PYL800 - Group 1 Presentation

Hriday Sabharwal - 2020PH10697 Khushvind Maurya - 2021MT10238 Asmit Singh - 2021MT10887 Mohit Raj Modi - 2021MT10919

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Outline

- 1 Problem 1
- 2 Problem 2
- 3 Problem 3
- 4 Problem 4

a. Plot y = A.sin(wt)

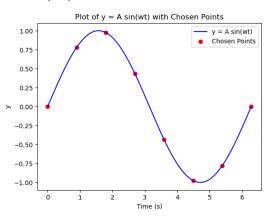


Fig. 1.1

b. Use linear and quadratic splines and c. Plot the spline fitted curve

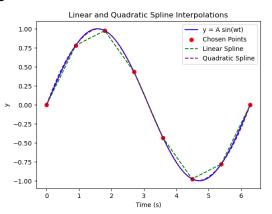


Fig. 1.2

d. Evaluate R^2 with increased data points

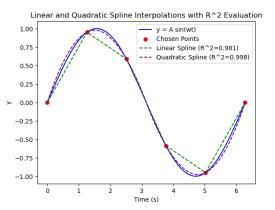


Fig. 1.3

Problem 1 - Code

```
import numpy as np
import matplotlib.pyplot as plt
from scipy.interpolate import interp1d
from sklearn.metrics import r2_score
A = 1 # Amplitude
w = 1 # Angular frequency
# Time Period
T = 2 * np.pi / w
# Choose 20 points within one period
t_points = np.linspace(0, T, 6)
inc_t_points = np.linspace(0, T, 20)
y_points = A * np.sin(w * t_points)
t = np.linspace(0, T, 1000)
y = A * np.sin(w * t)
```

Problem 1 - Code

```
# Linear spline interpolation
linear_interp = interp1d(t_points, y_points, kind='linear')
# Quadratic spline interpolation
quadratic_interp = interp1d(t_points, y_points, kind='quadratic')
# R^2 for linear spline
linear_r2 = r2_score(A * np.sin(w * inc_t_points), linear_interp(inc_t_points))
# R^2 for quadratic spline
quadratic_r2 = r2_score(A * np.sin(w * inc_t_points), quadratic_interp(inc_t_points)
```

Problem 1 - Code

```
# Plotting
fig, ax = plt.subplots()
ax.plot(t, y, label='y = A sin(wt)', color='blue')
ax.scatter(t_points, y_points, color='red', label='Chosen Points')
ax.plot(t, linear_interp(t), label=f'Linear Spline (R^2={linear_r2:.3f})', line
ax.plot(t, quadratic_interp(t), label=f'Quadratic Spline (R^2={quadratic_r2:.3f
ax.set_xlabel('Time (s)')
ax.set_ylabel('y')
ax.legend()
plt.title('Linear and Quadratic Spline Interpolations with R^2 Evaluation')
plt.show()
```

Linear:

$$ec{P}=ec{P_0}(1-t)+ec{P_1}t$$

Quadratic:

$$\vec{A} = \vec{P_0}(1-t) + \vec{P_1}t$$
; $\vec{B} = \vec{P_1}(1-t) + \vec{P_2}t$; $\vec{P} = \vec{A}(1-t) + \vec{B}t$
 $\Rightarrow \vec{P} = \vec{P_0}(1-t)^2 + 2\vec{P_1}t(1-t) + \vec{P_2}t^2$
 $= \vec{P_0}(1-2t+t^2) + \vec{P_1}(2t-2t^2) + \vec{P_2}(t^2)$

Cubic:

$$\begin{split} \vec{A} &= \vec{P_0}(1-t) + \vec{P_1}t \; ; \; \vec{B} = \vec{P_1}(1-t) + \vec{P_2}t \; ; \; \vec{C} = \vec{P_2}(1-t) + \vec{P_3}t \\ \vec{D} &= \vec{A}(1-t) + \vec{B}t \; ; \; \vec{E} = \vec{B}(1-t) + \vec{C}t \; ; \; \vec{P} = \vec{D}(1-t) + \vec{E}t \\ \Rightarrow \vec{P} &= \vec{A}(1-t)^2 + 2\vec{B}t(1-t) + \vec{C}t^2 \\ &= \vec{P_0}(1-t)^3 + \vec{P_1}t(1-t)^2 + 2\vec{P_1}t(1-t)^2 + 2\vec{P_2}t^2(1-t) + \\ \vec{P_2}t^2(1-t) + \vec{P_3}t^3 \\ &= \vec{P_0}(1-3t+3t^2-t^3) + \vec{P_1}(3t-6t^2+3t^3) + \vec{P_2}(3t^2-3t^3) + \vec{P_3}(t^3) \end{split}$$

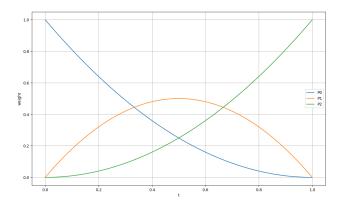


Fig. 3.1 Quadratic weights

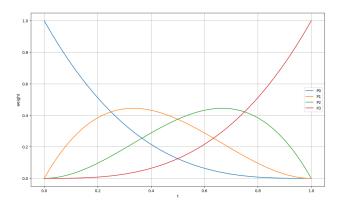


Fig. 3.2 Cubic weights

Problem 3 - Code

```
import matplotlib.pyplot as plt
import numpy as np
#weights for linear curve
wt=[np.polynomial.Polynomial([1,-1]),np.polynomial.Polynomial([0,1])]
#calculate weights for nth order curve
def wts(new_wt,n,ctr=1):
   global wt
    if ctr<n:
        temp=[np.polynomial.Polynomial([0])]*(len(new_wt)+1)
        for i in range(len(wt)):
            for j in range(len(new_wt)):
                temp[i+j]=np.polynomial.polynomial.polyadd(temp[i+j],(np.polyno
        return wts(temp,n,ctr+1)
   return new_wt
t=np.linspace(0,1,num=100)
```

Problem 3 - Code

```
def plot(x,wt,n):
    wt=wts(wt,n)
    for i in range(n+1):
        plt.plot(x,wt[i][0](x),label='P'+str(i))
    plt.legend()
    plt.xlabel('t')
    plt.ylabel('weight')
    plt.grid()
    plt.show()
```

It appears that loops come to fruition upon the following condition $x_2 < x_0 < x_3 < x_1$ or $x_1 < x_3 < x_0 < x_2$ and y_1, y_2 lie on the same side of the line containing y_0, y_3

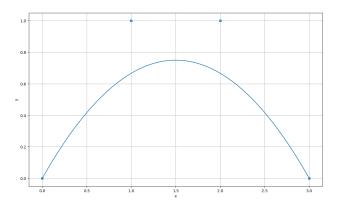


Fig. 4.1 $x_0 < x_1 < x_2 < x_3$

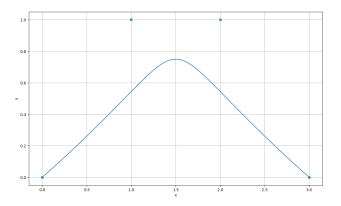


Fig. 4.2 $x_0 < x_2 < x_1 < x_3$

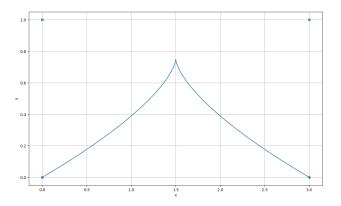


Fig. 4.3 $x_0 = x_2 < x_1 = x_3$

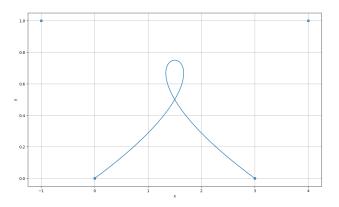


Fig. 4.4 $x_2 < x_0 < x_3 < x_1$

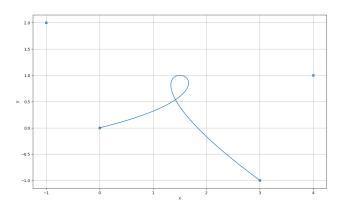


Fig. 4.5 y_1, y_2 lie on same side

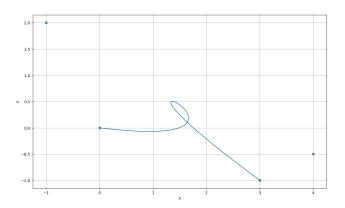


Fig. 4.6 y_1, y_2 lie on same side

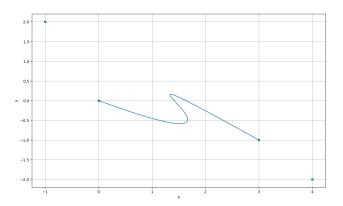


Fig. 4.7 y_1, y_2 lie on opposite sides

Problem 4 - Code

t=np.linspace(0,1,num=100)

```
import matplotlib.pyplot as plt
import numpy as np
#weights for linear curve
wt=[np.polynomial.Polynomial([1,-1]),np.polynomial.Polynomial([0,1])]
#calculate weights for nth order curve
def wts(new_wt,n,ctr=1):
   global wt
   if ctr<n:
        temp=[np.polynomial.Polynomial([0])]*(len(new_wt)+1)
        for i in range(len(wt)):
            for j in range(len(new_wt)):
                temp[i+j]=np.polynomial.polynomial.polyadd(temp[i+j],(np.polyno
        return wts(temp,n,ctr+1)
   return new wt
#array containing points P_0, P_1 ... P_n
P=np.array([np.array([0,0]),np.array([4,-2]),np.array([-1,2]),np.array([3,-1])]
```

Problem 4 - Code

```
def plot(x,wt,n):
                         #n=order of curve
    wt=wts(wt,n)
    new_x=np.zeros(len(x))
    new_y=np.zeros(len(x))
    for i in range(n+1):
        new_x=new_x+P[i][0]*wt[i][0](x)
        new_y=new_y+P[i][1]*wt[i][0](x)
    plt.plot(new_x,new_y)
    plt.scatter(np.transpose(P)[0],np.transpose(P)[1])
    plt.grid()
    plt.xlabel('x')
    plt.ylabel('y')
    plt.show()
plot(t,wt,3)
```