

CSCI 552(Spring 2021)

Homework #2

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Handout: Thursday, March 11, 2021

Due: 11:59 pm, Thursday, March 25, 2021

Total points: 35

All assignments will be submitted through Canvas. Documents will need to be in either Word or PDF format. Images need to be in jpeg format.

1. In multi-dimensional data visualization, some techniques are more suited for large volume of data (size) and some are better suited for data set of very high dimensions. List 2 techniques that are good for large size of data and 2 for very high dimensional data (there can be overlaps). Please explain why in each case.

There are many multi-dimensional data visualization technique.

Following are the 2 technique that are good for large size of data.

### 1) Radial visualization

Radial graph visualization is a variation of pie chart. Radial graph shows the ~~see~~ co-relation between parts and the whole, but it may also include sub-categories for each part of the whole. Each category in the data series plotted in a radial bar chart is assigned different color, while sub category are assigned same.

### 2) Node - Link graph

The use of nodes and link denote connection between a group of entities is used in this type of visualization to demonstrate how things are interwined.

The advantage is that it is intuitive and good for global structure. As the complexity is  $> O(N^2)$  it is not suitable for very large data set.

The 2 techniques for very high dimensional data set are below

1) Heat map.

In Heat map colored rectangles, each represent attribute. Heat map allows user to quickly grasp the state and impact of a large number of variables at once.

2) Table lens visualization

It is used to explore large amount of tabular data. It displays regional data in columns and rows without obscuring any data. It has ability to sort data, ~~or~~ focus or remove unwanted data.

2. In radial layout visualization of multi-dimensional data, variables (dimensions) are placed in a circle, and data points can be drawn as dots within the circle that best reflect the data points' attribute values (coordinates). This can be done through minimizing an object function to determine the location of each dot. Derive an object function formula for an  $n$ -dimensional data set for this type of radial visualization.

In Radial graph visualization object function to determine the location of each dot is follows

In a circle total angle is  $360^\circ$

$N$  is the number of attributes

$\therefore$  Angle of attribute =  $(2\pi)/N$

Start point =  $[1 \cdot \cos \theta, 1 \cdot \sin \theta]$

End point =  $[2 \cdot \cos \theta, 2 \cdot \sin \theta]$

As Radial is  $M$ -dimensional, Input is in  $n$  dimensional space. Out-put is in  $k$  dimensional space ( $k \leq n$ ).

Object function to determine location

$$J(\mathbf{y}) = \frac{\sum_{i,j} (d_{ij} - \hat{d}_{i,j})^2}{\sum_{i,j} \hat{d}_{i,j}^2}$$

$\hat{d}_{i,j}$  is the distance between 2 point in  $n$ -D space.

$d_{ij}$  is distance between point in  $k$ -D space.

$\mathbf{y}$  is data point in  $k$ -D space location of dot



3. One benefit of radial layout of node-link visualization is that it has more space for deeper level nodes.

(a) Show that this benefit is still not sufficient to overcome the exponential growth of nodes in hierarchical data sets.

→ 3.1 Radial graph is not sufficient to overcome the exponential growth of nodes in hierarchical data set because hierarchical data is not stable data set. It can grow in any where and in any direction. To plot such data on radial graph can lead to ~~not~~ no states to the data. It will be very hard to spot anomalies. Radial graph is not scalable, to plot hierarchical data as it is not scalable. It is because of continuous nature. As the Radial graph is not optimal the is waste of space, as the space gets wasted it is not good for exponential growth of hierarchical data set.

(b) Explain why hyperbolic tree visualization can more effectively overcome this problem.

→ 3.2

Hyperbolic tree visualization  
hyperbolic tree is plot in hyperbolic  
space which has more space  
the euclidean space. In hyperbolic  
space the circumference of the  
same circle will rise exponentially.  
This makes tree unclutter.  
In this tree putting parent and  
children far also, will take same  
space if parent and children very close.  
As it does not take extra space  
it is good for exponential data.  
This ability to uniformly embed  
an exponential growing structure  
are the aspects of layout.