

TYPE #3      Sum into Product

$$\sin C + \sin D = 2 \sin\left(\frac{C+D}{2}\right) \cos\left(\frac{C-D}{2}\right)$$

$$\sin C - \sin D = 2 \cos\left(\frac{C+D}{2}\right) \sin\left(\frac{C-D}{2}\right)$$

$$\cos C + \cos D = 2 \cos\left(\frac{C+D}{2}\right) \cos\left(\frac{C-D}{2}\right)$$

$$\cos C - \cos D = 2 \sin\left(\frac{C+D}{2}\right) \sin\left(\frac{D-C}{2}\right)$$

TYPE #4      Product into Sum

$$2 \sin A \cos B = \sin(A+B) + \sin(A-B)$$

$$2 \cos A \sin B = \sin(A+B) - \sin(A-B)$$

$$2 \cos A \cos B = \cos(A+B) + \cos(A-B)$$

$$2 \sin A \sin B = \cos(A-B) - \cos(A+B)$$

$$Q \quad \cos 3x + \underline{\sin 2x} - \underline{\sin 4x} = 0$$

$$\cos 3x = \underline{\sin 4x} - \underline{\sin 2x}$$

$$\cancel{\cos 3x} = 2 \cancel{\cos 3x} \sin x$$

$$\cos 3x = 0$$

$$3x = (2n-1) \frac{\pi}{2}$$

$$x = (2n-1) \frac{\pi}{6}$$

$$2 \sin x = 1$$

$$\sin x = \frac{1}{2}$$

$$x = n\pi + (-1)^n \frac{\pi}{6}$$

$$\underline{n \in \mathbb{I}}$$

$$Q \quad \sin 5x \cos 3x = \sin 6x \cos 2x$$

$$2 \sin 5x \cos 3x = 2 \sin 6x \cos 2x$$

$$\sin 8x + \sin 2x = \sin 8x + \sin 4x$$

$$\begin{aligned} \sin 2x &= \sin 4x \\ &= 2 \sin 2x \cos 2x \end{aligned}$$

$$\begin{aligned} \sin 2x &= 0 & 2x &= n\pi \\ & & x &= \frac{n\pi}{2} \end{aligned}$$

$$2 \cos 2x = 1$$

$$\cos 2x = \frac{1}{2}$$

$$2x = 2n\pi \pm \frac{\pi}{3}$$

$$x = n\pi \pm \frac{\pi}{6}$$

$$n \in \mathbb{I}$$

$$Q \quad \underline{5 \sin x} + 6 \sin 2x + \underline{5 \sin 3x} + \sin 4x = 0$$

$$5 (\sin x + \sin 3x) + 6 \sin 2x + \sin 4x = 0$$

$$5 (2 \underline{\sin 2x \cos x}) + 6 \underline{\sin 2x} + \underline{\sin 4x} = 0$$

$$2 \sin 2x \cos 2x$$

$$\underline{2 \sin 2x} ( \overset{\checkmark}{5 \cos x + 3 + \cos 2x} ) = 0$$

$$\sin 2x = 0$$

$$2x = n\pi$$

$$x = \underline{\underline{\frac{n\pi}{2} \quad n \in \mathbb{I}}}$$



$$\underline{5 \cos x} + 3 + \underline{\cos 2x} = 0$$

$$\cos 2x = 2 \cos^2 x - 1$$

$$5 \cos x + 3 + 2 \cos^2 x - 1 = 0$$

$$2 \cos^2 x + 5 \cos x + 2 = 0$$

$$(2 \cos x + 1)(\cos x + 2) = 0$$

$$\cos x = -\frac{1}{2} \quad \cos x = -2$$

                      
x

$$\cos x = -\frac{1}{2}$$

$$\frac{2\pi}{3} \quad (\pi - \frac{\pi}{3})$$

$$x = \frac{2n\pi \pm \frac{2\pi}{3}}{n \in \mathbb{I}}$$

Q  
Good

$$\cos \theta - \sin 3\theta = \cos 2\theta$$

$$\cos \theta - \cos 2\theta = \sin 3\theta$$

$$\cancel{2} \cancel{\sin \frac{3\theta}{2}} \sin \frac{\theta}{2} = \sin 3\theta$$

$$= \cancel{2} \cancel{\sin \frac{3\theta}{2}} \cos \frac{3\theta}{2}$$

$$\sin \frac{3\theta}{2} = 0$$

$$\frac{3\theta}{2} = n\pi$$

$$\theta = \frac{2n\pi}{3}$$

$$\sin \frac{\theta}{2} = \cos \frac{3\theta}{2} \quad \text{imp}$$

Given

$$\cos \frac{3\theta}{2} = \cos \left( \frac{\pi}{2} - \frac{\theta}{2} \right)$$

$$\frac{3\theta}{2} = 2n\pi \pm \left( \frac{\pi}{2} - \frac{\theta}{2} \right)$$

$$(1) \quad \frac{3\theta}{2} = 2n\pi + \frac{\pi}{2} - \frac{\theta}{2}$$

$$2\theta = 2n\pi + \frac{\pi}{2}$$

$$\theta = n\pi + \frac{\pi}{4} \quad n \in \mathbb{I}$$

$$\sin A = \cos \left( \frac{\pi}{2} - A \right)$$

$$\frac{3\theta}{2} = 2n\pi - \frac{\pi}{2} + \frac{\theta}{2}$$

$$\theta = 2n\pi - \frac{\pi}{2}$$

$$n \in \mathbb{I}$$



$$\begin{aligned} \text{Q } \sin x + \sin 5x &= \sin 2x + \sin 4x \\ \cancel{2 \sin 3x} \cos 2x &= \cancel{2 \sin 3x} \cos x \end{aligned} \quad (2)$$

$$\begin{aligned} (1) \quad \sin 3x &= 0 & \cos 2x &= \cos x \\ 3x &= n\pi \checkmark & 2x &= 2n\pi \pm x \\ x &= \frac{n\pi}{3} & (2) \quad 2x &= 2n\pi + x \\ & & x &= 2n\pi \checkmark \\ \hline \hline n &\in \mathbb{I} \end{aligned}$$

$$\begin{aligned} 2x &= 2n\pi - x \\ 3x &= 2n\pi \\ x &= \frac{2n\pi}{3} \checkmark \end{aligned}$$

$\left( \frac{n\pi}{3} \right), \quad \frac{2n\pi}{3}, \quad \frac{2n\pi}{3}$   
 $[0, 2\pi]$

$\checkmark$ $0, \frac{\pi}{3}, \frac{2\pi}{3},$ $\pi, \frac{4\pi}{3}, \frac{5\pi}{3}$ $2\pi$ $\checkmark$	$0, 2\pi$	$0, \frac{2\pi}{3}, \frac{4\pi}{3}, 2\pi$ <hr/> SINGLE CORRECT $\checkmark$ (A) $\frac{n\pi}{3}$ (B) $2n\pi$ (C) $\frac{2n\pi}{3}$ (D) None
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$x = \frac{n\pi}{3} \quad n \in \mathbb{Z}$