

- Given: a matrix size $m \times n$
- You can shift columns only
- Find largest sub-matrix in which all elements are 1

Thoughts:

If all 1's were on bottom or top of columns, would be trivial:

| | | | |
|---|---|---|----------|
| 0 | 0 | 0 | <u>1</u> |
| 0 | 1 | 1 | 1 |
| 1 | 1 | 1 | 1 |
| 1 | 1 | 1 | 1 |

Assuming sorted and

$top = m[0][n-1]$

$bottom = m[-1][n-1]$

Continue to move $bottom \leftarrow$ and $top \downarrow$ checking if maximum area after each iteration.

Problem: NOT SORTED; Have to find sub-matrix that could be ANYWHERE

- Create a container that tracks current height of matrix.
- If next column value is 1 increment height by 1, otherwise assign to 0.
- Create a copy of height container representing sorted heights
- Iterate over each item in height calculate area by

$$height[i] * (height.size() - i)$$

| | | |
|---|---|---|
| 0 | 0 | 1 |
| 0 | 1 | 1 |
| 1 | 1 | 1 |

1.) $height[i] = 1$; $i = 0$; $1 * (3 - 0) = 3$ /

2.) $height[i] = 2$; $i = 1$; $2 * (3 - 1) = 4$ (circled)

3.) $height[i] = 3$; $i = 2$; $3 * (3 - 2) = 3$

answer

$f(m: \text{List}[\text{List}[\text{int}]) \rightarrow \text{int}$

Time Complexity: $O(mn \log n)$

Space Complexity: $O(n)$

ans: int $\Rightarrow 0$

height: List[int] */ of size m[0].size*

for row $\rightarrow m$

for $j = 0 \rightarrow \text{row.size}()$

height[j] = 0 if row[j] == 0 else height[j] + 1

s-height: List[int] \Rightarrow height

sort(s-height)

for $j = 0 \rightarrow \text{row.size}()$

ans = max(ans, s-height[j] * (row.size() - j))

return ans