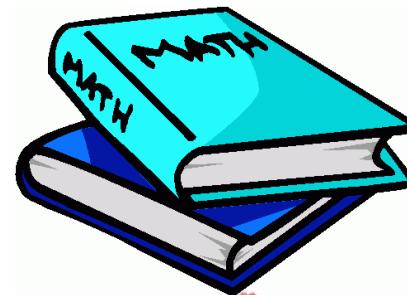


# LIMIT



**Definition:** is used to describe the value that a function or sequence "approaches" as the input or index approaches some value

## EXAMPLE ↴ ↵

Shown as:

$$\lim_{x \rightarrow a} f(x)$$

This means that we are looking at values of  $f(x)$  as  $x$  gets closer and closer to the value of  $a$ .

Sometimes you are able to substitute in  $x = a$  to find the term and sometimes we have to factor and try to cancel some terms before evaluating.

$$\lim_{x \rightarrow 1} \frac{x^2 - 1}{x - 1}$$

Notice that we can't just evaluate this at  $x = 1$ . The function isn't defined at  $x = 1$ . However, by manipulating the equation, we can try to get some cancellation to occur:

$$\begin{aligned} & \lim_{x \rightarrow 1} \frac{x^2 - 1}{x - 1} \\ &= \lim_{x \rightarrow 1} \frac{(x - 1)(x + 1)}{(x - 1)} \\ &= \lim_{x \rightarrow 1} (x + 1) \\ &= 2 \end{aligned}$$



Since we are looking at the values closer and closer to  $x = 1$ , we are allowed to cancel the  $x - 1$  term and are left with  $x + 1$  term. We can then proceed to evaluate this at  $x = 1$ .

