

# **Experiment-4**

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To find the closure, candidate keys, prime attributes and highest normal form using the given relation and functional dependencies.

## **Question 1**

R(ABCD),  $FDs = \{AB -> C, C -> D, D -> A\}$ 

#### Solution

Closure:

 $AB+ = \{A, B, C, D\}$ 

 $BC+ = \{B, C, A, D\}$ 

 $BD+ = \{B, D, A, C\}$ 

Candidate Key: AB, BD, BC Prime Attributes: {A, B, C, D} Non-Prime Attributes: {}

Normal Form: It cannot be BCNF as C is a SK(C -> D). All determinants have prime attributes,

so the relation is in 3NF.

#### **Ouestion 2**

R(ABCDE),  $FDs = \{A -> D, B -> A, BC -> D, AC -> BE\}$ 

### Solution

Closure:

 $A + = \{A, D\}$ 

 $B+=\{B,A,D\}$ 

 $C+=\{C\}$ 

 $BC+ = \{B, C, A, D, E\}$ 

 $AC+ = \{A, B, C, D, E\}$ 

Candidate Key: AC, BC Prime Attributes: {A, B, C}



Non-Prime Attributes: {D, E}

Normal Form: Partial dependency exists (A -> D). Hence relation is in 1NF.

## **Question 3**

$$R(ABCDE), FDs = \{B -> A, A -> C, BC -> D, AC -> BE\}$$

### Solution

Closure:

$$B+ = \{A, B, C, D, E\}$$
  
 $A+ = \{A, C, B, D, E\}$ 

Candidate Key: A, B
Prime Attributes: {A, B}

Non-Prime Attributes: {C, D, E}

Normal Form: All determinants are either CK or SK. So this relation is in BCNF.

### **Question 4**

$$R(ABCDEF), FDs = \{A -> BCD, BC -> DE, B -> D, D -> A\}$$

### Solution

Closure:

 $A+= \{A, B, C, D, E\}$   $AF+= \{A, F, B, C, D, E\}$  $DF+= \{D, F, B, C, A, E\}$ 

 $BF+ = \{B, F, C, A, D, E\}$ 

Candidate Key: AF, DF, BF Prime Attributes: {A, D, B, F} Non-Prime Attributes: {C, E}

Normal Form: Partial dependency exists (A -> BCD). Hence relation is in 1NF.

# **Ouestion 5**

$$FDs = \{X -> Y, WZ -> X, WZ -> Y, Y -> W, Y -> X, Y -> Z\}$$

# Solution

Closure:

 $Y + = \{Y, X, W, Z\}$ 

 $X+ = \{X, Y, W, Z\}$ 

 $WZ+=\{W,\,Z,\,X,\,Y\}$ 

Candidate Key: Y, X, WZ
Prime Attribute: {X, Y, W, Z}
Non-Prime Attributes: { }

Normal Form: All determinants are CK. Highest NF = BCNF.

## **Question 6**

R(ABCDEF),  $FDs = {A -> BC, A -> D, D -> E, BC -> D}$ 

### Solution

Closure:

 $A+ = \{A, B, C, D, E\}$  $AF+ = \{A, B, C, D, E, F\}$ 

Candidate Key: AF
Prime Attributes: {A, F}

Non-Prime Attributes: {B, C, D, E}

Normal Form: A -> BC introduces partial dependency (A is part of key AF and BC is non-prime).

Hence highest NF = 1NF.