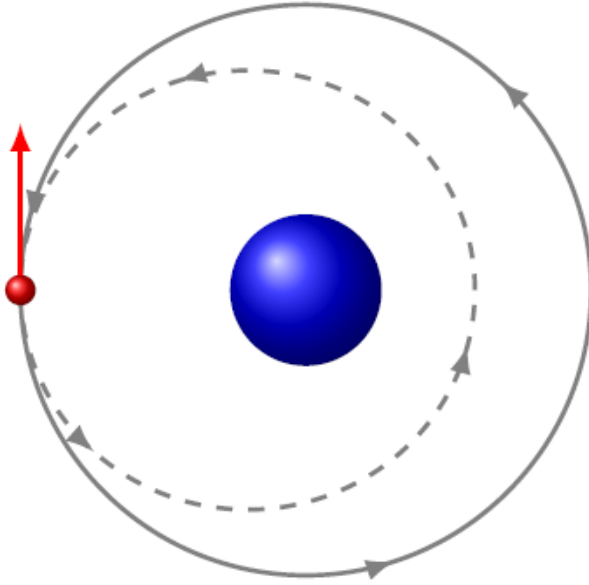
- Doesn't change semi-major axis a
- Doesn't change orbital period

- Doesn't change orbital energy
- Increases eccentricity e , ($b < a$)

Maneuvers

Retrograde and Prograde Burns

Retrograde

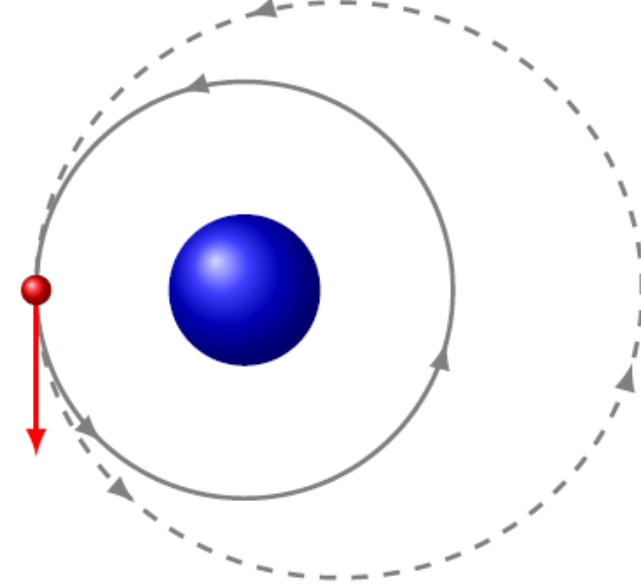


Acceleration in the **opposite** direction of the tangential velocity vector.

Properties:

- raising/lowering perigee and apogee

Prograde



Acceleration in the **same** direction of the tangential velocity vector.

- changes eccentricity

Maneuvers

Hohmann Transfer

Maneuver to transition between circular orbits

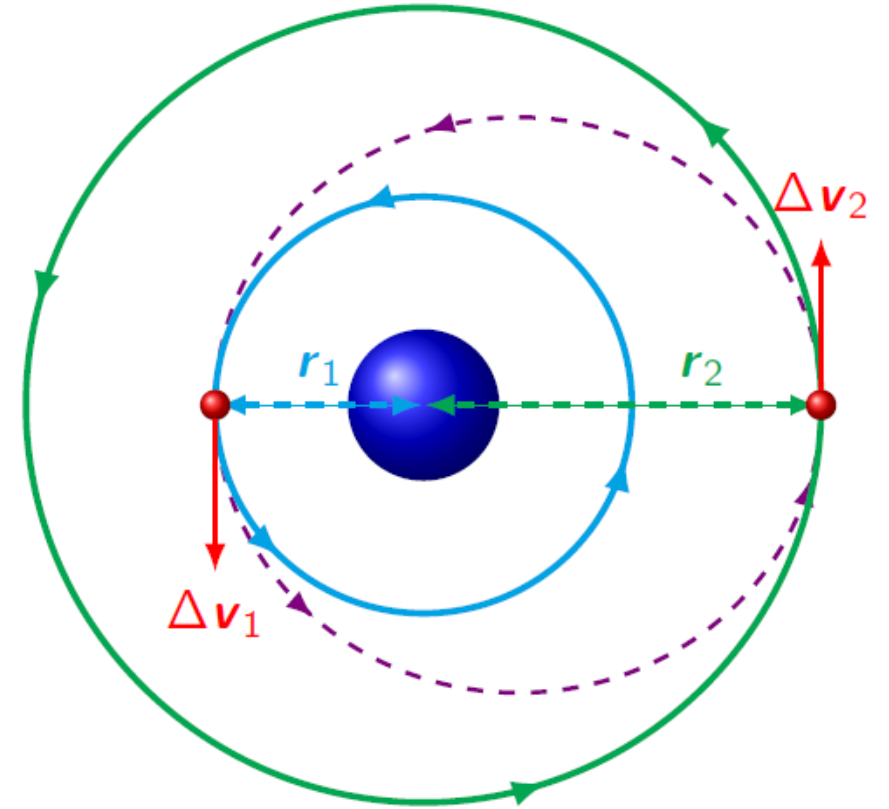
- Consists of two **prograde** or **retrograde** burns
- first burn **shifts apogee** from distance r_1 to r_2
- On resulting elliptical orbit perform second burn **at apogee** to transition to circular orbit with radius r_2

Assuming instantaneous impulses, we have

$$\Delta v_1 = \sqrt{\frac{Gm_{\odot}}{r_1}} \left(\sqrt{\frac{2r_2}{r_1 + r_2}} - 1 \right)$$

and

$$\Delta v_2 = \sqrt{\frac{Gm_{\odot}}{r_2}} \left(1 - \sqrt{\frac{2r_1}{r_1 + r_2}} \right)$$



Maneuvers

Hohmann Transfer on STK

- Use **Astrogator** in **STK** to create:
 - A new satellite with **Astrogator** as propagator
 - Set initial state in **Earth Inertial Cartesian Coordinates** ($r_1=6678$ km, 0, 0)
 - Propagate until apogee (apoapsis) and perform Hohmann to $r_2 = 42164$ km
- $\Delta v_1 = ?$
- $\Delta v_2 = ?$
- → show in STK (Stk_Initial_Velocity.vdf)

6,371 + 307 km



Maneuvers

Hohmann Transfer on STK

- Use **Astrogator** in **STK** to create:
 - A new satellite with **Astrogator** as propagator
 - Set initial state in **Earth Inertial Cartesian Coordinates** ($r_1=6678$ km, 0, 0)
 - Propagate until apogee (apoapsis) and perform Hofmann to $r_2 = 42164$ km

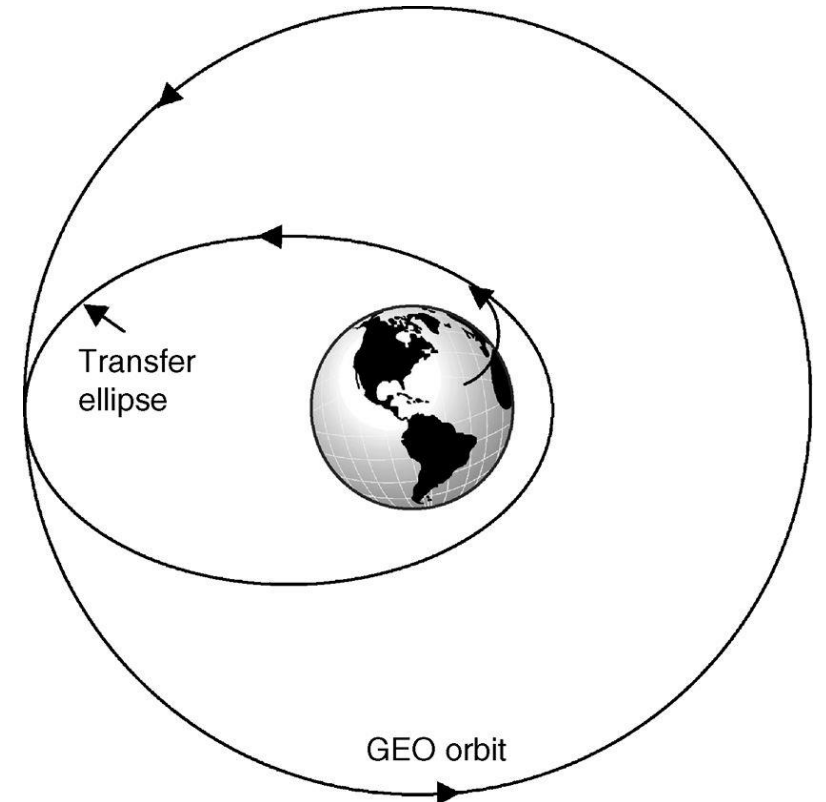
6,371 + 307 km

- $$\Delta v_1 = \sqrt{\frac{\mu}{r_1}} \left(\sqrt{\frac{2r_2}{r_1+r_2}} - 2 \right) = \sqrt{\frac{3.986013 \times 10^5}{6678}} \left(\sqrt{\frac{2 \times 42164}{48842}} - 2 \right) = 2.425 \text{ km/s}$$
- $$\Delta v_2 = \sqrt{\frac{\mu}{r_2}} \left(1 - \sqrt{\frac{2r_1}{r_1+r_2}} \right) = \sqrt{\frac{3.986013 \times 10^5}{42164}} \left(1 - \sqrt{\frac{2 \times 6678}{48842}} \right) = 1.467 \text{ km/s}$$
- → show in STK (Stk_Initial_Velocity.vdf)

Launch Sequence

GEO Satellite Launch Sequence A

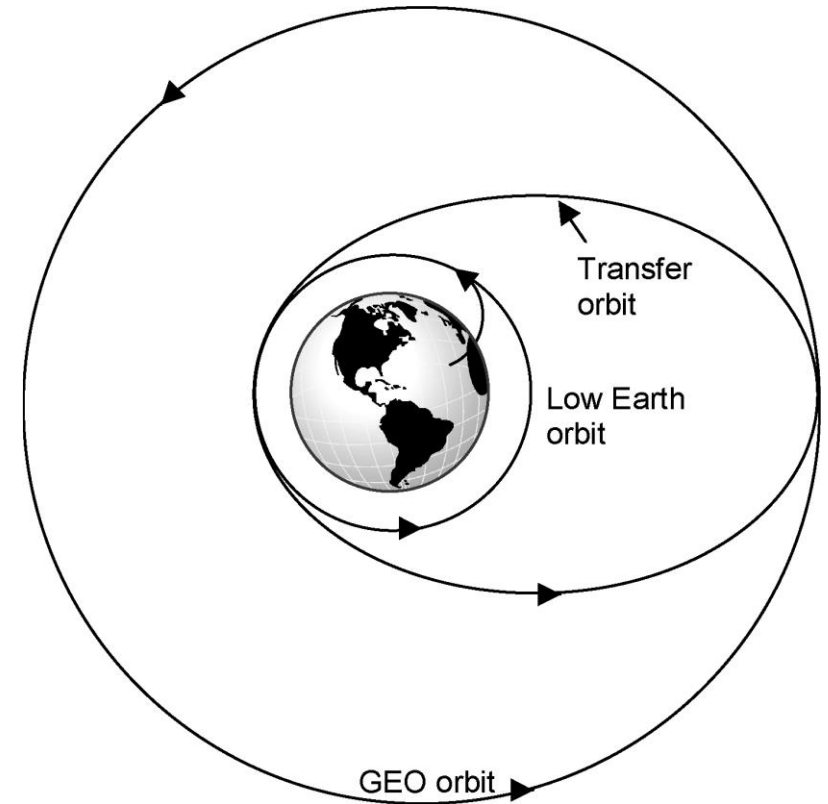
- The satellite heading for a geostationary orbit is first placed in an **elliptical transfer orbit**
- Perigee at an altitude between 200 km and 300 km and its **apogee at the geostationary altitude**
- An apogee maneuver **circularizes the orbit** at the geostationary altitude



Launch Sequence

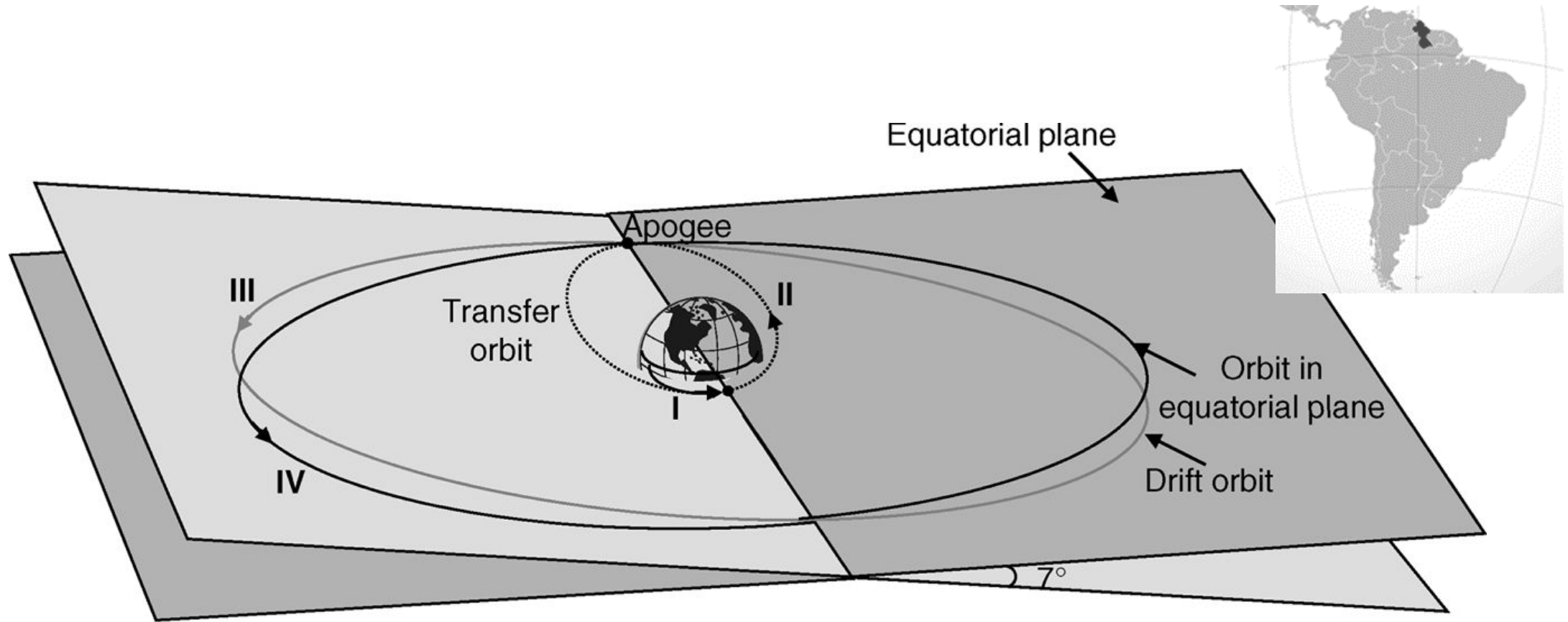
GEO Satellite Launch Sequence B

- The satellite heading for a geostationary orbit is first placed in a **circular low-Earth orbit**
- The low Earth circular orbit is transformed into an **elliptical transfer orbit** with a perigee maneuver
- An apogee maneuver **circularizes the orbit** at the geostationary altitude



Launch Sequence

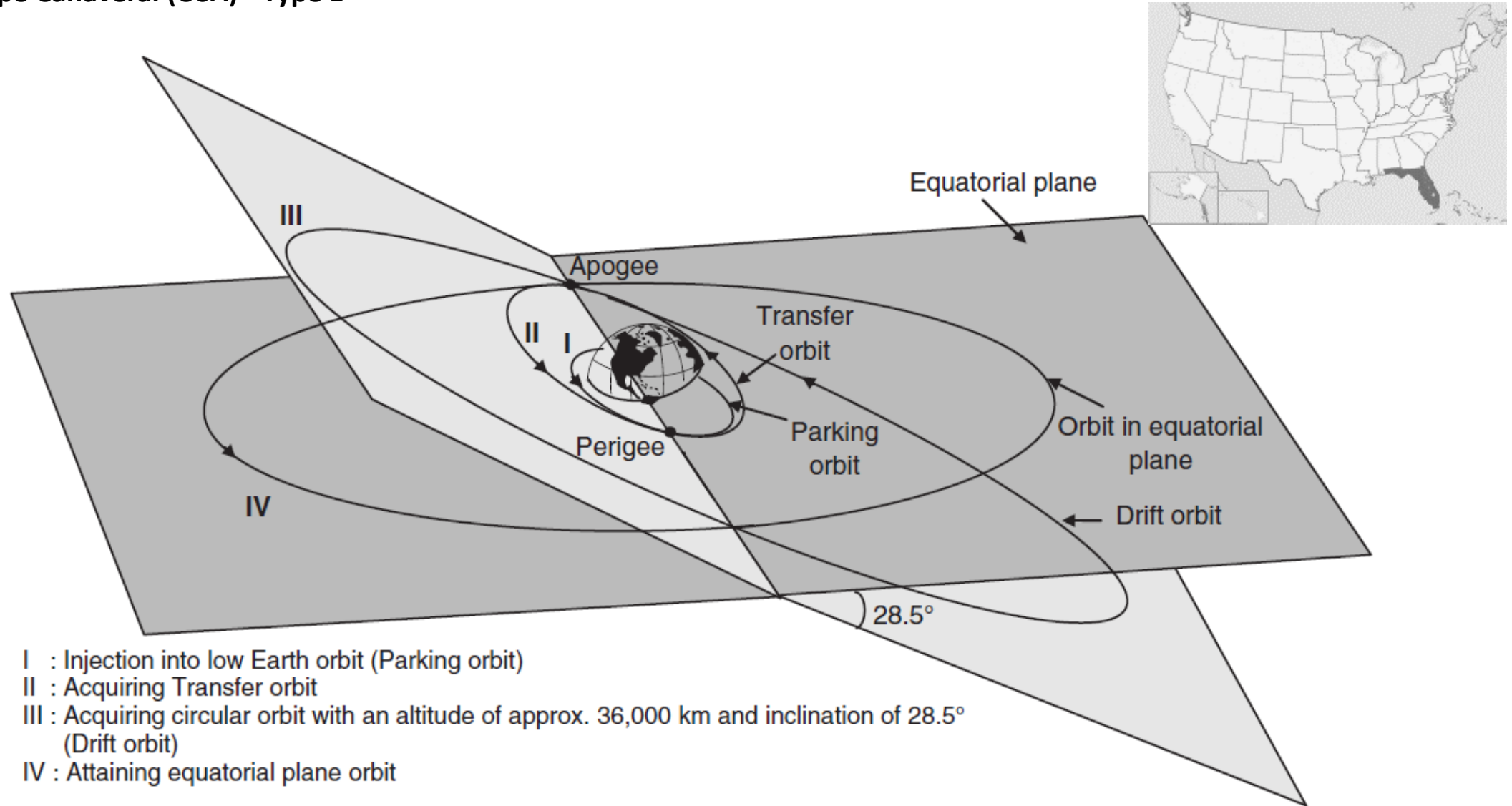
Launch From Kourou (French Guyana) - Type A



- I : Injection into Transfer orbit
- II : Satellite orbits in transfer orbit several times
- III : Acquiring circular orbit with an altitude of approx. 36,000 km and inclination of 7° (Drift orbit)
- IV : Attaining equatorial plane orbit

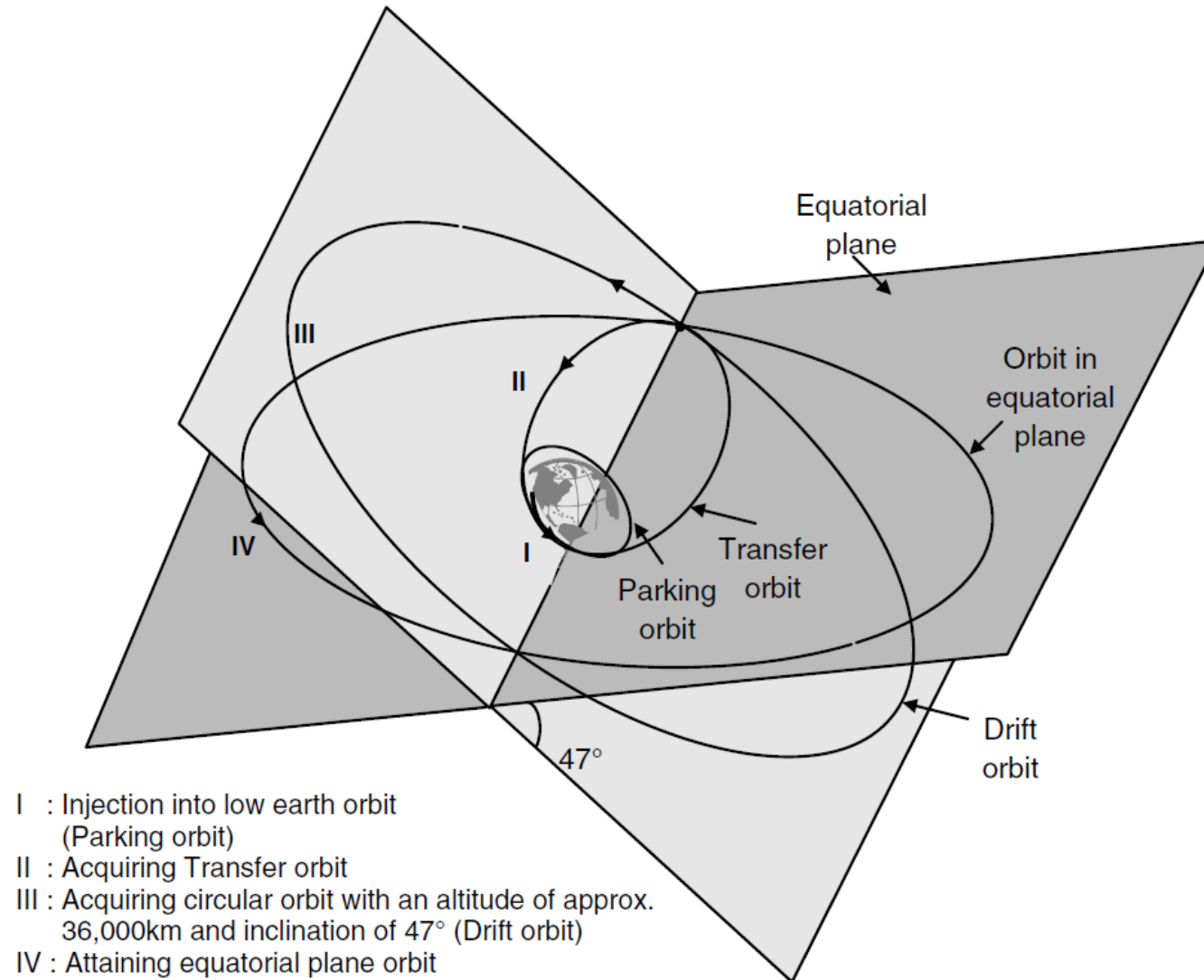
Launch Sequence

Launch From Cape Canaveral (USA) - Type B



Launch Sequence

Launch From Baikonur (Kazakhstan) - Type B



Launch Sequence

Sea Launch



Energia announced it was selling Sea Launch to the S7 Group, a Russian company whose holdings include an airline.



Liftoff of the Long March 11 from a mobile platform in the Yellow Sea, June 5, 2019. Credit: China Academy of Launch Vehicle Technology (CALT).

Launchers

Launchers From Kourou: Ariane-5

- Launch mass: 750–780 tons
- Height: 47–57 m
- Capacity to GTO: 6.9–10 tons
- Capacity to LEO: 16–21 tons
- Stages: 2
- Launches: 117
- Successes: 112



Launchers

Launchers From USA: Delta-IV Heavy

- Launch mass: 249.5–733.4 tons
- Height: 63–72 m
- Capacity to GTO: 3.9–12.98 tons
- Capacity to LEO: 8.6–22.56 tons
- Stages: 2
- Launches: 15
- Successes: 14

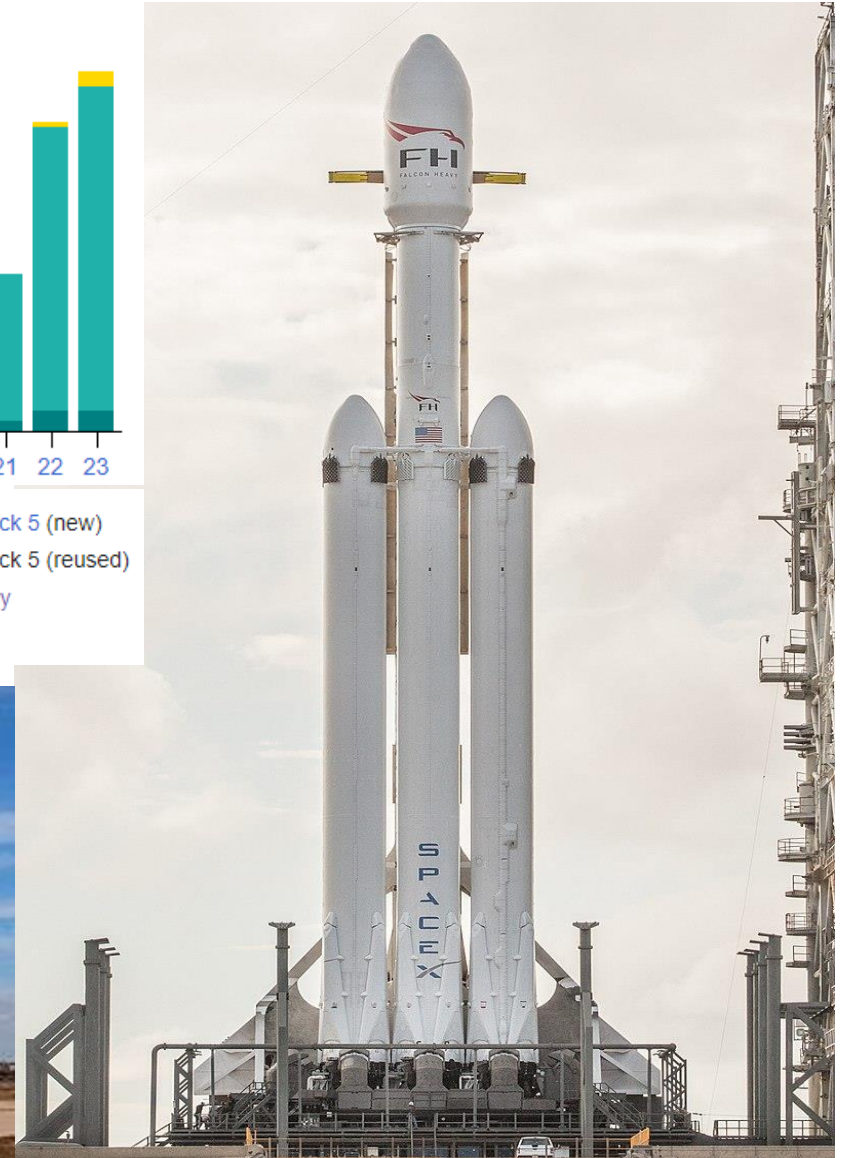
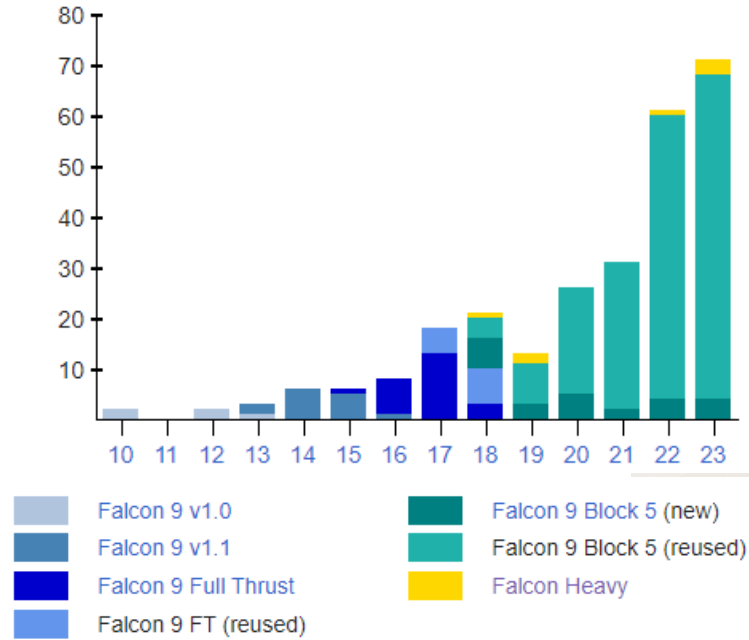


https://en.wikipedia.org/wiki/Delta_IV_Heavy

Launchers

Launchers From USA: Falcon-9 Heavy

- Launch mass: 1.420 T
- Height: 70 m
- Capacity to GTO: 26.7 tons
- Capacity to LEO: 63.8 tons
- Stages: 2+
- Launches: 7
 - Falcon 9: 262
- Successes: 7
 - Falcon 9: 260
- Landings: 221 / 230

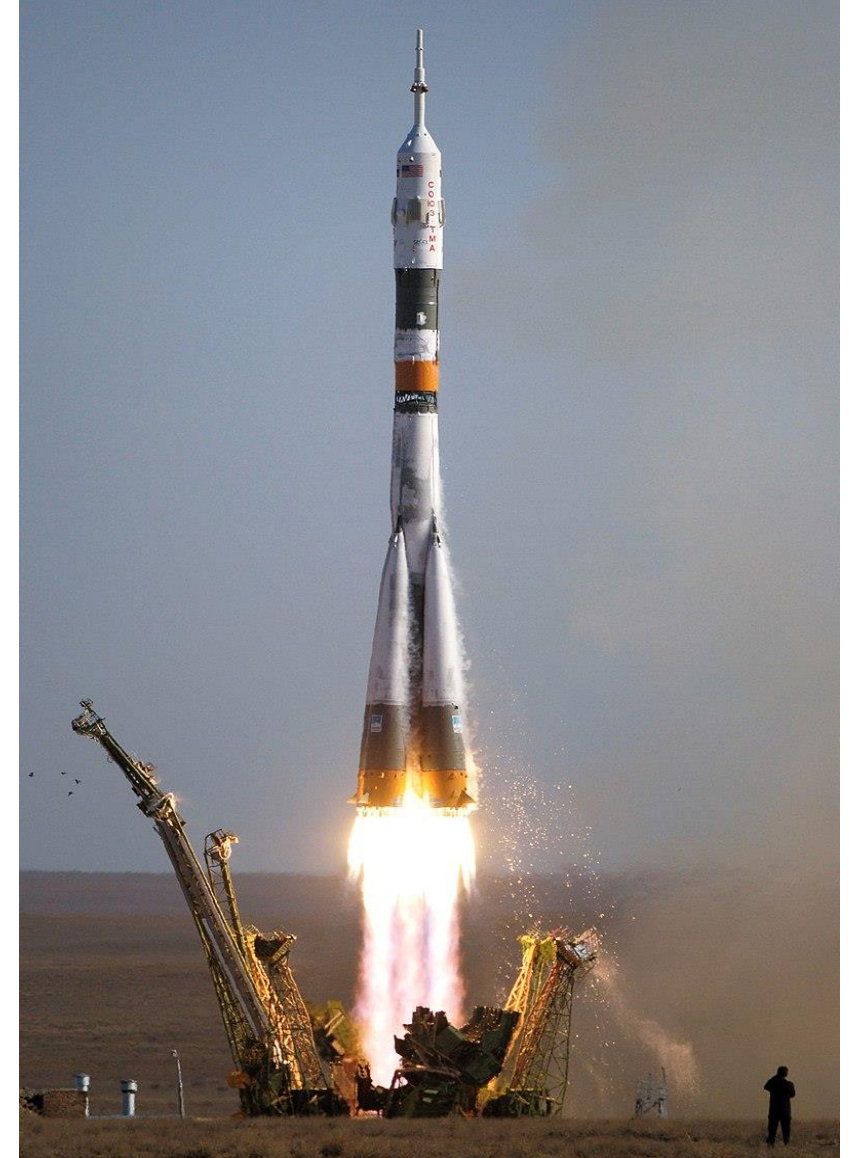


https://en.wikipedia.org/wiki/Falcon_Heavy

Launchers

Launchers From Baikonur: Soyuz

- Launch mass: 313 tons
- Height: 51 m
- Capacity to LEO: 6.9 tons
- Stages: 2
- Launches: 745
- Successes: 724



[https://en.wikipedia.org/wiki/Soyuz_\(rocket_family\)](https://en.wikipedia.org/wiki/Soyuz_(rocket_family))

Launchers

Launchers From China: Long March 5

- Launch mass: 867 tons
- Height: 57 m
- Capacity to GTO: 13 tons
- Capacity to LEO: 25 tons
- Stages: 2
- Launches: 9
- Successes: 8

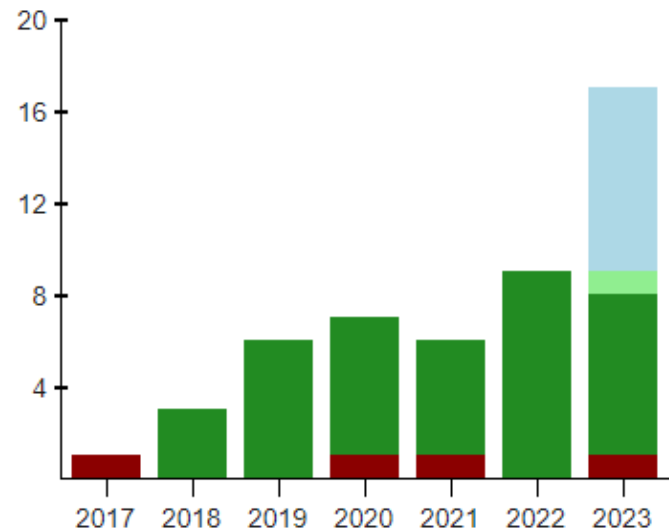


[https://en.wikipedia.org/wiki/Long_March_\(rocket_family\)](https://en.wikipedia.org/wiki/Long_March_(rocket_family)) - https://en.wikipedia.org/wiki/Long_March_5

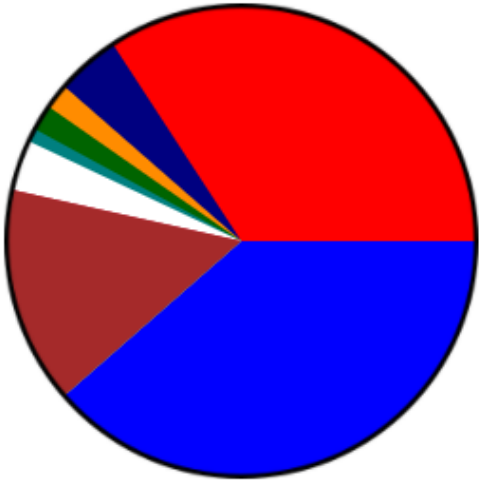
Launchers









Launchers From New Zealand: Electron

- Launch mass: 12 tons
- Height: 17 m
- Capacity to LEO: 150 kg
- Stages: 2
- Launches: 40
- Successes: 36

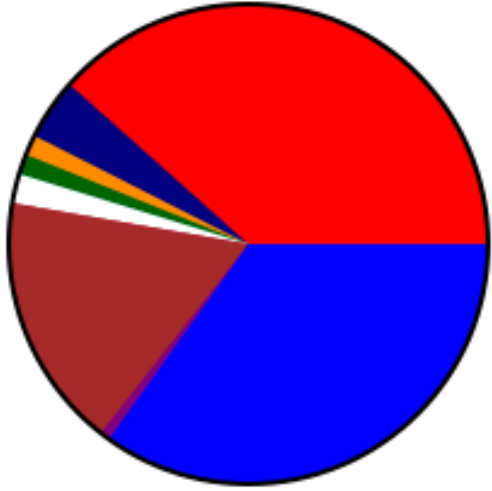


Launch by Country in 2020



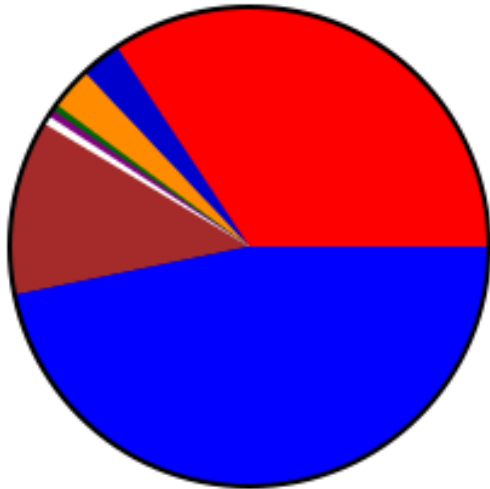
Country	Launches	Successes	Failures	Partial failures	Remarks
 United States	44	40	4	0	Includes seven Electron launches from Mahia
 China	39	35	4	0	
 Russia	17	17	0	0	Includes two Soyuz launches from Kourou
 Europe	5	4	1	0	
 Japan	4	4	0	0	
 India	2	2	0	0	
 Iran	2	1	1	0	
 Israel	1	1	0	0	
World	114	104	10	0	

Launch by Country in 2021



Country ↕	Launches ▼	Successes ↕	Failures ↕	Partial failures ↕	Remarks ↕
 China	56	53	3	0	Includes one unannounced orbital test flight
 United States	51	48	3	0	Includes Electron launches from Mahia
 Russia	25	24	0	1	Includes European Soyuz launches from Kourou, French Guiana by Arianespace
 Europe	6	6	0	0	
 Japan	3	3	0	0	
 India	2	1	1	0	
 Iran	2	0	2	0	
 South Korea	1	0	1	0	[42]
World	146	135	10	1	

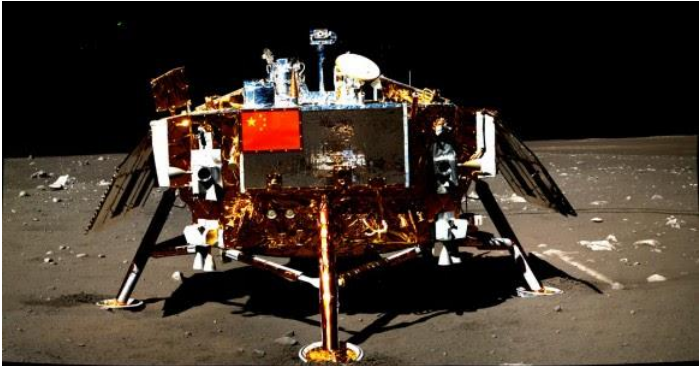
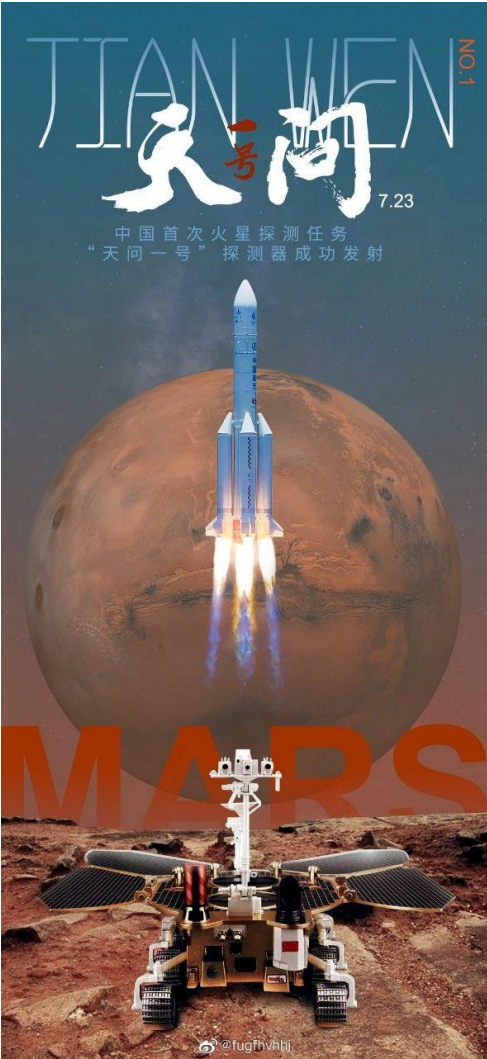
Launch by Country in 2022



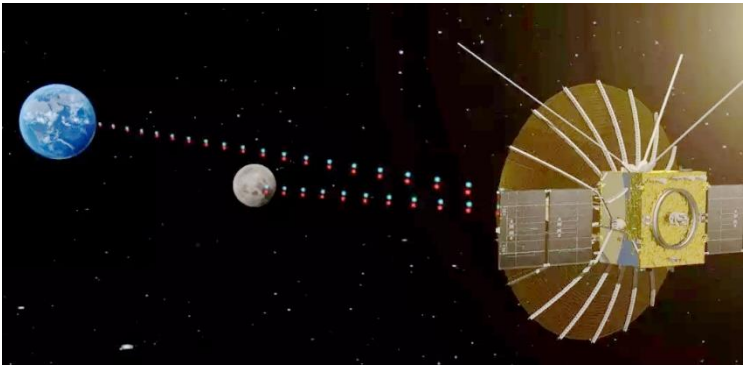
Country	Launches	Successes	Failures	Partial failures	Remarks
 United States	87	84	2	1	Includes Electron launches from Mahia
 China	64	62	2	0	
 Russia	22	22	0	0	Includes Soyuz launches from Kourou and Baikonur
 Europe	5	4	1	0	
 India	5	4	1	0	
 Iran	1	1	0	0	
 Japan	1	0	1	0	
 South Korea	1	1	0	0	
World	186	178	7	1	

China

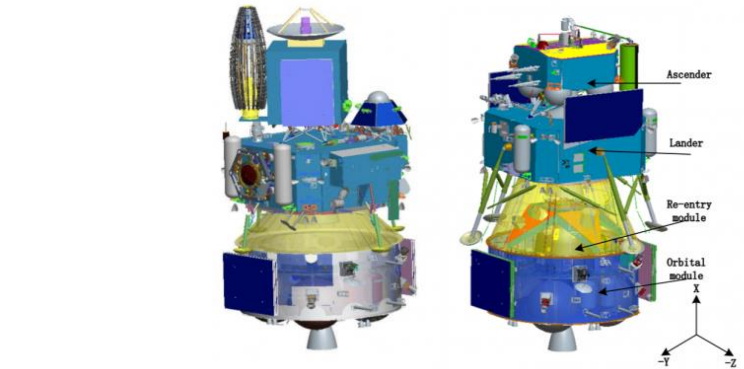
China Interplanetary Space Plan



Chang'e 3 probe in the moon
seen by rover Yutu



Queqiao relay satellite in lagrange
point for chang'e 4 & 5



Return moon sample

Mars 2020 rover

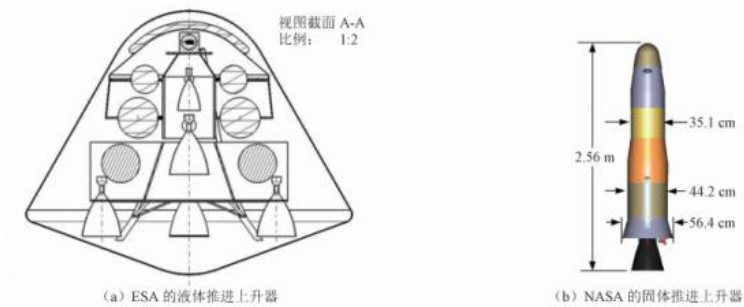


图7 两种不同推进系统的上升器外形

Mars 2030 return samples

Questions?