

LUMBINI ENGINEERING MANAGEMENT AND SCIENCE COLLEGE
(Pokhara University)
ASSIGNMENT - I

Subject: Theory of Computation (TOC)

Date: 2081/02/23

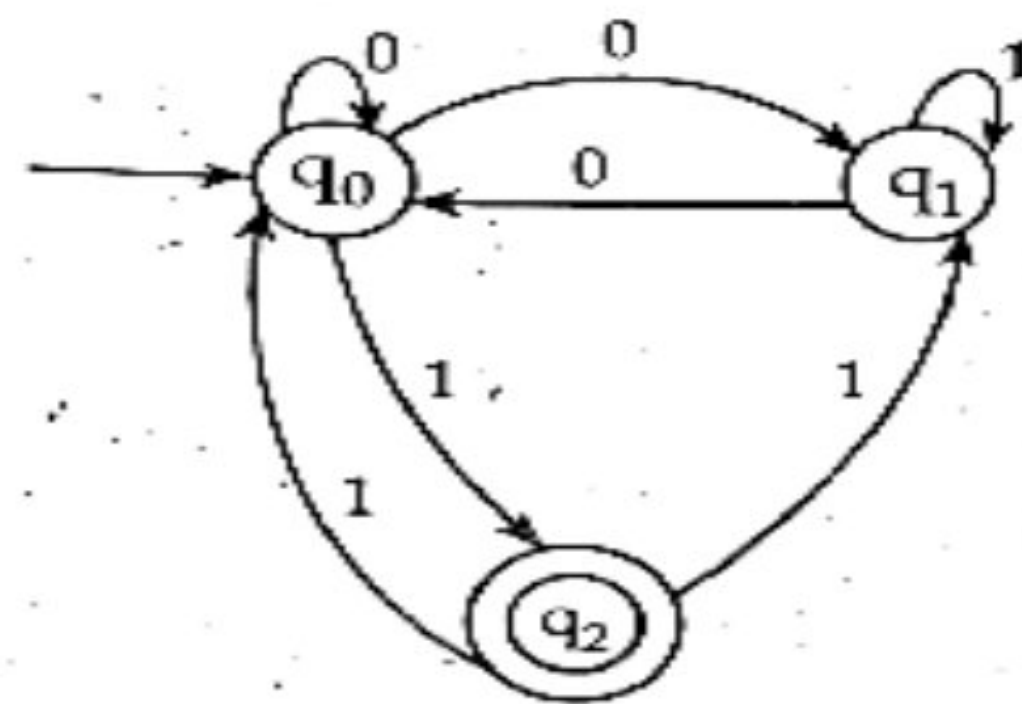
Instructions:

Answer all questions.

Provide detailed explanations and examples where necessary.

Submit the assignment by the specified deadline.

1. Define alphabet, string and language with examples. Discuss the operational characteristics of a Finite Automata.
2. What are the components of finite automata? Design a DFA that accepts the strings given by: $M = \{w \in \{a, b\}^* : w \text{ has a number of 'a' divisible by 3 and number of 'b' divisible by 2}\}$.
3. What is the significant of finite automata? Design a DFA that accepts the strings over an alphabet $\Sigma = \{0,1\}$ that either start with 01 or end with 02. Test your design for any two strings.
4. Define DFA formally. Construct a DFA over $\{a, b\}$ accepting strings having even number of 'a' and odd number of 'b'.
5. Differentiate between DFA and N DFA. Convert the following N DFA to its DFA



6. Construct a FA equivalent to the following Transition Table and construct an equivalent DFA.

$Q \setminus \Sigma$	0	1
$\rightarrow q_0$	$\{q_0, q_1\}$	q_0
q_1	q_2	q_1
q_2	q_3	$\{q_3, q_2\}$
$*q_3$	\emptyset	q_3

7. $M = (\{q_1, q_2, q_3\}, \{0,1\}, q_1, \{q_3\})$ is a nondeterministic finite automation, where is given by.
 $(q_1, 0) = \{q_2, q_3\}$
 $(q_1, 1) = \{q_1\}$
 $(q_2, 0) = \{q_1, q_2\}$
 $(q_2, 1) = \emptyset$
 $(q_3, 0) = \{q_2\}$
 $(q_3, 1) = \{q_1, q_2\}$
Construct an equivalent DFA.
8. Construct a FA equivalent to the following R.E.
 - a. $a^* + (ab + a)^*$
 - b. $(aa + b)^* (bb + a)^*$

c. $a(a+b)^*bb$

9. Explain about decision algorithms for regular language.
10. Show that $L = \{ww \mid w \rightarrow \{a, b\}^*\}$ is not regular.
11. Show that $L = \{a^n b a^n, n \geq 0\}$ is not a regular language by using pumping lemma.
12. Show that the class of languages of FA is closed under union, intersection and Kleene closure.
13. Define Parse Tree. When a grammar is called ambiguous? Explain with example.
14. Design CFG for language $L(G) = \{a^m b^n \mid m \geq n\}$ along with parse tree.
15. For the grammar given below:
 $E \rightarrow E + T \mid T, \quad T \rightarrow T \times F \mid F, \quad F \rightarrow (E) \mid a \mid b$
Give the derivation (both in sentential and parse tree) of: **$(a+b) \times a + b$**
16. Define context free grammar. Convert the given context free grammar (CFG) into equivalent CNF.
 $S \rightarrow AB$
 $A \rightarrow aAA \mid \epsilon$
 $B \rightarrow bBB \mid \epsilon$
17. Prove that a following grammar is ambiguous.
 $S \rightarrow aB \mid ab$
 $A \rightarrow aAB \mid a$
 $B \rightarrow ABb \mid b$
18. Write Short Notes on:
 - a. Regular Expression
 - b. Relation and Function