

■ Lagrange Interpolation :

■ Question 1:

```
In[90]:= y = {1, 2, 3, 10, 11};
```

```
f = {2, 5, 10, 20, 3};
```

```
n = Length[y];
```

```
n = Length[f];
```

```
i = 1;
```

```
While[i ≤ n ,
```

$$L[i, x_] = \left(\prod_{j=1}^{i-1} \frac{x - y[[j]]}{y[[i]] - y[[j]]} \right) \left(\prod_{j=i+1}^n \frac{x - y[[j]]}{y[[i]] - y[[j]]} \right); i++];$$

$$\text{Lagrange}[x_] = \sum_{k=1}^n L[k, x] * f[[k]];$$

```
g = Simplify[N[Lagrange[x]]]
```

```
Print["Simplified Langrange Interpolating Polynomial=" g]
```

```
Out[97]= 1.69048 - 1.23849 x + 1.64028 x2 - 0.0876984 x3 - 0.00456349 x4
```

```
Simplified Langrange Interpolating Polynomial=
```

$$(1.69048 - 1.23849 x + 1.64028 x^2 - 0.0876984 x^3 - 0.00456349 x^4)$$

■ Question 2:

```
In[99]:= y = {3, 4, 5, 7};
```

```
f = {4, 7, 12, 22};
```

```
n = Length[y];
```

```
n = Length[f];
```

```
i = 1;
```

```
While[i ≤ n ,
```

$$L[i, x_] = \left(\prod_{j=1}^{i-1} \frac{x - y[[j]]}{y[[i]] - y[[j]]} \right) \left(\prod_{j=i+1}^n \frac{x - y[[j]]}{y[[i]] - y[[j]]} \right); i++];$$

$$\text{Lagrange}[x_] = \sum_{k=1}^n L[k, x] * f[[k]];$$

```
g = Simplify[N[Lagrange[x]]]
```

```
Print["Simplified Langrange Interpolating Polynomial=" g]
```

```
Out[106]= 22. - 15.75 x + 4. x2 - 0.25 x3
```

$$\text{Simplified Langrange Interpolating Polynomial} = (22. - 15.75 x + 4. x^2 - 0.25 x^3)$$

■ Question 3:

```

In[108]:= y = {4, 5, 6};
          f = {5, 8, 13};
          n = Length[y];
          n = Length[f];
          i = 1;
          While[i ≤ n,
            L[i, x_] =  $\left( \prod_{j=1}^{i-1} \frac{x - y[[j]]}{y[[i]] - y[[j]]} \right) \left( \prod_{j=i+1}^n \frac{x - y[[j]]}{y[[i]] - y[[j]]} \right); i++];$ 
            Lagrange[x_] =  $\sum_{k=1}^n L[k, x] * f[[k]];$ 
            g = Simplify[N[Lagrange[x]]]
            Print["Simplified Langrange Interpolating Polynomial=" g]

Out[115]= 13. - 6. x + 1. x2

Simplified Langrange Interpolating Polynomial=(13. - 6. x + 1. x2)

```