Computer Science 384 St. George Campus February 7, 2025 University of Toronto

Homework Assignment #2: Constraint Satisfaction **Due: March 4, 2025 by 11:00 PM**

Late Policy: Please refer to the Course Information sheet posted on Quercus. Please note that grace tokens will be applied **automatically** as long as you submit your assignment during the grace token period.

Total Marks: This assignment represents 10% of the course grade.

Handing in this Assignment

What to hand in on paper: Nothing.

What to hand in electronically: You must submit your assignment electronically. Download csp.zip which contains propagators.py and futoshiki_csp.py and other related files from the A2 web page. Modify propagators.py and futoshiki_csp.py so that they solve the problems specified in this document. Submit your modified files propagators.py and futoshiki_csp.py You will submit your assignment using MarkUs. It is your responsibility to include all necessary files in your submission. You can submit a new version of any file at any time, though your grace tokens will be used if you submit after the deadline.

We will test your code electronically. You will be supplied with a testing script that contains a test or a very simple CSP. You can add your own tests to this script. It's up to you to figure out further test cases to further test your code – that's part of the assignment! You will also have access to a *subset* of hidden tests on MarkUs to test your code before the deadline.

When your code is submitted, we will run a more extensive set of tests. You have to pass all of these more elaborate tests to obtain full marks on the assignment.

Your code will not be evaluated for partial correctness, it either works or it doesn't. It is your responsibility to hand in something that passes at least some of the hidden tests on MarkUs.

- Make certain that your code runs on teach.cs using python3 (version 3.12) using only standard imports. This version is installed as "python3" on teach.cs. Your code will be tested using this version and you will receive zero marks if it does not run using this version.
- Do not add any non-standard imports from within the python file you submit (the imports that are already in the template files must remain). Once again, non-standard imports will cause your code to fail the testing and you will receive zero marks.
- *Do not change the supplied starter code*. Your code will be tested using the original starter code, and if it relies on changes you made to the starter code, you will receive zero marks.

Clarifications: Important corrections (hopefully few or none) and clarifications to the assignment will be announced on Quercus.

You are responsible for monitoring Quercus announcements for any clarifications or corrections.

Help Sessions: There will be several help sessions for this assignment. Dates and times for these sessions will be posted on Quercus.

Questions: Questions about the assignment should be posed on Piazza.

Introduction

There are two parts to this assignment:

- 1. the implementation of two constraint propagators and a variable ordering heuristic a Forward Checking constraint propagator, a Generalized Arc Consistence (GAC) constraint propagator, and the Minimum Remaining Values (MRV) heuristic,
- 2. the encoding of two different CSP models to solve the logic puzzle, Futoshiki, as described below. In one model you will use only binary not-equal constraints, while in the other model you will use 9-ary all-different constraints in addition to binary not-equal constraints.

What is supplied:

- cspbase.py class definitions for the python objects Constraint, Variable, and BT.
- **propagators.py** starter code for the implementation of your two propagators and variable ordering heuristic. You will modify this file with the addition of three new procedures prop_FC, prop_GAC, and ord_mrv, to realize Forward Checking, GAC and MRV, respectively.
- csp_sample_run.py This file contains a sample implementation of two CSP problems.
- **futoshiki_csp.py** starter code for the two Futoshiki CSP models.
- autograder.py for testing your code.

Futoshiki Formal Description

The Futoshiki puzzle¹ has the following formal description:

- The puzzle is played on a grid *board* with dimensions n rows by n columns. The board is always a square.
- The board has n^2 spaces on it, where each space may take a value between 1 and n inclusive. You will use a list of lists in order to represent assigned values to the variables on this grid.
- The start state of the puzzle may have some spaces already filled in.
- Additionally, the starting board may have some *inequality constraints* specified between some of the spaces. These inequality constraints will *only* apply to two cells that are horizontally adjacent to one another, i.e. the constraints will only apply to rows and not columns. If there is *no* inequality constraint between two adjacent cells, this will be represented with a dot (i.e., with a '.'). For example, consider this 2 x 2 board: [[0,<,0,],[0,.,0]]. The assignments [[1,<,2,],[2,.,1]] would satisfy the inequality constraint.
- A puzzle is solved if:
 - Every space on the board is given one value between 1 and n inclusive.
 - All specified inequality constraints are satisfied.
 - No row contains more than one of the same number.

¹https://en.wikipedia.org/wiki/Futoshiki

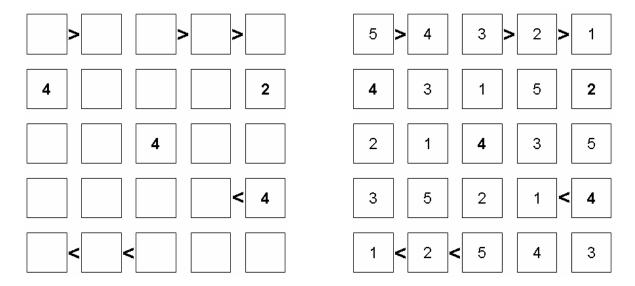


Figure 1: An example of a 5×5 Futoshiki grid in its initial state (left) and solution (right).

- No column contains more than one of the same number.

An example of a Futoshiki instance and its solution are depicted in figure 1. You can also play Futoshiki online² but column inequality constraints might be included.

Question 1: Propagators (worth 60/100 marks)

You will implement python functions to realize two constraint propagators — a Forward Checking constraint propagator and a Generalized Arc Consistence (GAC) constraint propagator. These propagators are briefly described below. The files cspbase.py and propagators.py provide the complete input/output specification of the functions you are to implement. In all cases, the CSP object is used to access variables and constraints of the problem, via methods found in cspbase.py.

Brief implementation description: A Propagator Function takes as input a CSP object csp and (optionally) a variable newVar. The CSP object is used to access the variables and constraints of the problem (via methods found in cspbase.py). A propagator function returns a tuple of (bool,list) where bool is False if and only if a dead-end is found, and list is a list of (Variable, value) tuples that have been pruned by the propagator. ord_mrv takes a CSP object csp as input, and returns a Variable object var.

You must implement:.

prop_FC (worth 25/100 marks)

A propagator function that propagates according to the Forward Checking (FC) algorithm that check constraints that have *exactly one uninstantiated variable in their scope*, and prune appropriately.

If newVar is None, forward check all constraints. Else, if newVar=var only check constraints containing newVar.

prop_GAC (worth 25/100 marks)

A propagator function that propagates according to the Generalized Arc Consistency (GAC) algo-

²https://www.futoshiki.org/

rithm, as covered in lecture. If newVar is None, run GAC on all constraints. Else, if newVar=var only check constraints containing newVar.

ord_mrv (worth 10/100 marks)

A variable ordering heuristic that chooses the next variable to be assigned according to the Minimum Remaining Values (MRV) heuristic. ord mrv returns the variable with the most constrained current domain (i.e., the variable with the fewest legal values).

Question 2: Futoshiki Models (worth 40/100 marks)

You will implement two different CSP encodings to solve the logic puzzle, Futoshiki. In one model you will use only binary not-equal constraints, while in the other model you will use n-ary all-different constraints in addition to binary not-equal constraints. These CSP models are briefly described below. The file futoshiki_csp.py provides the complete input/output specification for the two CSP encodings you are to implement.

The correct implementation of each encoding is worth 20/100 marks.

Brief implementation description: A Futoshiki Model takes as input a Futoshiki board, and returns a CSP object, consisting of a variable corresponding to each cell of the board. The variable domain of that cell is $\{1,...,n\}$ if the board is unfilled at that position, and equal to i if the board has a fixed number i at that cell. All appropriate constraints will be added to the board as well. You must implement:

futoshiki_csp_model_1 A model built using only binary not equal constraints for the row and column constraints, and binary inequality constraints.

futoshiki_csp_model_2 A model built using *n*-ary all-different constraints for the row and column constraints, and binary inequality constraints.

Caveat: The Futoshiki CSP models you will construct can be space expensive, especially for constraints over many variables, (e.g., those contained in the second Futoshiki CSP model). *HINT: Also be mindful of the time complexity of your methods for identifying satisfying tuples, especially when coding the second Futoshiki CSP model*.

HAVE FUN and GOOD LUCK!