

■ Gauss-Seidel Method

■ $4x_1 + x_2 + 2x_3 = 4$

■ $-3x_1 + 5x_2 + x_3 = 7$

■ $x_1 + x_2 + 3x_3 = 3$

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In[1]:= A = {{4.0, 1.0, 2.0}, {-3.0, 5.0, 1.0}, {1.0, 1.0, 3.0}};
d = {{4.0, 0, 0}, {0, 5.0, 0}, {0, 0, 3.0}};
u = {{0, 1.0, 2.0}, {0, 0, 1.0}, {0, 0, 0}};
l = {{0, 0, 0}, {-3.0, 0, 0}, {1.0, 1.0, 0}};
b = Transpose[{{4.0, 7.0, 3.0}}];
x[1] = Transpose[{{0, 0, 0}}]; Do[x[n+1] = LinearSolve[(l+d), -u.x[n]+b];
Print[x^n, "=", MatrixForm[x[n]], {n, 1, 15}]
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$$x = \begin{pmatrix} 0 \\ 0 \\ 0 \end{pmatrix}$$

$$x^2 = \begin{pmatrix} 1. \\ 2. \\ -3.70074 \times 10^{-17} \end{pmatrix}$$

$$x^3 = \begin{pmatrix} 0.5 \\ 1.7 \\ 0.266667 \end{pmatrix}$$

$$x^4 = \begin{pmatrix} 0.441667 \\ 1.61167 \\ 0.315556 \end{pmatrix}$$

$$x^5 = \begin{pmatrix} 0.439306 \\ 1.60047 \\ 0.320074 \end{pmatrix}$$

$$x^6 = \begin{pmatrix} 0.439845 \\ 1.59989 \\ 0.320088 \end{pmatrix}$$

$$x^7 = \begin{pmatrix} 0.439983 \\ 1.59997 \\ 0.320015 \end{pmatrix}$$

$$x^8 = \begin{pmatrix} 0.439999 \\ 1.6 \\ 0.320001 \end{pmatrix}$$

$$x^9 = \begin{pmatrix} 0.44 \\ 1.6 \\ 0.32 \end{pmatrix}$$

$$x^{10} = \begin{pmatrix} 0.44 \\ 1.6 \\ 0.32 \end{pmatrix}$$

$$x^{11} = \begin{pmatrix} 0.44 \\ 1.6 \\ 0.32 \end{pmatrix}$$

$$x^{12} = \begin{pmatrix} 0.44 \\ 1.6 \\ 0.32 \end{pmatrix}$$

$$x^{13} = \begin{pmatrix} 0.44 \\ 1.6 \\ 0.32 \end{pmatrix}$$

$$x^{14} = \begin{pmatrix} 0.44 \\ 1.6 \\ 0.32 \end{pmatrix}$$

$$x^{15} = \begin{pmatrix} 0.44 \\ 1.6 \\ 0.32 \end{pmatrix}$$