

BRIGHT GALAXIES AS REDSHIFT TRACERS FOR DARK SIREN COSMOLOGY

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A dissertation submitted to Ghent University in partial fulfilment of the requirements for the degree of
Master of Science in Physics and Astronomy

Academic year: 2024 - 2025



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AY 2024-2025

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Ghent, June, 2025

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Acknowledgement

Abstract

Abstract (Nederlands)

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List of Abbreviations

GW	Gravitaional-Wave	xi
CBC	compact binary coalescence	9
LVK	LIGO, Virgo, KAGRA	6
BNS	binary neutron star	11
BBH	binary black hole	11
NSBH	neutron star black hole	19
EM	Electromagnetic	xi
LOS	line-of-sight	xii
SNR	signal-to-noise ratio	7
SNe	supernovae	9
GWTC	Gravitational-Wave Transient Catalog	6
BCG	Brightest Cluster Galaxy	16
MDC	Mock Data Challenge	27
DES	Dark Energy Survey	27
KDE	kernel density estimation	30
CMB	cosmic microwave background	xiii
SHOES	Supernovae H0 for the Equation of State	3
HST	Hubble Space Telescope	3
SNe Ia	Type Ia supernovae	2
TRGB	Tip of the Red Giant Branch	4
BAO	Baryon Acoustic Oscillations	5

JWST James Webb Space Telescope	3
ADDGALS Adding Density-Determined Galaxies to Lightcone Simulations . .	40
SDSS Sloan Digital Sky Survey	40
MDC Mock Data Challenge	27

Introduction

1.1 The Hubble Constant

The Hubble constant, denoted H_0 , quantifies the present-day expansion rate of the Universe. An empirical relationship between galaxy redshift and distance was published by Edwin Hubble in 1929 (Hubble, 1929), showing that galaxies recede from us at velocities proportional to their distances. A few years earlier, Georges Lemaître had independently derived a similar velocity-distance relation in 1927 (Lemaître, 1927), based on theoretical grounds using general relativity and available data. This linear relation, now known as Hubble's law, is expressed as:

$$v = H_0 d \quad (1.1)$$

where v is the recession velocity and d is the proper distance to the galaxy. This linear relationship forms the foundation of modern observational cosmology, and established the expanding Universe as a cornerstone of modern cosmology laying the foundation for the standard cosmological model.

In modern terms, the Hubble constant also governs the shape of the luminosity distance-redshift relation and determines the age and size of the Universe. In a flat Λ CDM cosmology, the Hubble constant enters the luminosity distance formula as:

$$d_L(z) = \frac{c(1+z)}{H_0} \int_0^z \frac{dz'}{\sqrt{\Omega_m(1+z')^3 + \Omega_\Lambda}}. \quad (1.2)$$

Accurate measurements of H_0 are essential for understanding the expansion history of the Universe and for anchoring other cosmological parameters. However, different observational methods have yielded inconsistent values, leading to a discrepancy, what is now known as the *Hubble tension*.

1.1.1 Early H_0 Measurements

The quest to measure the Hubble constant has a long history, beginning with Hubble's original work in the 1920s. The first estimates of H_0 were based on the apparent brightness of Cepheid variable stars in nearby galaxies, which were used as standard

candles (Hubble, 1929). These early measurements were limited by the available technology and the uncertainties in distance measurements.

In the 1930s, Edwin Hubble and Milton Humason measured redshifts and estimated distances to additional galaxies at Mount Wilson Observatory. Their work led to an initial estimate of $H_0 \approx 500 \text{ km s}^{-1} \text{ Mpc}^{-1}$, significantly higher than current values (Hubble, 1936). The discrepancy was largely due to underestimating galaxy distances and misidentifying Cepheid populations.

Throughout the 1940s and 1950s, astronomers like Walter Baade and Fritz Zwicky introduced new distance indicators, such as the use of Population I and II stars, and proposed Type Ia supernovae as standard candles (Baade, 1979a; Baade, 1979b; Zwicky, 1942). Baade's recalibration of Cepheid distances effectively halved Hubble's original value, leading to estimates closer to $H_0 \approx 250 \text{ km s}^{-1} \text{ Mpc}^{-1}$ (Baade, 1979a; Longair, 2006).

Later on, the advent of techniques such as surface brightness fluctuations and the discovery of quasars enabled distance measurements over greater cosmological scales. However, large discrepancies persisted, with estimates of H_0 ranging from 50 to $100 \text{ km s}^{-1} \text{ Mpc}^{-1}$ (Sandage, 1958; Vaucouleurs, 1972; Sandage and Tammann, 1982; De Vaucouleurs, 1985).

With the advent of the 21st century and significant advancements in both space-based and ground-based observational capabilities, including high-resolution radio telescopes and precision optical instruments, two independent and fundamentally different methods for measuring the Hubble constant emerged. One approach relies on the cosmic distance ladder, anchored by Cepheid variables and Type Ia supernovae, while the other infers H_0 from early-Universe observations of the CMB, interpreted through the standard Λ CDM cosmological model.

1.2 Modern Cosmology and the Hubble Tension

1.2.1 Local measurements: Cosmic Distance Ladder

The traditional approach to measuring H_0 is the *cosmic distance ladder*, which combines a series of interconnected distance indicators. The ladder begins with geometric parallax for nearby stars, continues with Cepheid variable stars in more distant galaxies, and culminates in the use of Type Ia supernovae (SNe Ia) as standard candles

at cosmological distances. Each rung of the ladder calibrates the next, enabling a distance-redshift relation that extends to hundreds of megaparsecs (Freedman et al., 2001; Riess et al., 2019; Freedman and Madore, 2010; Riess et al., 2022).

The 1980s and 1990s saw significant advancements in distance measurement techniques, including the use of the *Hubble Space Telescope* (*HST*) and improved calibration methods. The introduction of the *HST* in 1990 allowed for more precise measurements of Cepheid variables in nearby galaxies, leading to a more accurate determination of H_0 . The *HST Key Project*, led by Freedman et al., used Cepheids in host galaxies of Type Ia supernovae to derive a value of $H_0 = 72 \pm 8 \text{ km s}^{-1} \text{ Mpc}^{-1}$ (Freedman et al., 2001). This result significantly improved both the precision and reliability of local distance measurements.

The Supernovae H0 for the Equation of State (SH0ES) project, which built upon the *HST Key Project*, further refined the measurement of H_0 using a larger sample of Cepheid-calibrated supernovae. Recently, in 2022, they reported a value of $H_0 = 73.30 \pm 1.04 \text{ km s}^{-1} \text{ Mpc}^{-1}$ (Riess et al., 2022). Recently, results from the James Webb Space Telescope (JWST) have also emerged (Freedman et al., 2024). These results, while consistent with previous measurements, raise questions about the underlying physics of cosmic expansion.

While the cosmic distance ladder achieves high precision, it involves multiple sources of systematic uncertainty at each step including stellar evolution models, metallicity corrections, dust extinction, and supernova standardization, all of which must be carefully calibrated and validated.

1.2.2 Indirect measurements: Cosmic Microwave Background

The second approach to measuring H_0 relies on the *CMB* radiation, which provides a snapshot of the Universe at a much earlier time. The CMB is a relic radiation from the hot, dense state of the early Universe, and its temperature fluctuations encode information about the density and expansion rate of the Universe.

By fitting the observed power spectrum to the standard ΛCDM model, one can infer a value of the Hubble constant indirectly. This method relies on model assumptions, especially the flatness of the Universe and the constancy of dark energy. While not a direct measurement, the CMB-based value of H_0 is internally consistent and extremely precise.

The introduction of the *Planck* satellite in 2009 provided a new avenue for measuring H_0 through observations of the CMB. The CMB measurements, combined with the standard Λ CDM model, yielded a value of $H_0 = 67.4.30 \pm 0.5 \text{ km s}^{-1} \text{ Mpc}^{-1}$ (Aghanim et al., 2020). This value was significantly lower than the local measurements obtained from Cepheid-calibrated supernovae, leading to the emergence of the so-called *Hubble tension*.

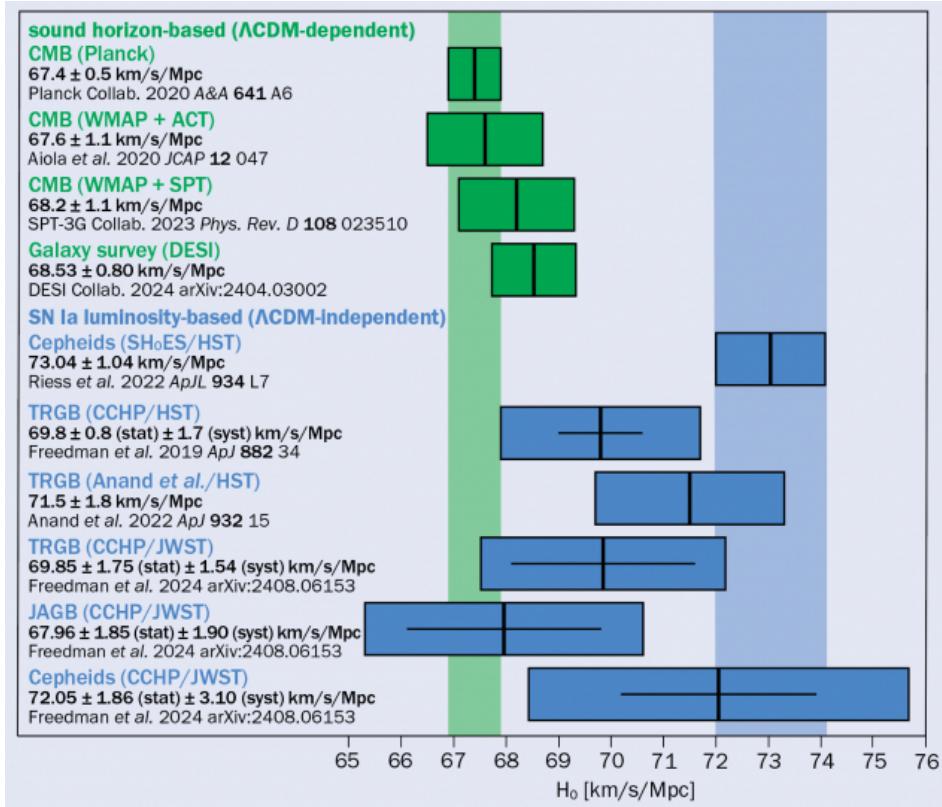


Fig. 1.1: Hubble tension: Comparison of the local and CMB-based measurements of H_0 over the years (CERN, 2025).

1.2.3 The Hubble Tension and quest for independent measurements

The Hubble tension, now exceeding 5σ , is one of the most significant unresolved issues in cosmology and has prompted investigations into both systematic errors and possible extensions to the standard cosmological model. Independent methods are therefore crucial for arbitrating between these measurements. These include:

- **Tip of the Red Giant Branch (TRGB)**

The TRGB method uses the well-defined luminosity at which low-mass stars ignite helium as a standard candle. This luminosity, shows minimal sensitivity to stellar population effects and dust, making it a robust alternative to Cepheid variables. The Carnegie-Chicago Hubble Program has applied this method

to derive an independent calibration of Type Ia supernovae and obtained H_0 values closer to those inferred from the CMB (Freedman et al., 2024). As such, TRGB offers a valuable cross-check on the Cepheid-based ladder.

- **Baryon Acoustic Oscillations (BAO)**

BAO are imprints of sound waves in the early Universe, visible as a characteristic scale in the clustering of galaxies. This scale acts as a standard ruler and allows geometric distance measurements across cosmic time. When combined with redshift data and a calibration from the sound horizon measured by the CMB, BAO can be used to infer H_0 (Cuceu et al., 2019; Alam et al., 2021). Although BAO are not purely local measurements, they offer a powerful, independent cosmological probe that is less susceptible to astrophysical systematics.

- **Gravitational-wave standard sirens**

The use of gravitational-wave events as standard sirens provides a unique opportunity to measure H_0 independently. The use of GW sources as *standard sirens* (Schutz, 1986), provide a direct measurement of the luminosity distance through their waveform. When combined with a redshift, obtained either via electromagnetic counterparts or galaxy catalogs, these events can trace the distance-redshift relation and yield an independent estimate of the Hubble constant.

Standard sirens can be categorized into two broad categories: bright sirens and dark sirens, depending on whether an electromagnetic counterpart is detected. This thesis explores one implementation of this approach, focusing on *dark sirens*: gravitational-wave events without identified electromagnetic counterparts. By statistically associating these events with potential host galaxies in wide-field catalogs, we aim to extract constraints on H_0 . In particular, we investigate how restricting the galaxy catalog to its brightest subsets can improve the resulting cosmological inference.

Together, these emerging methodologies, TRGB, BAO, and standard sirens, form a triangulation of H_0 that spans distinct epochs and assumptions. Whether the Hubble tension reflects unknown systematics or fundamentally new physics, its resolution will likely come from the convergence (or divergence) of these independent measurements.

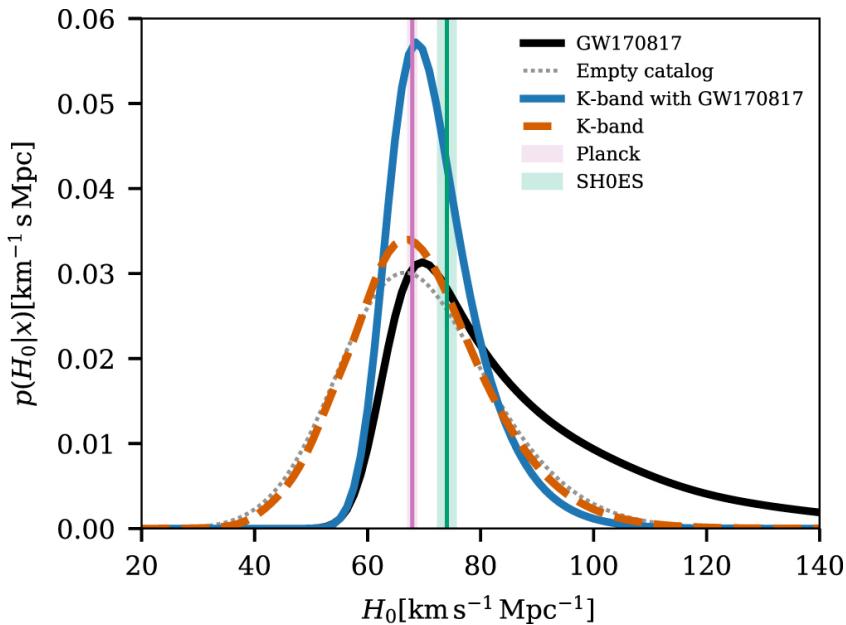


Fig. 1.2: Hubble constant posterior from Gravitational-Wave Transient Catalog (GWTC)-3 released by the LIGO, Virgo, KAGRA (LVK) collaboration, compared to the CMB and local measurements. The tension between these measurements is evident, with the GW posteriors (blue/orange), with/without the sole bright siren evenet, being consistent with both Planck (pink) and SH0ES measurements, owing to the rather wide constraints. Additionally, the empty catalog (gray) and the bright siren (black) results are also plotted (Abbott et al., 2023a).

1.3 GW Cosmology

GW observations have introduced a novel, independent method for measuring cosmological distances: the so-called *standard sirens*. First proposed by Schutz (1986), standard sirens are the gravitational-wave analogs of EM standard candles, such as Type Ia supernovae. Unlike EM methods, standard sirens enable a direct, calibration-free determination of the luminosity distance from the observed waveform of a compact binary coalescence.

The amplitude and frequency evolution of the GW signal encodes the luminosity distance, which can be inferred under the assumption of general relativity. However, GW detectors are not sensitive to the redshift of the source. Therefore, to place a GW event on the Hubble diagram and infer the Hubble constant H_0 , one must independently obtain the redshift.

In the case of bright sirens, events with an EM counterpart, such as GW170817 (Abbott et al., 2017), the redshift can be directly measured from the host galaxy spectrum. For the more common class of dark sirens, such as GW170814 (Soares-Santos et al., 2019), where no EM counterpart is detected, a statistical association is made between the GW localization volume and galaxy catalogs. This association

yields a redshift probability distribution, which can be combined with the luminosity distance posterior to constrain H_0 .

The promise of standard sirens lies in their independence from traditional distance ladders and CMB modeling. This makes them a crucial tool in addressing the Hubble tension. They are free from many astrophysical systematics affecting EM methods, such as dust extinction, metallicity effects, or empirical calibrations. Additionally, because GWs are less susceptible to environmental interactions, they can probe larger cosmological volumes with fewer intermediate assumptions. As GW detectors improve in sensitivity and the number of observed events increases, standard sirens are expected to play a progressively larger role in cosmological inference.

1.4 Thesis Objectives

The primary objective of this thesis is to investigate the impact of using brightness-ranked galaxy catalogs on the precision of H_0 measurements from dark sirens. By focusing on the brightest galaxies, we aim to improve the statistical constraints on H_0 while minimizing systematic uncertainties associated with galaxy catalog incompleteness.

This work involves H_0 inference using the `gwcosmo` pipeline, which combines GW distance posteriors with galaxy redshift priors. We will explore the effects of applying brightness cuts to the galaxy catalog, examining how these cuts influence the resulting H_0 posterior distributions. The analysis will be performed on a subset of GWTC-3 events, focusing on those with high signal-to-noise ratios (SNRs) and no known electromagnetic counterparts. The results will be validated through the use of simulated catalogs and mock data challenges, allowing us to assess the robustness of our findings.

In Chapter 2, we will provide an overview of the theoretical framework for standard siren cosmology, including the principles of dark sirens. We will also discuss the challenges and limitations associated with this approach, particularly in the context of galaxy catalog incompleteness. Chapter 3 details the data sources used in our analysis, including the GW event catalog and galaxy catalogs. We will describe the selection criteria for the events and the modelling of missing EM data. In Chapter 4, we will detail the methodology used in our analysis, including the construction of brightness-ranked galaxy catalogs and the statistical techniques employed to derive redshift priors. In particular the `gwcosmo` pipeline will be introduced, which combines the GW distance posterior with the galaxy redshift prior to infer H_0 . In this chapter we also present our results using real data and discuss the impact

of brightness cuts on the resulting H_0 posterior distributions. In Chapter 5, we will present the results of our analysis using simulated catalogs and mock data challenges, allowing us to assess the robustness of our findings. Finally, in Chapter 6, we will summarize our findings and discuss their implications for future research in cosmology.

Gravitational-Wave Cosmology

2.1 Standard Siren Cosmology

The detection of GW from compact binary coalescences (CBCs) have opened a transformative avenue in modern cosmology. These events acts as *standard sirens*, the gravitational analog of standard candles, as the luminosity distance (d_L) to a GW source is directly encoded in the strain amplitude and frequency evolution of the GW. The amplitude, corrected for antenna pattern and inclination, provides a direct, calibration-free distance measurement under the assumption of general relativity.

From Maggiore (2007), the strain measured by a GW detector can be expressed as:

$$h(t) = \frac{4}{d_L} \left(\frac{G\mathcal{M}_z}{c^2} \right)^{5/3} (\pi f(t))^{2/3} F(\iota, \psi, \theta, \phi) \quad (2.1)$$

where:

- $h(t)$ is the strain measured at time t ,
- d_L is the luminosity distance to the source,
- $\mathcal{M}_z = (1+z)\mathcal{M}$ is the redshifted chirp mass,
- $f(t)$ is the instantaneous GW frequency,
- $F(\iota, \psi, \theta, \phi)$ is a function that captures the detector response depending on inclination angle ι , polarization angle ψ , and sky position (θ, ϕ) .

The amplitude scaling with $1/d_L$ makes it possible to extract the luminosity distance directly from the signal, once the source's intrinsic properties and orientation are marginalized over. Furthermore, the $1/d_L$ scaling, in comparison to the $1/d_L^2$ scaling of EM signals, means that GW signals allow observations of sources at much larger distances, making them ideal for cosmological applications.

The direct self-calibrated measurement of the luminosity distance from the GW signal is a key advantage of standard sirens over traditional EM standard candles. This is in stark contrast to traditional EM standard candles, such as supernovae (SNe), where the distance is inferred from the observed flux and requires a calibration step to

account for the intrinsic brightness of the source. The GW signal is also less affected by the intergalactic medium, as it is not subject to scattering or absorption like EM signals. This allows for a more direct measurement of the distance to the source not affected by dust extinction or other astrophysical uncertainties that plague EM observations. This makes GW standard sirens a powerful tool for cosmology.

The concept of standard sirens was first introduced by Bernard F. Schutz, who noted that if the redshift of a GW source can be measured, one could use GW events to trace the expansion history of the universe, in particular an independent measurement of the Hubble constant (H_0) (Schutz, 1986). This is due to the relation between the luminosity distance, redshift and the Hubble constant, in a flat Λ CDM cosmology, being:

$$d_L = \frac{c(1+z)}{H_0} \int_0^z \frac{dz'}{\sqrt{(1+z')^3 \Omega_m + \Omega_\Lambda}} \quad (2.2)$$

Unlike traditional EM methods, which require cross-calibration across multiple rungs of the distance ladder (parallax, Cepheids, SNe Ia) with each step introducing uncertainties that compound, the standard siren approach provides a direct cosmological probe. This reduces systematic uncertainties and provides an independent check on other H_0 measurement techniques, possibly providing a solution to the Hubble tension, the current discrepancy between local and global measurements of the Hubble constant (Riess et al., 2019; Aghanim et al., 2020).

However, a key limitation is that while GW detectors provide a precise measurement of d_L , they do not directly measure the redshift. This necessitates an independent redshift measurement to place the source on the Hubble diagram. For *bright sirens*, this redshift is obtained from the host galaxy identified via the electromagnetic counterpart. In contrast, for *dark sirens*, the redshift is inferred statistically by cross-referencing the GW localization volume with galaxy catalogs or by leveraging population-based methods, as discussed in the following sections.

This forms the basis for *standard siren cosmology*, where GW sources are used as cosmic rulers. Over the past decade, this idea has transitioned from theoretical speculation to experimental reality, primarily through observations made by the LVK collaboration. The first GW event, **GW150914**, was detected in 2015, marking the beginning of a new era in astrophysics and cosmology (Abbott et al., 2016). Since then, the LVK collaboration has detected numerous GW events, including binary black hole mergers, binary neutron star mergers, and neutron star-black hole mergers. These observations have provided valuable insights into the nature of gravity, the formation of compact objects, and the expansion history of the universe.

2.2 Bright vs. Dark Sirens

Standard sirens fall into two broad categories: *bright sirens* and *dark sirens*, depending on whether an electromagnetic counterpart is detected.

Bright sirens are rare but powerful. A prime example is **GW170817**, a binary neutron star (BNS) merger detected by LIGO-Virgo in 2017, which was accompanied by a short gamma-ray burst and subsequent kilonova (Abbott et al., 2017). This multi-messenger event enabled the unambiguous identification of its *host galaxy*, NGC 4993, providing both distance (from GW) and redshift (from optical spectroscopy) measurements. The resulting Hubble constant measurement was a major milestone demonstrating that GW observations could offer an independent and competitive cosmological probe (Abbott et al., 2017).

Such bright sirens provide a straightforward route to cosmological inference, using independent distance and redshift measurements. However, bright sirens require specific astrophysical conditions: the emission of EM signals strong enough to be detected, accurate sky localization, and timely follow-up by optical telescopes. Such conditions are only met for a small fraction of CBC events, especially those involving neutron stars. Majority of the observed mergers, especially binary black holes (BBHs) do not produce detectable EM counterparts, and are thus classified as dark sirens.

In the absence of a direct redshift measurement, dark sirens require a *statistical approach*. This involves cross-matching the sky localization and distance posterior from the GW event with a galaxy catalog covering the relevant region. The redshift information of a number of candidate galaxies is then used to statistically infer the likely redshift distribution of the source. This is done by constructing a *LOS redshift prior* for each GW event, which is then used to infer the Hubble constant. The LOS redshift prior is constructed by taking into account the galaxy number density and redshift distribution within the localization volume of the GW event. The GW localization volume is typically much larger than the volume of a galaxy, leading to a large number of galaxies that could potentially host the GW event. This results in a large number of potential redshift measurements, which can be used to construct a more accurate LOS redshift prior.

The statistical nature of dark sirens allows for the inclusion of a larger number of events, as it does not rely on the detection of an EM counterpart. This is particularly important for BBH events, which are more common and have a higher detection rate than BNS events. The LVK collaboration has detected numerous dark siren events, which have been used to constrain the Hubble constant and test cosmological models.

As the number of BBH detections increases with each observing run, dark sirens will dominate the future of standard siren cosmology. However, this statistical method introduces new complexities and depends heavily on the quality and completeness of the galaxy catalog used, which plays a pivotal role in the reliability of the inferred Hubble constant. The incompleteness of the galaxy catalog can lead to biases in the inferred redshift distribution, which can affect the accuracy of the Hubble constant measurement. This is particularly important for dark sirens, as they rely on the statistical association of GW events with galaxies in the catalog. State of the art dark siren methods have been developed to mitigate these issues, but they still rely on the quality and completeness of the galaxy catalog used. The next section discusses the current state of the art in dark siren cosmology, including the challenges and limitations of existing methods.

2.3 State of the Art Dark Siren Methods

The statistical framework for dark siren cosmology has evolved rapidly. Early implementations relied on basic overlap between GW localization volumes and precompiled galaxy catalogs. The first generation of tools, including `gwcosmo` (Gray et al., 2020; Gray et al., 2022; Gray et al., 2023) and `icarogw` (Mastrogiovanni et al., 2021; Mastrogiovanni et al., 2024), introduced a more rigorous Bayesian framework: for each GW event, a *LOS redshift prior* is constructed using galaxy number counts and redshifts, weighted by host probability, typically modeled using stellar mass proxies such as K -band luminosity.

One major challenge in this process is that current galaxy catalogs, such as **GLADE+** (Dálya et al., 2022), are incomplete beyond low redshift (typically $z > 0.2 - 0.3$). This incompleteness leads to a nontrivial *out-of-catalog* term in the redshift prior, which must be modeled analytically using a *Schechter luminosity function*. This function estimates the number density of missing faint galaxies, often assuming fixed parameters (e.g., M_* , α) calibrated from deep surveys. If this modeling is inaccurate, the resulting posterior for H_0 can be biased or artificially broadened.

Despite these challenges, dark siren methods have been successfully applied to increasingly large datasets. The LVK collaboration has published joint analyses using CBC events from the **O1**, **O2**, and **O3** observing runs. For instance, Abbott et al., 2021a; Abbott et al., 2023a presented cumulative constraints on H_0 using numerous CBC events, demonstrating convergence toward a 10–15% precision regime, albeit still limited by catalog systematics.

These analyses highlight the potential of dark sirens to provide competitive cosmological constraints, especially as galaxy catalogs improve and detection rates increase. Future observing runs, such as O4 and O5, are expected to significantly enhance the statistical power of dark siren cosmology, potentially reducing uncertainties in H_0 , providing better constraints on cosmological model, and testing the validity of general relativity on cosmological scales. The next generation of GW detectors, such as the **Einstein Telescope** and **Cosmic Explorer**, will further enhance the sensitivity and detection rates of GW events, opening up new avenues for cosmological exploration.

2.3.1 Redshift Inference Methods

In dark siren cosmology, two principal strategies exist for inferring the redshift of gravitational-wave sources: the *catalog-based method*(CITATION NEEDED) and the *population-based method* (Ezquiaga and Holz, 2022). The catalog method, discussed earlier, statistically associates GW sources with galaxies from a survey by constructing a redshift prior along each line of sight, derived from galaxy positions and redshifts within the GW localization volume. This approach captures the clustering of galaxies and allows for redshift inference when direct EM counterparts are absent, but suffers from incompleteness at higher redshifts and spatial variation in survey depth(CITATION NEEDED). Conversely, the population method, often referred to as the *spectral siren approach*, leverages features in the observed distribution of source-frame binary parameters, especially masses, which are redshifted in the detector frame. If the intrinsic mass distribution contains recognizable structure (e.g., a cutoff or peak), its displacement due to cosmic redshift can break the mass-redshift degeneracy, enabling cosmological inference independent of galaxy surveys (Ezquiaga and Holz, 2022). However, this approach is sensitive to modeling assumptions about the underlying binary population.

Recent work has sought to improve robustness by combining dark siren methods with *spectral sirens*, extracting redshift information from the observed mass distribution of GW sources under population synthesis assumptions (Ezquiaga and Holz, 2022). These hybrid approaches aim to reduce dependence on incomplete catalogs and mitigate selection biases while extracting maximal cosmological information from current GW detections. Recently, both `gwcsmo` and `icarogw` have been updated to support such joint inference schemes (Gray et al., 2023; Mastrogiovanni et al., 2024).

2.3.2 Galaxy Weighting Choices

In the construction of the LOS redshift prior, each host galaxy is weighted by the probability of hosting a GW event. This probability is typically modeled as a function of the galaxy's luminosity, and relies on the assumption that the merger host probability of a galaxy is related to its luminosity in a specific band. The choice of band remains uncertain, with different bands correlating with different aspects. The blue band, for instance, correlates with star formation rate and is therefore appropriate for mergers with short time delays (coalescence shortly after formation), while the near-infrared band correlates with the total luminous mass and is thus appropriate for mergers with longer time delays (mergers in older, more evolved galaxies). It is not known how exactly galaxy color is correlated with the merger rate.

For modelling the out-of-catalog contribution, a Schechter luminosity function is assumed, which describes the distribution of galaxy luminosities in a given band. Wrong assumptions on the Schechter parameters, or incorrect description of selection biases can lead to biases in the inferred Hubble constant. The key assumption in constructing the out-of-catalog contribution is that the galaxy catalog is magnitude limited, i.e. galaxies are not detected only because they are too faint. If other selection biases (based on e.g., colors or spectral features) were present, the out-of-catalog contribution would be biased, leading to an incorrect estimate of the redshift prior (Abbott et al., 2023a).

If the assumption of a magnitude-limited catalog is valid, then the luminosity function of the galaxy catalog would match the assumed Schechter function at its bright end, and then start to decrease as it reaches the corresponding absolute magnitude threshold. As can be seen in Figure 2.1, this is indeed the case for the K -band luminosity function, which is well described by the assumed Schechter function. The B_J -band luminosity function, on the other hand, is not well described by the assumed luminosity function, and the assumption of a magnitude-limited catalog is not valid as there seem to be some additional missing galaxies at low redshift. This could lead to an incorrect estimate of the out-of-catalog contribution, and therefore an incorrect estimate of the redshift prior (Abbott et al., 2023a).

For this reason, traditionally, the K -band luminosity has been used for galaxy weighting in GW cosmology inference pipelines. This is also due to the fact that the K -band luminosity is better correlated with the stellar mass of the galaxy, making it a more reliable tracer of the underlying matter distribution (Strazzullo et al., 2006; Sureshkumar et al., 2021; Abbott et al., 2023a).

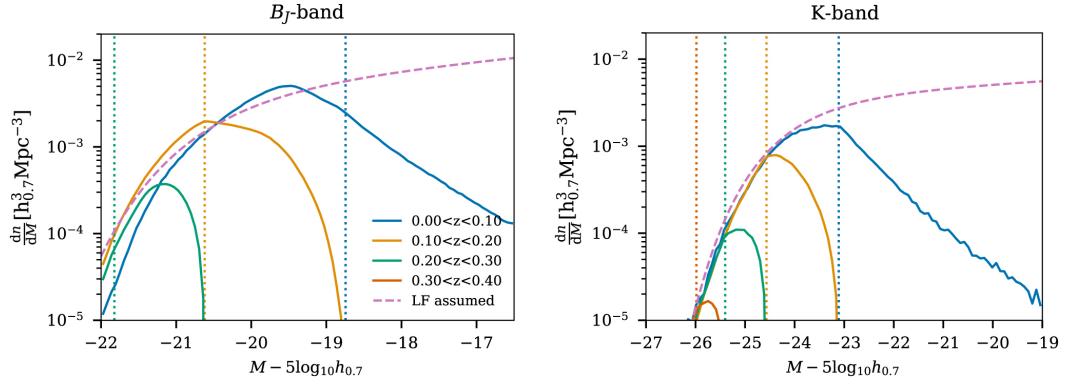


Fig. 2.1: The B_J -band luminosity function (left) and the K -band luminosity function (right) for the GLADE+ catalog. The solid lines show the luminosity function of the catalog, while the dashed lines shows the assumed Schechter function. The vertical dashed line indicates the median absolute magnitude threshold for galaxy detection. The bright end of the K -band luminosity seems to match the assumed Schechter function, while the B_J -band luminosity function does not. This indicates that the assumption of a magnitude-limited catalog is not valid for the B_J -band luminosity function (Abbott et al., 2023a).

However, this choice is not without its limitations. The K -band luminosity is not always available for all galaxies in the catalog, leading to potential biases in the selection of galaxies used to construct the redshift prior. For example, the K -band luminosity is only available for about 1 million galaxies in the GLADE+ catalog, which is a small fraction of the total number of galaxies in the catalog. This can lead to uncertainties in the redshift prior, which can in turn affect the inferred value of the Hubble constant. However, this effect should be relatively small, as we are interested in the overall matter distribution, and the K -band luminosity is a good tracer of the underlying matter distribution. This also forms the basis for this thesis, as we will be using the brightest galaxies in the K -band to trace the underlying matter distribution for improved H_0 inference as discussed in the next section.

2.4 Refining the Redshift Prior: Brightest Galaxies as Tracers

The current state of the art in dark siren cosmology relies heavily on the quality and completeness of the galaxy catalog used to construct the LOS redshift prior. The incompleteness of the galaxy catalog can lead to biases in the inferred redshift distribution, which can affect the accuracy of the Hubble constant measurement. State of the art dark siren methods have been developed to mitigate these issues, but they still rely on the quality and completeness of the galaxy catalog used.

One strategy to mitigate this limitation is by refining the construction of the redshift prior by focusing on the *brightest galaxies*, which are more likely to be catalogued and potentially better tracers of the underlying matter distribution. This would effectively make the catalog more complete and increase precision without introducing significant bias. The rationale is that the brightest galaxies are more likely to be associated with massive halos, which are more likely to host detectable GW events. The brightest galaxies are also more likely to be catalogued, as they are easier to detect and measure. These galaxies would also crudely trace the underlying matter distribution, as they are more likely to be associated with massive halos. This would be particularly useful for dark sirens, as they rely on the statistical association of GW events with galaxies in the catalog. By replacing the redshift of the true host galaxy with the redshift of a nearby bright galaxy in the catalog, the small error incurred would be insignificant compared to the overall uncertainty in the redshift prior and the luminosity distance measurement.

Figure 2.2 illustrates this approach, highlighting how the brightest galaxies can be used to trace the underlying matter distribution. The last two panels in the figure show an overly restrictive cut, which would lead to a loss of information and a biased redshift prior. This emphasizes the importance of selecting an optimal brightness cut that balances the need for completeness with the desire for precision. The goal would be to find the optimal brightness cut that maximizes the precision of the redshift prior while minimizing bias.

This approach, of using the brightest galaxies to trace the matter distribution, is similar to the *Brightest Cluster Galaxy (BCG)* method used in traditional cosmology, where the brightest galaxy in a cluster is used as a standard candle. The BCG method has been shown to be effective in reducing the scatter in distance measurements and improving the precision of cosmological constraints (Lauer et al., 2014). By applying a similar approach to dark sirens, one can potentially improve the precision of the inferred Hubble constant without introducing significant bias.

To implement this approach, we define a subset of the galaxy catalog, GLADEPXX, which includes only the top $XX\%$ of galaxies ranked by K -band luminosity, as the K -band luminosity is better associated with the mass of the galaxies (Strazzullo et al., 2006; Sureshkumar et al., 2021). The construction of the LOS redshift prior is then modified to account for this restricted catalog. Specifically, the Schechter luminosity function is adjusted to reflect the brighter subset, making the out-of-catalog contribution smaller, effectively making the catalog more complete. This modified prior is then used in the Bayesian framework to infer the Hubble constant.

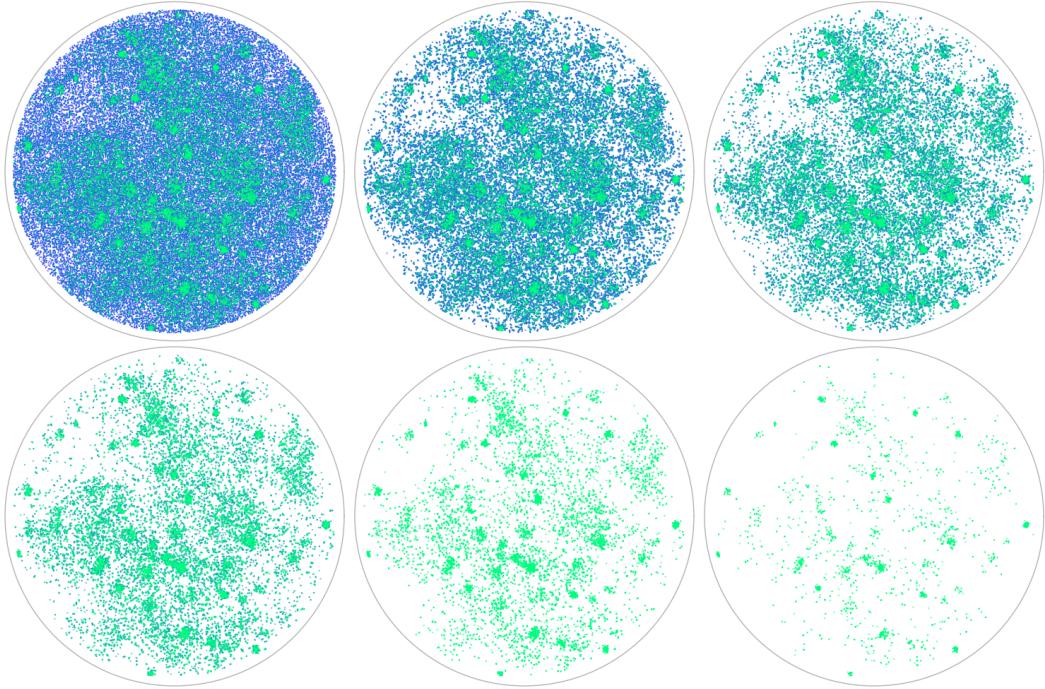


Fig. 2.2: Illustration of the proposed method for refining H_0 inference using the brightest galaxies as redshift tracers. The panels show different brightness cuts being applied to a galaxy catalog. The top left panel shows the case with a full galaxy catalog, while the subsequent panels (left-to-right) show the effect of applying increasingly strict brightness cuts. These depict how we can trace the matter distribution by using only the brightest galaxies. The last two panels (bottom center and right) show overly restrictive cuts, which would lead to a loss of information and a biased result. This is a conceptual visualization, generated with AI assistance, intended to represent the methodology rather than actual observational data.

The next chapters provide a detailed description of the methodology, including the selection criteria for GLADEPXX, the modeling of the out-of-catalog part and the validation of this approach using mock data.

Data

The foundation of any standard siren cosmological analysis lies in the quality, completeness, and coverage of the data. In this thesis, we rely on two primary data sources: GW observations from the LVK detectors, and galaxy catalogs providing EM redshift information. These datasets are used in tandem to statistically construct a redshift prior for each GW event and ultimately to constrain the Hubble constant H_0 .

3.1 GW Event Data

3.1.1 The GWTC-3 Catalog

The GW data used in this study are obtained from the *GWTC* (Abbott et al., 2019; Abbott et al., 2021b; Abbott et al., 2024; Abbott et al., 2023b). This catalog comprises all CBC events detected during the three observing runs (O1, O2, O3) of the Advanced LIGO and Virgo detectors. GWTC includes over 93 confident detections, primarily BBH mergers, with a few neutron star black hole (NSBH) and BNS systems.

3.1.2 Event Parameter Estimation?

Is it needed to mention the parameter estimation? I think not.

3.1.3 Event Selection Criteria

To focus our analysis on dark siren cosmology, we restrict our sample to events that do not have any confirmed electromagnetic counterpart (i.e., no associated kilonova or GRB), have a network SNR exceeding 11, have somewhat good sky localization, and are accompanied by publicly available posterior samples for distance and sky position.

These criteria are designed to ensure both the statistical robustness of the inference and compatibility with existing galaxy catalogs. After applying these cuts, a subset of 47 events, with 42 BBHs, 3 NSBHs, and 2 BNSs, is retained for cosmological analysis.

3.1.4 Distance Posteriors and Sky Localization

Each event is characterized by a posterior distribution over the three-dimensional localization volume, typically encoded using the HEALPix format. The posterior provides the probability density $p(d_L, \alpha, \delta)$, where d_L is the luminosity distance and (α, δ) denote right ascension and declination.

These distance posteriors are crucial for constructing the LOS redshift prior when cross-matched with galaxy catalogs. Events with poor localization or multimodal distance distributions contribute more uncertainty to the inferred H_0 , emphasizing the importance of event quality.

3.1.5 Assumptions About the Source Population

Although this thesis primarily focuses on statistical redshift modeling, it is important to acknowledge that the cosmological inference also depends weakly on assumptions about the source population. For instance, `gwcosmo` allows one to specify priors on:

- Merger rate evolution with redshift, typically modeled as $R(z) \propto (1+z)^\kappa$
- Mass distributions of the binaries

For our analysis we assume that CBCs follow a Madau-Dickinson merger redshift evolution model (Madau and Dickinson, 2014):

$$R(z) = R_0(1+z)^\gamma \frac{1 + (1+z_p)^{-(\gamma+\kappa)}}{1 + \left(\frac{1+z}{1+z_p}\right)^{\gamma+\kappa}} \quad (3.1)$$

Here R_0 is the local merger rate, κ the high-z slope, γ the low-z slope and z_p the break-point. All the assumed priors are given in Table 3.1. **TODO: add sources for the parameters.**

For BBH we use power-law with a Gaussian peak mass model, with powerlaw slope α , the mean of the Gaussian σ_g , the width of the peak μ_g , and the relative weight between power-law and the peak λ_g . We also assume the minimum and maximum masses for the black hole distribution. For neutron stars we assume that mass is

Tab. 3.1: Priors on merger rate shape parameters.

Parameter	Prior
R_0	$1/R_0$ (implicit)
κ	2.86
γ	4.59
z_p	2.47

uniformly distributed between $M_{min,NS}$ and $M_{max,NS}$. All the assumed priors are given in Table 3.2. **TODO: add sources for the parameters.**

Tab. 3.2: Priors on the mass model parameters.

Parameter	Prior
α	3.78
σ_g	3.88
μ_g	32.27
λ_g	0.03
$M_{min,BH}$	$4.98M_\odot$
$M_{max,BH}$	$112.5M_\odot$
$M_{min,NS}$	$1.0M_\odot$
$M_{max,NS}$	$3.0M_\odot$

3.2 EM Galaxy Catalogs

3.2.1 The GLADE+ Catalog

For redshift information, we use the **GLADE+** galaxy catalog (Dálya et al., 2022), an extended version of the original GLADE catalog designed for GW follow-up. GLADE+ is a composite catalog that combines several large surveys to achieve all-sky coverage:

- 2MASS XSC and 2MPZ (infrared-based all-sky surveys)
- WISExSCOS (photometric redshifts)
- HyperLEDA (spectroscopic redshifts)
- SDSS DR16 (optical photometric and spectroscopic data)

As of the latest release, GLADE+ includes over 22 million objects with available positions, redshifts (spectroscopic or photometric), and photometry in multiple bands, most critically the K -band.

3.2.2 Catalog Completeness

A significant limitation of GLADE+ is its incompleteness beyond redshift $z \sim 0.3$. While the catalog is approximately complete for bright galaxies at low redshift, its coverage of fainter galaxies or more distant regions is limited. This incompleteness introduces a bias when performing statistical redshift inference, as missing galaxies contribute to the out-of-catalog part of the redshift prior.

To address this, the `gwcosmo` pipeline models the galaxy population using a truncated Schechter luminosity function:

$$\phi(M) \propto 10^{0.4(\alpha+1)(M-M^*)} \exp[-10^{0.4(M-M^*)}] \quad (3.2)$$

where M is the absolute magnitude in the K -band, M^* is the characteristic magnitude, and α is the faint-end slope. For our analysis, we adopt the standard parameters: $\alpha = -1.09$, $M_K^* = -23.39 + 5 \log h$, consistent with Kochanek et al., 2001, and truncate at $M_{K,min}^* = -27.00 + 5 \log h$ and $M_{K,max}^* = -19.00 + 5 \log h$.

3.2.3 Redshift Uncertainty Modeling

Redshift measurements in GLADE+ are heterogeneous. Spectroscopic redshifts are generally precise, but photometric redshifts can have uncertainties on the order of $\sigma_z \sim 0.01 - 0.05$. These uncertainties are modeled by convolving the redshift of each galaxy with a Gaussian of fixed width, an assumption used in constructing the redshift prior.

Additionally, to reduce systematic error, galaxies with unphysical redshifts or unreliable photometry are filtered out during preprocessing. The net result is a cleaned, sky-localized, and redshift-tagged galaxy distribution that can be used for LOS prior construction.

Furthermore, K -corrections are applied in `gwcosmo` following Kochanek et al., 2001, and the apparent magnitude thresholds m_{thr} are computed per HEALPix pixel as a median apparent magnitude in a given pixel, giving a K -band threshold of 13.5 on average.

3.2.4 K -band Luminosity as Host Probability Proxy

In dark siren analysis, we must assign each galaxy a probability of being the true host. Following common practice, this probability is assumed to scale with stellar

mass, for which K -band luminosity serves as a good proxy **CITATION NEEDED**. The host probability p_i for each galaxy is given by:

$$p_i \propto L_{K,i} \quad (3.3)$$

This choice is motivated by the assumption that more massive galaxies are more likely to host CBCs events. While simplistic, it provides a reasonable baseline.

GLADE+ Bright Galaxies as Redshift Tracers

The core idea investigated in this thesis is the use of **bright galaxies** as redshift tracers for GW events. The GLADE+ galaxy catalog is a comprehensive database of galaxies in the local universe, but it suffers from incompleteness at high redshifts. This incompleteness arises from the limited depth of the catalog, which is primarily designed to cover the local universe, owing to the sensitivity constraints of the current EM telescope. We overcome this limitation by focusing on the brightest galaxies in the catalog, which are more likely to be well-represented and can provide a more accurate estimate of the redshift of GW events. This essentially makes the catalog deeper and more complete at high redshifts, while allowing us to use the GLADE+ catalog as a proxy for the underlying matter distribution in the universe.

4.1 Bright Galaxy Subsets

The analysis begins with the construction of **bright galaxy subsets**, denoted GLADEPXX, where only the top $XX\%$ of galaxies by cumulative K -band luminosity are included. The K -band luminosity is chosen as it is better associated with the mass of the galaxies (Strazzullo et al., 2006; Sureshkumar et al., 2021). Limiting the analysis to these bright subsets allows us to:

- Reduce the out-of-catalog correction by focusing on galaxies likely to be well-represented.
- Improve the signal-to-noise ratio of the statistical redshift prior.
- Minimize the inclusion of poorly characterized or faint galaxies.

The bright galaxy subsets are defined by selecting galaxies based on their absolute magnitude, which is inferred from their redshift and apparent magnitude. For a given subset, the dimmest galaxy sets the absolute magnitude limit, M_{max} , for that subset. This limit is then used in the Schechter luminosity function to adjust the out-of-catalog contribution, effectively reducing its impact. By focusing on the brightest galaxies, we assume that they trace the mass distribution in the Universe more effectively, and are more likely to host CBC events.

This approach improves the completeness of the galaxy catalog in the high-redshift regime, as the out-of-catalog contribution becomes smaller. Figure 4.1 illustrates how the redshift distribution shift towards higher values making the catalog more complete, highlighting the effectiveness of this method in probing deeper z -ranges.

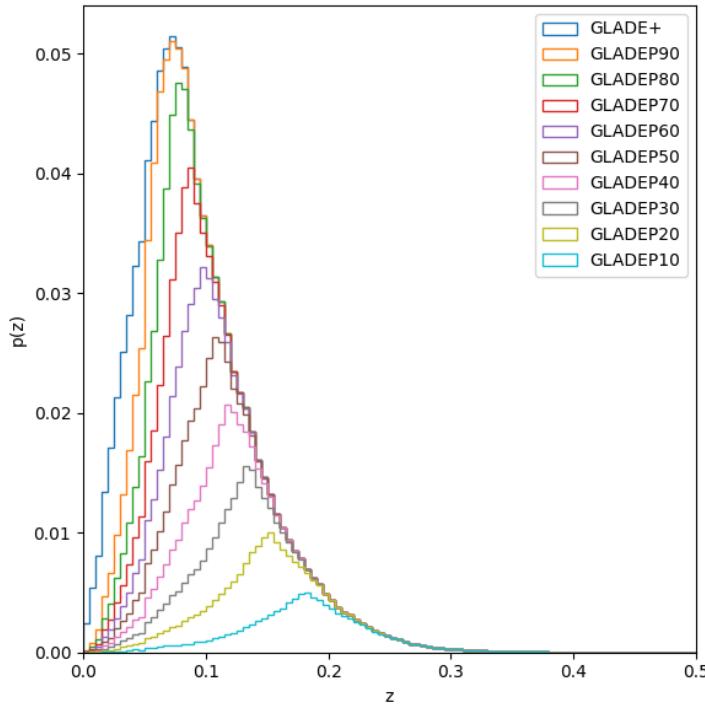


Fig. 4.1: Normalized redshift distributions $p(z)$ for the full GLADE+ galaxy catalogue (blue) and the brightest percentiles (other curves). Each subset, labeled “GLADEPXX,” includes only the top XX% brightest galaxies in the K -band. Focusing on increasingly brighter subsets shifts and sharpens the redshift distribution, effectively probing deeper ranges in z .

4.1.1 Trade-Offs and Limitations

While bright subsets reduce catalog incompleteness, they may inadvertently exclude genuine host galaxies, especially if those lie in less luminous systems or in under-represented regions of the catalog. The effectiveness of these cuts depends on the intrinsic distribution of host galaxies, the depth and completeness of the original catalog, and the accuracy of K -band photometry.

One major limitation of this approach is that brightest galaxies may not be representative of the overall galaxy population, as they may be biased towards certain types of galaxies or regions of the sky. This effect is however mitigated by the fact that we are using the K -band luminosities, which are good tracer for the stellar mass (Strazzullo et al., 2006; Sureshkumar et al., 2021), and in turn the overall matter distribution. Furthermore, the bright galaxy subsets are constructed from the

GLADE+ catalog, which is designed to be a complete and representative sample of galaxies in the local universe. This means that the bright galaxy subsets are likely to be representative of the overall galaxy population, and give a crude estimate of the matter distribution, even if they are not a complete sample.

Estimating the true redshift of a GW event by the nearest brightest galaxies is supposed to have a negligible effect on the results. This is because the bright galaxies are more likely to be located in regions of high density, such as galaxy clusters or groups, which are also likely to host GW events. This means that the bright galaxies are likely to be located in the same large-scale structure as the GW event, and thus provide a good estimate of the redshift of the event.

One important thing to note is that while the use of a bright subset enhances the completeness of the catalogue at high redshifts, it also introduces a trade-off. If the brightness cut is too restrictive, the exclusion of fainter galaxies may lead to an underrepresentation of the overall matter distribution, potentially biasing the results. One needs to carefully balance these considerations by comparing different brightness thresholds. A moderate brightness cut will maximize the benefit in terms of depth without incurring significant bias.

The appropriate brightness cut can be established only via a set of astrophysics-motivated large-scale simulations. A *GW Mock Data Challenge (MDC)* using the simulated BUZZARD galaxy catalog from the Dark Energy Survey (DES) Collaboration (DeRose et al., 2019; DeRose et al., 2022). It is designed to determine the optimal brightness threshold which maximizes the measurement precision with bright subsets while keeping the biases in control. Tests performed in the process will help refine the methodology and ensure that the improved constraints on the Hubble constant are robust against additional systematic uncertainties.

While the bright galaxy subsets may not be a perfect representation of the overall galaxy population, they are still a useful tool for improving the completeness of the galaxy catalog and reducing the out-of-catalog correction. The error incurred by using the bright galaxies as redshift tracers maybe small compared to the current errors in luminosity distance measurements from the GW events, this may become a problem in the future as the GW measurements become more precise. In this case, one may need to use more sophisticated methods to estimate the redshift of the GW event, such as more complex models of the galaxy population, but for now this is a good first step towards improving the completeness of the galaxy catalog and reducing the out-of-catalog correction, by leveraging the currently available EM data.

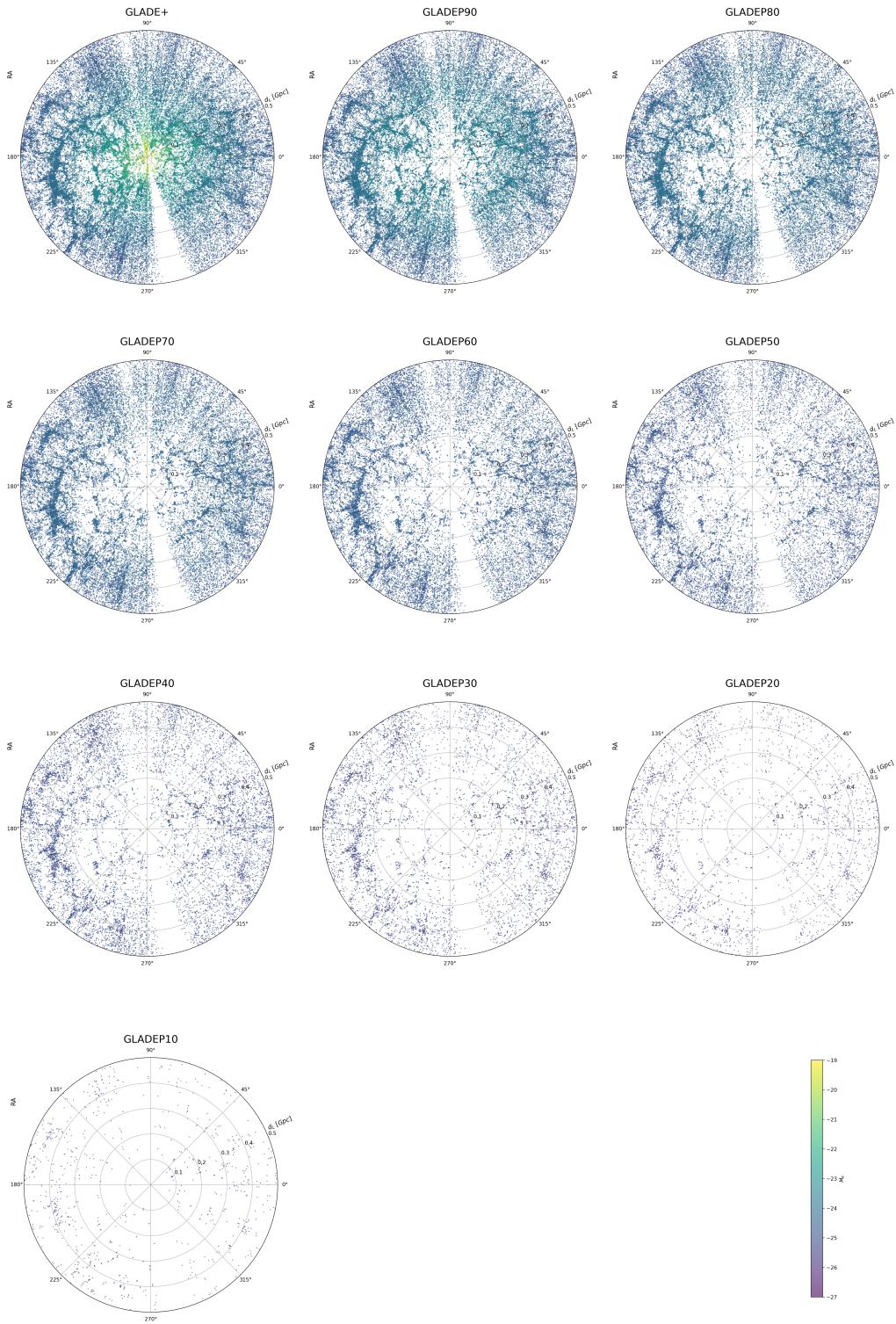


Fig. 4.2: Spatial distribution of galaxies from the GLADE+ catalog and its bright subsets, employed for dark standard siren cosmology. The plots show a 10-degree slice in declination, centered at 0° , with the radial coordinate representing luminosity distance d_L (in Gpc) and the angular coordinates being right ascension (RA). This shows how the bright galaxies trace the large-scale structure of the universe.

4.2 The `gwcosmo` Pipeline

Based on the work presented in Gray et al., 2020; Gray et al., 2022; Gray et al., 2023, `gwcosmo` is a Python package specifically designed for the joint inference of cosmological parameters using data from standard sirens and galaxy catalogs. The pipeline employs Bayesian inference techniques to simultaneously constrain cosmological parameters, such as the Hubble constant and dark energy equation of state parameters. It does this using various data inputs, including the gravitational wave strain data from gravitational wave observatories such as LIGO, Virgo, and KAGRA, entries from galaxy catalogs containing photometric or spectroscopic redshift information, as well as other relevant galaxy properties, and CBC source population models.

`gwcosmo` represents a significant advancement in extracting cosmological information especially from CBC events that lack unique EM counterparts. It addresses the challenge of redshift inference in dark siren cosmology by statistically marginalizing over potential host galaxies from a flux-limited catalog. This is achieved through hierarchical Bayesian modeling that incorporates GW strain data, the spatial and redshift distribution of galaxies, and astrophysical population models.

The pipeline is designed to be flexible and extensible, allowing users to customize the models and priors used in the analysis. It also provides tools for visualizing the results, including posterior distributions and confidence intervals for the inferred parameters. The package is built on top of established libraries such as `numpy`, `scipy`, and `matplotlib`, making it accessible to researchers familiar with these tools. The `gwcosmo` pipeline is a particularly useful tool in the intersection of gravitational wave astronomy and cosmology, as it enables the extraction of valuable cosmological information from gravitational wave events, which can complement traditional methods of measuring cosmological parameters. The package is actively maintained and updated to incorporate new developments in both gravitational wave detection and cosmological modeling, ensuring that it remains a relevant tool for researchers in the field.

4.2.1 Bayesian Framework: **TO BE UPDATED** (see `gwcosmo` paper)

The goal is to evaluate the posterior distribution:

$$p(\Lambda \mid \{d_{\text{GW}}\}, \{d_{\text{EM}}\}) \propto p(\Lambda) p(\{d_{\text{GW}}\}, \{d_{\text{EM}}\} \mid \Lambda), \quad (4.1)$$

where:

- Λ are the hyperparameters of interest (e.g., cosmological parameters, population hyperparameters),
- d_{GW} are the GW observables (e.g., luminosity distance posteriors),
- d_{EM} are the galaxy catalogue data (e.g., redshifts, magnitudes, positions).

The likelihood is approximated by marginalizing over all galaxies k within the GW localization volume:

$$p(\Lambda \mid \{d_{\text{GW}}\}, \{d_{\text{EM}}\}) \propto \prod_i \sum_k w_k p(d_{\text{GW},i} \mid z_k, \Lambda), \quad (4.2)$$

where w_k is the weight assigned to each galaxy, typically modeled based on a proxy for host probability (e.g., luminosity in a selected band, merger rate evolution).

4.2.2 Key Features of `gwcosmo`

Some of the key features of the `gwcosmo` pipeline include:

- **Joint Population + Cosmology Inference:** Simultaneously samples over cosmological parameters and population hyperparameters, avoiding bias from fixed population assumptions.
- **Galaxy Catalogue Weighting:** Utilizes LOS redshift priors constructed from galaxy distributions, incorporating completeness corrections based on flux thresholds.
- **Selection Effects:** Corrects for GW detector sensitivity and incompleteness in galaxy catalogues by modeling detection probabilities and magnitude limits.

4.2.3 Implementation and Applications

The pipeline is implemented in Python and uses kernel density estimation (KDE) of GW posteriors and efficient catalog summation to handle discrete and incomplete galaxy data. The most recent version was applied by Gray et al., 2023 to reanalyze 47 events from the GWTC-3 catalog using the GLADE+ galaxy catalog, yielding an updated measurement of the Hubble constant:

$$H_0 = 69^{+12}_{-7} \text{ km s}^{-1} \text{ Mpc}^{-1}.$$

`gwcosmo` is publicly available and is expected to be a useful tool for future gravitational-wave cosmology with upcoming detector runs and deeper galaxy surveys.

4.3 LOS Redshift Prior

We base our analysis on the `gwcosmo` pipeline (Gray et al., 2020; Gray et al., 2022; Gray et al., 2023), which relies on a precomputed LOS redshift prior, a prior on the GW signal’s redshift and direction. This LOS redshift prior is used in tandem with the luminosity distance posterior from the GW signal, to get a measurement for the Hubble constant H_0 .

4.3.1 LOS Redshift Prior Construction

The LOS redshift prior is constructed from the GLADE+ galaxy catalog, which contains a wealth of information about the galaxies in the local universe. The redshift prior is constructed by taking into account the distribution of galaxies along the line of sight to the GW event, as well as their luminosity and redshift. This allows us to obtain a more accurate estimate for the redshift of the GW signal, which is crucial for cosmological measurements. The prior is constructed by dividing the sky into HEALPix pixels, and computing the redshift distribution of galaxies in each pixel. The redshift prior is then weighted using the luminosity of the potential host galaxies, allowing us to obtain a more accurate estimate for the Hubble constant.

Furthermore, the prior accounts for the incompleteness of the galaxy catalog, using source population models and the magnitude threshold calculated per pixel, which is particularly important for high-redshift events where the number of galaxies is significantly reduced. This allows us to separate the LOS redshift prior into an in-catalog and out-of-catalog contribution.

Taking into account, the fact that the host galaxy can be present, marked as G , or not, marked as \bar{G} , inside the catalog, one can write the LOS redshift prior as:

$$p(z|\Omega_i, \Lambda, s, I) = \iint \sum_{g=G, \bar{G}} p(z, M, m, g|\Omega_i, \Lambda, s, I) dM dm \quad (4.3)$$

$$\begin{aligned} &= p(G|\Omega_i, \Lambda, s, I) \iint p(z, M, m|G, \Omega_i, \Lambda, s, I) dM dm \\ &\quad + p(\bar{G}|\Omega_i, \Lambda, s, I) \iint p(z, M, m|\bar{G}, \Omega_i, \Lambda, s, I) dM dm \end{aligned} \quad (4.4)$$

The first term in the equation represents the contribution from galaxies that are present in the catalog, while the second term represents the contribution from galaxies not present in the catalog. The two terms are weighted by their respective probabilities of being present or not in the catalog. The terms inside the integral are the priors on the redshift z , absolute magnitude M , and apparent magnitude of the galaxies m , informed by the galaxy catalog, within the sky area covered by pixel i . Here the parameters G/\bar{G} give the presence or absence of the galaxy in the catalog, Ω_i the sky location of the GW event, Λ the cosmological and population hyperparameters of interest, s the presence of a GW source, and I the additional assumptions which are not explicitly expressed. One also needs to marginalize over the absolute magnitude M and the apparent magnitude m of the galaxy, as these determine, to the leading order, which galaxies are present in a flux-limited EM survey (Gray et al., 2023).

The integral in the in-catalog term can be expressed as the sum over the possible host galaxies in the catalog, weighted by their respective probabilities of being the host galaxy. These galaxies are weighted by their luminosity, which is a function of the absolute magnitude and redshift. The rationale being that the more luminous, and thus heavier galaxies are more likely to host CBC events, and therefore contribute more to the LOS redshift prior. This reduces the in-catalog part to a weighted sum over the galaxies in the catalog, where the galaxies are treated as point sources modeled by a Gaussian. This term can thus be expressed as:

$$\begin{aligned} \iint p(z, M, m | G, \Omega_i, \Lambda, s, I) dM dm &= \frac{1}{p(s|G, \Omega_i, \Lambda, I) N_{gal}(\Omega_i)} \\ &\times \sum_k^{N_{gal}(\Omega_i)} p(z|\hat{z}_k) p(s|z, M(z, \hat{m}_k, \Lambda), \Lambda, I) \end{aligned} \quad (4.5)$$

where the term $p(z|\hat{z}_k)$ represents the probability of a galaxy being at redshift z , given its observed redshift \hat{z}_k . This term is used to weight the contribution from each galaxy in the catalog, based on its observed redshift.

The integral in the out-of-catalog term marginalizes over the possible host galaxies not present in the catalog. This term is more complex, as it requires a model for the distribution of galaxies in the universe, which is not directly available from the catalog. We use a Schechter luminosity function to model the distribution of galaxies

in the universe, which allows us to estimate the contribution from galaxies outside the catalog. The out-of-catalog term can be expressed as:

$$\begin{aligned}
& \iint p(z, M, m | \bar{G}, \Omega_i, \Lambda, s, I) dM dm \\
&= \frac{1}{p(s | \bar{G}, \Omega_i, \Lambda, I) p(\bar{G} | \Omega_i, \Lambda, I)} \\
&\times \left[\Theta[z_{cut} - z] \int_{M(z, m_{th}(\Omega_i), \Lambda)}^{M_{max}(H_0)} p(z, M | \Lambda, I) p(s | z, M, \Lambda, I) dM \right. \\
&\quad \left. + \Theta[z - z_{cut}] \int_{M_{min}(H_0)}^{M_{max}(H_0)} p(z, M | \Lambda, I) p(s | z, M, \Lambda, I) dM \right]
\end{aligned} \quad (4.6)$$

Here we also account for the EM selection effects of the catalog. Due to the flux limited nature of the galaxy catalog, the probability of a galaxy being present in the catalog depends on the galaxy's apparent magnitude, and whether it is greater or smaller than apparent magnitude threshold of the catalog along the same line of sight, $m_{th}(\Omega_i)$. The Heaviside function Θ is used to separate the two cases of the out-of-catalog contribution, depending on whether the redshift z is below or above a certain threshold z_{cut} . This is due to the exclusion of galaxies with redshift z greater than z_{cut} from the catalog, which is a result of unreliable redshift or color information at these higher redshifts.

The term $p(s | z, M, \Lambda, I)$ is the weighting factor for the contribution from each galaxy, based on its luminosity and redshift. The galaxies are weighted by their luminosity in the K -band, which is a good tracer of the mass of the galaxies (Strazzullo et al., 2006; Sureshkumar et al., 2021). Furthermore, the merger host probability is also taken into account, which is a function of the redshift. This is modeled by a Madau-Dickinson merger rate evolution model (Madau and Dickinson, 2014), which describes the evolution of the merger rate with redshift, discussed in Section 3.1.5. The term $p(s | z, M, \Lambda, I)$, also incorporates the source population models, used to populate the out-of-catalog contribution. These models are also discussed in Section 3.1.5.

The term $p(z, M | \Lambda, I)$ represents the luminosity function of the galaxies, taken to be the Schechter luminosity function, discussed in Section 3.2.2. The integration limits are set by the minimum and maximum absolute magnitudes of the galaxies, $M_{min}(H_0)$ and $M_{max}(H_0)$. These are H_0 -dependent, as the parameters of the Schechter luminosity function are also H_0 -dependent, but the final distribution remains insensitive to the exact values of H_0 (Gray et al., 2023).

4.4 Results

In this chapter we present the main outcomes of our analysis: how applying brightness cuts to the GLADE+ catalog alters LOS redshift prior for individual events, how these modified priors propagate into the inferred posterior on the Hubble constant H_0 , and where the optimal balance lies between catalog depth and sampling variance.

To test the impact of catalog completeness, we apply successive cuts to the galaxy catalog by selecting only the brightest $XX\%$ of galaxies in K -band luminosity, forming subsets labeled GLADEPXX. This process shifts the effective magnitude threshold upward, reducing the number of galaxies but improving the catalog's completeness above the cut.

4.4.1 LOS Redshift Prior

Figure 4.3 shows the LOS redshift prior for the event GW170809 under different catalog cuts. Bright galaxy subsets (e.g., GLADEP20) result in sharper redshift distributions and reduce the weight of the out-of-catalog term. The low- z tail contributed by faint galaxies in the nearby universe is also suppressed. Notably, these priors maintain consistency in shape, indicating that bright galaxies are reliable tracers of large-scale structure. The application of a brightness cut significantly modifies the LOS redshift distribution. Specifically, the bright galaxy subsets yield an amplified redshift prior at higher distances, effectively extending the reach of the catalogue, somewhat mitigating the incompleteness issues that arise at deeper redshifts. This behavior is qualitatively consistent across events.

4.4.2 Hubble Constant Posterior

Once one has the LOS redshift prior, one can use it to compute the posterior distribution of the Hubble constant H_0 given the GW event data, as the relation between the redshift z , luminosity distance d_L and the Hubble constant H_0 is given by:

$$d_L = \frac{c(1+z)}{H_0} \int_0^z \frac{dz'}{\sqrt{(1+z')^3 \Omega_m + \Omega_\Lambda}} \quad (4.7)$$

for a flat Λ CDM cosmology. At lower redshifts, this can be simplified to:

$$d_L \approx \frac{cz}{H_0} \quad (4.8)$$

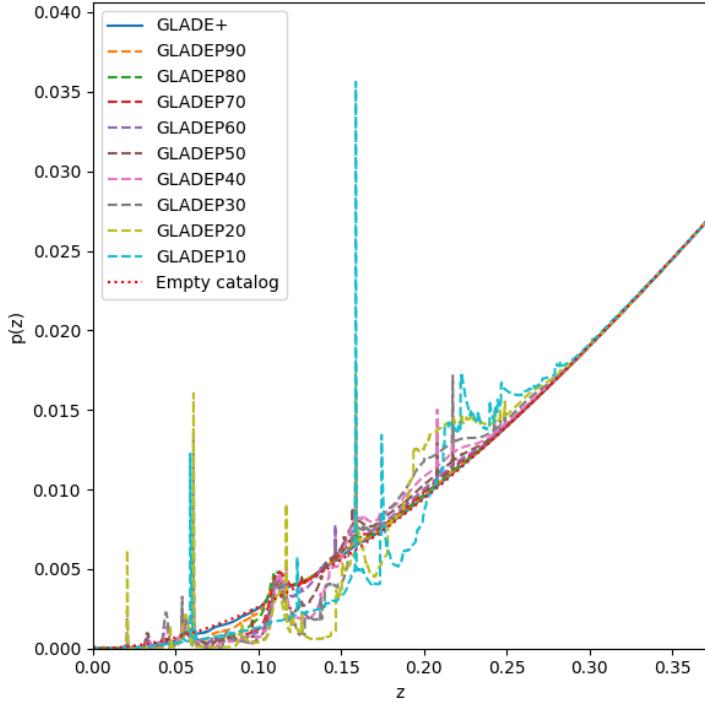


Fig. 4.3: LOS redshift prior for GW170809 for different brightness-ranked GLADE subsets. The full GLADE+ catalog (solid blue) is compared to the different subsets. Applying a brightness cut amplifies the prior at higher distances, extending the effective reach of the catalog and partially mitigating incompleteness at greater redshifts.

Thus the LOS redshift prior, $p(z|\Omega_i, \Lambda, s, I)$, and the luminosity distance posterior, $p(d_L, \Omega | \text{GW})$, from the GW event data can be combined to obtain the posterior distribution of H_0 , which can then be used to obtain constraints on the value of H_0 .

Figure 4.4 shows the resulting H_0 posteriors for GW170809 under various catalog cuts. As the catalog is restricted to brighter galaxies, the H_0 posterior becomes increasingly narrow. For example, GLADEP20 yields a visibly tighter posterior compared to the full GLADE+, with minimal shift in the median. However, the most aggressive cut (GLADEP10) introduces broader tails, likely due to insufficient galaxy sampling in the localization volume. (**LINK TO THE 20% LIMIT IN BUZZARD?**)

We repeat this procedure for a subset of BBH events from GWTC that meet our selection criteria. Figure 4.5 shows the combined H_0 posterior from the selected dark siren events using the full GLADE+ catalog and the different subsets.

Table 4.1 summarizes the H_0 posteriors for all cuts. The uncertainty is minimized around the GLADEP20 subset, showing 30-40% tighter constraints, while median values shift towards a higher value. For less extreme cuts, the median values doesn't

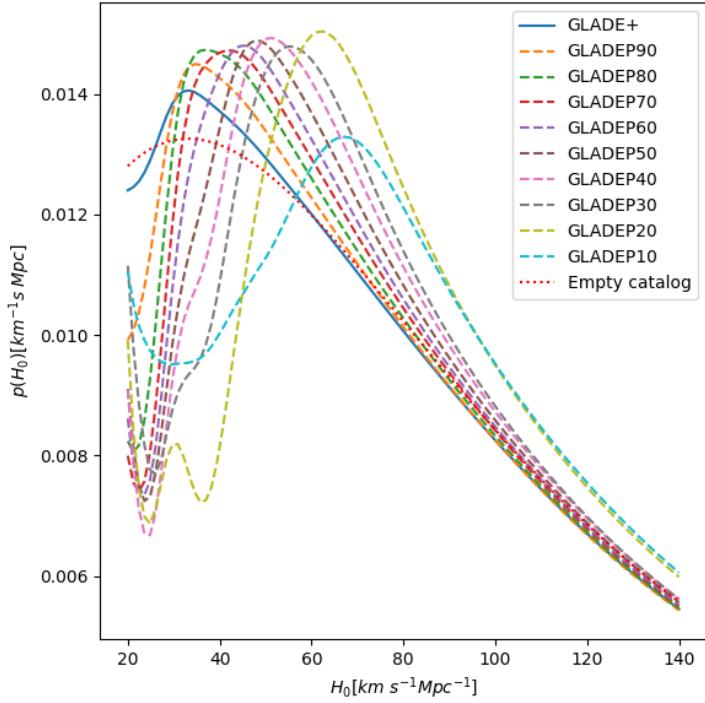


Fig. 4.4: H_0 posterior distributions for GW170809 using full and brightness-cut galaxy catalogs. GLADEP20 yields the tightest credible interval. GLADEP10 suffers from sparse sampling.

show a huge shift. This suggests that moderate brightness cuts improve precision without introducing systematic bias.

4.4.3 Cost-Benefit Trade-Off

We observe that precision improves with increasing brightness until an optimum is reached (near GLADEP20). Beyond this point, the posterior widens again, moving towards an empty catalog result, due to under-sampling. This defines a practical limit for catalog pruning. In real applications, the exact optimum may depend on event SNR, catalog completeness, and the merger rate model.

Our results suggest that targeting the brightest galaxies in a well-characterized catalog can substantially improve the statistical precision of H_0 constraints from dark sirens. This approach complements other efforts to mitigate catalog incompleteness, including joint inference with galaxy clustering and population-informed redshift estimation.

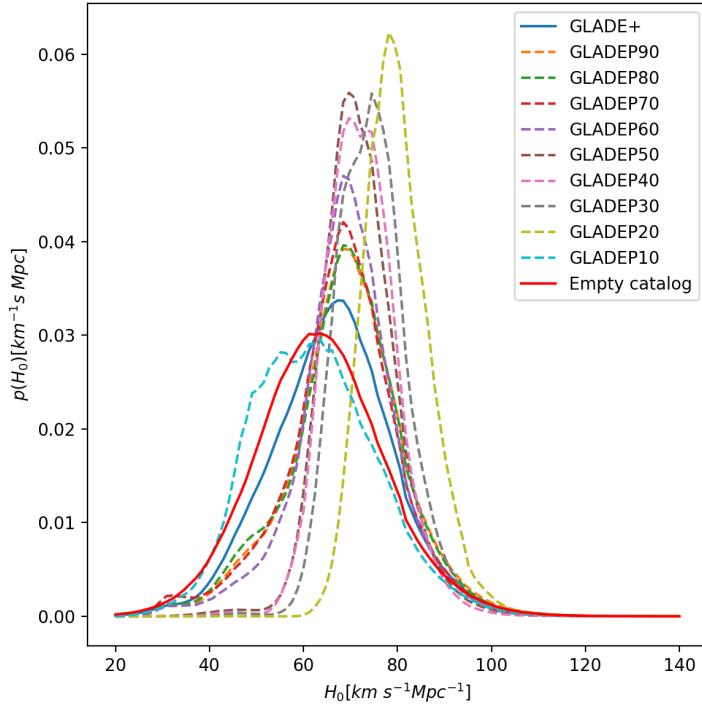


Fig. 4.5: Cumulative H_0 posterior from the selected dark siren events using full GLADE+ (blue) and the different subsets (dashed lines). The brightness-weighted catalog yields a tighter constraint without a significant shift.

Tab. 4.1: Maximum *a posteriori* probabilities with 68% confidence ranges of the H_0 posterior distributions alongside the maximum magnitude limits for the different percentiles of the GLADE+ galaxy catalogue.

Catalogue	$M_{K,max}$	H_0 [$\text{km s}^{-1}\text{Mpc}^{-1}$]
GLADE+	-19.00	$67.87^{+8.97}_{-10.29}$
GLADEP90	-23.07	$68.94^{+9.24}_{-7.55}$
GLADEP80	-23.62	$68.93^{+9.25}_{-7.57}$
GLADEP70	-23.94	$68.63^{+8.61}_{-7.42}$
GLADEP60	-24.19	$68.85^{+7.72}_{-6.43}$
GLADEP50	-24.14	$70.05^{+6.12}_{-5.20}$
GLADEP40	-24.63	$69.94^{+7.46}_{-3.88}$
GLADEP30	-24.87	$74.70^{+4.69}_{-6.58}$
GLADEP20	-25.15	$78.28^{+5.53}_{-4.95}$
GLADEP10	-25.53	$63.46^{+6.39}_{-14.37}$

Mock Data Challenge

To validate the method developed in this thesis, we conduct a Mock Data Challenge (MDC) using simulated GW events and galaxy catalog. The goal of this challenge is to assess the robustness of our inference pipelines and the impact of different brightness cuts on the measurements derived from GW observations. The MDC is designed to mimic real-world scenarios, allowing us to evaluate the performance of our methods under controlled conditions. This is done with the help of the BUZZARD mock catalogs, which provide a realistic simulation of the galaxy distribution and properties in the universe. The MDC will involve generating synthetic GW events, simulating their detection by LVK detectors, and analyzing the resulting data using our inference pipelines.

5.1 BUZZARD Mock Catalog

Cosmological analyses increasingly rely on simulated galaxy catalogs to test, validate, and calibrate inference pipelines. Among the most sophisticated of these are the BUZZARD mock catalogs presented by DeRose et al. (2019), a suite of synthetic sky simulations designed to closely emulate observations from the Dark Energy Survey (DES). The BUZZARD project aims to produce realistic mock universes that replicate the key statistical, spatial, and photometric properties of large-area surveys (DeRose et al., 2019; DeRose et al., 2022). These mocks are particularly useful for evaluating systematic uncertainties, testing survey strategies, and validating cosmological pipelines, including those involving standard sirens.

The BUZZARD mocks are constructed through a multi-step process that integrates large-scale dark matter simulations with empirical galaxy assignment and ray-traced gravitational lensing. The underlying dark matter distribution is generated using N -body simulations run using the 2LPTIC (Crocce et al., 2006) and LGADGET2 code (Springel, 2005). The simulations follow the evolution of particles under gravity across large comoving volumes, capturing the hierarchical growth of structure in a flat Λ CDM cosmology. The cosmological parameters used in the simulation are detailed in Table 5.1. Three lightcones covering different redshift regimes, denoted L1, L2, and L3, are used to build a deep mock catalog that spans from redshift $z \sim 0$ to $z \sim 2.35$, with increasing resolution and particle number at lower redshifts to mimic the increasing survey completeness at low z .

Tab. 5.1: The Λ CDM cosmology parameters used in the BUZZARD simulations.

Parameter	Description	Value
Ω_m	Matter density parameter	0.286
H_0	Hubble constant	$70 \text{ km s}^{-1} \text{ Mpc}^{-1}$
σ_8	Matter density fluctuation quantifying the clumpiness of matter distribution	0.815
n_s	Scalar spectral index: scale dependence of the primordial density perturbations	0.965
Ω_b	Baryon density parameter	0.046
N_{eff}	Effective number of neutrino species	3.046

Dark matter halos are identified in the simulation snapshots using the ROCKSTAR halo finder (Behroozi et al., 2012a), which groups particles into gravitationally bound objects based on adaptive phase-space density estimation. Temporal halo merger trees are constructed with the CONSISTENT-TREES algorithm (Behroozi et al., 2012b), enabling tracking of individual halos across cosmic time. These trees are crucial for assigning realistic galaxy properties and modeling assembly history.

Once the halo population is established, galaxies are inserted using the Adding Density-Determined Galaxies to Lightcone Simulations (ADDGALS) algorithm (Wechsler et al., 2022). ADDGALS is a semi-empirical prescription that associates galaxies with dark matter particles based on the local density field, using relationships inferred from observations such as the Sloan Digital Sky Survey (SDSS). Specifically, the algorithm calibrates the conditional luminosity function, the probability of a galaxy having a given luminosity in a particular local density environment, such that the final galaxy sample reproduces the observed luminosity function and galaxy clustering statistics (DeRose et al., 2019; Wechsler et al., 2022).

Each synthetic galaxy is assigned rest-frame and observed-frame photometry in multiple DES bands (e.g., g , r , i , z), drawn from a training set derived from real SDSS data (DeRose et al., 2019). This ensures that the color-magnitude distribution of BUZZARD galaxies matches the data, which is essential for generating realistic photometric redshifts. Photometric errors and selection effects are modeled to mimic DES observations, including depth variations and photometric scatter.

An important feature of BUZZARD is the inclusion of weak gravitational lensing through full-sky ray-tracing with the CALCLENS algorithm (Becker, 2013). CALCLENS computes the lensing convergence, shear, and magnification along each line of sight by integrating over the matter distribution in the simulation. These quantities are then assigned to each galaxy, enabling synthetic lensing measurements. This is particularly important for cosmological studies involving large-scale structure, cosmic shear, and galaxy bias calibration.

The final BUZZARD realizations contain over 800 million galaxies each and cover more than 10,000 square degrees of sky, comparable to the footprint of the full DES. The mocks include a variety of galaxy samples such as REDMAGIC (a luminous red galaxy sample with low photo-z scatter) and METACALIBRATION (used for weak lensing shear measurements).

These samples are used in key DES analyses and their inclusion in BUZZARD makes the mock catalogs highly relevant for pipeline validation.

BUZZARD has been extensively validated against DES Year 1 (Y1)–DES Year 2 (Y2) data, demonstrating good agreement in angular correlation functions, redshift distributions, galaxy-galaxy lensing signals, and shear measurements. The photometric redshift performance in BUZZARD mimics that of DES pipelines, allowing realistic estimation of redshift uncertainty impacts. These qualities make BUZZARD an ideal environment for end-to-end tests of cosmological inference workflows.

The first BUZZARD data release, BUZZARD DR1, has been made publicly available. It consists of multiple simulations to generate a mock galaxy catalog covering the same sky area as the Dark Energy Survey (DES) surveys. It contains more than 3 billion galaxies with realistic properties, including redshift distributions, luminosity functions, and clustering statistics. In order to facilitate simulated analyses of existing and upcoming large scale structure surveys, photometry is provided in multiple bands, including the DECam (u, g, r, i, z, Y), VISTA (z, Y, J, H, K_s), WISE ($W1, W2$), Rubin (u, g, r, i, z, Y), and Roman (Y, J, H, K) passbands.

In this thesis, the BUZZARD mock catalog is used to evaluate the impact of galaxy catalog properties on the measurement of the Hubble constant H_0 from dark sirens. Specifically, they allow controlled tests of how catalog pruning, for instance, selecting only the brightest galaxies, affects the redshift prior and the resulting cosmological inference. Because BUZZARD includes realistic magnitude distributions, redshift evolution, and clustering properties, it provides a physically motivated and statistically robust testbed for these experiments.

For our analysis, we use the Roman K -band luminosities of the galaxies in the BUZZARD catalog, based on the rationale that K -band luminosities are good tracers for the stellar mass(**CITATION NEEDED**). Furthermore, we apply an apparent magnitude threshold of 18 to the catalog to replicate realistic observational conditions, albeit with a somewhat optimistic depth. This apparent magnitude cut is chosen to ensure that the catalog contains a sufficient number of galaxies for statistical analysis. The resulting catalog, referred to as BUZZARD m_{18} , contains approximately 9.2 million galaxies with K -band apparent magnitudes brighter than 18, spanning redshifts from $z = 0$ to $z = 2.35$. The BUZZARD catalog is then cross-matched with the GW events generated by GWSim, detailed in the next section, to create a realistic dataset for our analysis. We then use this apparent magnitude limited catalog to select only the brightest galaxies, in order to test our results from GLADE+.

The use of BUZZARD thus supports one of the main goals of this thesis: to develop and validate a method for extracting cosmological information from gravitational-wave observations without electromagnetic counterparts, using only statistically constructed galaxy redshift priors. By using BUZZARD to test this methodology on a simulated sky, we can quantify biases, evaluate uncertainties, and refine our technique.

5.2 GWSim

To validate our methodology and assess the performance of standard siren inference using galaxy catalogs, we require a controlled and physically motivated sample of GW events with known properties. For this purpose, we use `GWSim` (Karathanasis et al., 2023), a publicly available Python package designed to generate realistic mock catalogs of GW events from BBH mergers, incorporating both astrophysical source population models and cosmological assumptions.

`GWSim` enables simulation of GW events from a wide range of mass, spin, and merger rate distributions, within cosmological frameworks such as flat Λ CDM, w_0 CDM, and w_0-w_a CDM models. Each mock event is associated with a redshift and sky location, and can be assigned to a host galaxy either by sampling from an isotropic homogeneous distribution or by drawing directly from a user-provided galaxy catalog. In our analysis, we use `GWSim` in conjunction with the complete BUZZARD mock catalog to create realistic GW injections associated with galaxies that replicate the large-scale structure and photometric properties of DES-like surveys.

The simulation pipeline consists of several modular steps:

- **Source Population Modeling:** The intrinsic BBH population is defined using a combination of merger rate models (e.g., constant, phenomenological, or delay-time models), mass distributions (e.g., power-law, power-law + Gaussian, or multi-peak), and spin distributions (e.g., uniform, Gaussian, or mass-correlated). We adopt a truncated power-law with Gaussian peak for the mass distribution and assume no spin dependence for simplicity. The same source population model discussed in Section 3.1.5 is used, in order to isolate the effects of the galaxy catalog on H_0 inference.
- **Cosmological Framework:** For each GW source, the redshift and luminosity distance are related through cosmological parameters. In this study, we assume a flat Λ CDM cosmology with the same parameters as used in the BUZZARD simulations (see Table 5.1).
- **Host Galaxy Assignment:** GW events are assigned to galaxies in the BUZZARD catalog using a merger-rate-weighted sampling. We optionally apply luminosity weighting in the K -band to preferentially select massive galaxies, as motivated by the correlation between K -band luminosity and stellar mass(**CITATION NEEDED**). This is done by assigning the weight of each galaxy to be proportional to its Roman K -band luminosity. Assuming the same host galaxy weighting in the `gwcosmo` analysis and injection generation, detailed in Section 3, allows us to avoid the problem of incorrect host weighting in the inference step, which can lead to biased results.
- **Detection Modeling:** The GW strain and signal-to-noise ratio (SNR) are computed assuming the sensitivity curves and duty cycles of the LIGO, Virgo, KAGRA (LVK)

detector network for observation run O4 over a period of 1 year. Only events with network SNR exceeding a detection threshold ($\text{SNR} > 11$) are retained.

- **Parameter Estimation:** For each detected event, posterior samples of source parameters are generated using the `Bilby` package (Ashton et al., 2019; Ashton and Talbot, 2021). These include the luminosity distance, component masses, sky location, and binary inclination, forming the basis for cosmological inference.

5.3 H_0 Inference with `gwcosmo`

Once we have generated a set of mock GW events, we can cross-match them with the BUZZARD galaxy catalog and its brightest subsets to create realistic datasets for our analysis. For each catalog, this involves associating each event with its corresponding host galaxy, which is crucial for constructing the redshift prior and performing the cosmological inference. The cross-matching process takes into account the sky localization of the GW events and the spatial distribution of galaxies in the catalog, ensuring that we accurately capture the potential host galaxies for each event.

In order to model the out-of-catalog contribution to the redshift prior, we also need to account for the galaxies that are not included in the BUZZARD catalog. This is done by assuming a Schechter luminosity function for the galaxy population, as discussed in Section 3.2.2. Here, it has to be noted that the Roman K -band luminosity function in BUZZARD is not the same as the one used in earlier analysis using the GLADE+ catalog. For this reason, we estimate the Schechter function parameters for the BUZZARD_{m18} catalog, BUZZARD catalog with an apparent magnitude threshold of 18, using the $1/V_{max}$ estimator described in Schmidt (1968) and Takeuchi et al. (2000). This gives us a Schechter function with $\alpha = 1.26$, $M_K^* = -22.07 + 5 \log h$, $M_{K,min} = -26.00 + 5 \log h$, and $M_{K,max} = -18.00 + 5 \log h$.

Once we have the Schechter function parameters, we can use them to model the out-of-catalog contribution to the redshift prior. This allows us to construct the redshift prior for each GW event, and estimate the Hubble constant H_0 using `gwcosmo`, analogous to Chapter 4. Here it is to be noted that the source population model used in `gwcosmo` is the same as the one used in `GWSim`. Furthermore, the same cosmological parameters and host galaxy weighting are used in both `GWSim` injection generation and `gwcosmo` analysis to ensure consistency in the analysis. This is crucial for obtaining reliable results and minimizing biases in the inferred H_0 values, isolating the effects of the use of galaxy catalog subsets as redshift tracers.

The use of `GWSim` in conjunction with the BUZZARD catalog provides a self-consistent mock dataset that closely mirrors observational data. This allows us to assess how galaxy brightness cuts can affect the resulting H_0 posterior distributions and the overall performance of our inference pipelines.

5.4 Results

Conclusion

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