Stochastic Integer Programming Library version 2.0

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 ${\bf Abstract}\;$ We present a collection of stochastic integer programming problem instances.

Keywords Stochastic Integer Programming · Problem Instances

1 Introduction

The SIPLIB [1] is an abbreviated term of the Stochastic Integer Programming (SIP) Library firstly contructed in 2002 by Shabbir Ahmed and his colleagues. The library has been providing a collection of test instances to facilitate computational and algorithmic research in SIP. Some new test problems with instances have been added to SIPLIB gradually and now it contains nine different problems in total. The instances are basically given in the standard SMPS format accompanied with additional information including parameter data, size of the instance in terms of the number of rows, columns, and integers, benchmarking information such as best known objective value or bounds, optimality gap, and solution time.

At the time SIPLIB appeared, it provided enoughly large-sized instances that is reasonable to argue that the performance of algorithm is remarkable if it solves the instances. State-of-the-art in SIP combined with the speedup in computing machinery, however, makes many instances in SIPLIB so easy that we have not enough basis to use them for showing the excellence of

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newly suggested solution methods. At this point, we are motivated to develop the second version of SIPLIB, say SIPLIB 2.0 that provides larger-sized test instances with higher degree of tailorability, e.g., users can easily generate instances of test problems as largely as they want.

(as we include DCLP (data center location problem), this paragraph must be modified) Stochastic programming (SP) is a framework for modeling optimization problems that involve uncertainty. Whereas optimization problems are typically formulated with known parameters, the problems in real world contain some unknown parameters in many cases. For details on SP, see, e.g., [2,3]. SIP is a branch of SP that indicates any type of SP including at least one integer decision variable. The integers can be placed anywhere in general SIP. However, we restrict our focus on two-stage SIP that contains integer variables (including binary) in its second stage throughout this paper and SIPLIB 2.0. The main reason is that the class of SIP is most widely used to model real world problems. Moreover, two-stage SIP itself has enough difficulties that have not been conquered yet even without any other details like chance-constraints and multi-stages. The main difficulty in solving two-stage SIP is that the secondstage value function is not necessarily convex, but only lower semicontinuous. Thus, the standard decomposition approaches that work nicely for stochastic linear programs, break down when the second stage integer variables are present [4]. Hereinafter, we use the term SIP to indicate the two-stage SIP that contains integer variables in its second stage.

We provide the test sets in two formats: SMPS files (*.cor, *.tim, *.stoch) and Julia files (*.jl). SMPS is widely used to describe stochastic linear and quadratic programs. Once having SMPS files of a problem instance, we can directly solve it using various mixed integer linear program (MILP) solvers such as CPLEX, GUROBI, and CBC. One can also use the existing open-source SIP solvers like DSP [5], PySP [6], and SMI [7] given that SMPS files. A drawback of SMPS format is its low readability by human, which we decided to provide Julia files to let users be able to easily read problems and tailor the instances.

Julia is an open source high-level, high-performance dynamic programming language for numerical computing. It is also known as its good performance, approaching that of statically-compiled languages like C [8]. The syntax of Julia is simple and should feel familiar to anyone who has experienced in another high-level languages like MATLAB or Python. A Julia package called Jump (Julia for Mathematical Programming [9]) provides a domain-specific modeling language for mathematical optimization embedded in Julia. JuMP enables us to easily translate mathematical model to JuMP.Model-type object. Some structured mathematical models like SIP can also be translated to the Jump. Model-type object combined with the package StructJump [10]. Once we have a Julia code for constructing JuMP. Model-type object, it is easy to generate instances whenever we need to modify the original mathematical model. For each problem in SIPLIB 2.0, we provide a Julia script for constructing Jump. Model-type object. We also provide a Julia script (SmpsWriter.jl) for converting any JuMP.Model-type objects to SMPS files for users' convenience. Those who feel the given instances are not large enough can simply generate

more scenario data by just modifying the parameter in Julia script corresponding to the number of scenarios.

By SIPLIB 2.0, we provide 1) richer collection of test instances for computational and algorithmic research in SIP with benchmarking computational results, 2) not only SMPS files but also Julia files that are easily readable/tailorable. Hence, the users can obtain as large-sized instances as they need by generating new scenarios and including them into instances. For those who want to utilize the instances in the legacy SIPLIB with strong tailorability provided by SIPLIB 2.0, we include the original SIPLIB instances as well.

(Contents of the paper, not finished yet) In this paper, we provide a detailed description of the test problems in SIPLIB 2.0, including information on the instances, their origin, formal mathematical models with explanation on notations, and scenario data generation procedure. SIPLIB 2.0 classifies problems based on the stages, variables, and constraints. We borrow some classification criteria from the most frequently utilized mixed integer programming (MIP) library, MIPLIB 2010 [21], whenever they are applicable to SIP as well.

2 Stochastic integer programming

In this section, we explain general description of SIP. This includes formal mathematical formulation, existing general solution methods to solve the SIPs, and currently available software libraries.

2.1 Formulation

In this subsection, we introduce the form of SIP of interest. The notations and dimensional information are summarized in Table 1. We are interested in finding solution for two-stage SIP of the form:

$$z := \min_{x \in X} \left\{ c^{\top} x + \mathcal{Q}(x) : Ax \ge b \right\}, \tag{1}$$

where $Q(x) := \mathbb{E}_{\boldsymbol{\xi}} \left[\phi \left(h(\boldsymbol{\xi}) - T(\boldsymbol{\xi}) x \right) \right]$ is the recourse function associated with the random variable (r.v.) $\boldsymbol{\xi}$. We assume that $\boldsymbol{\xi}$ follows a known discrete probability distribution with the finite realizations, called *scenarios*, ξ_1, \dots, ξ_r and respective nonnegative probabilities $\mathbb{P}(1), \dots, \mathbb{P}(r)$, i.e., $\mathbb{P}(s) \equiv \mathbb{P}[\boldsymbol{\xi} = \xi_s]$ for $s \in \mathcal{S} := \{1, \dots, r\}$. When the distribution is continuous, we can approximate it by a suitably discretized distribution. The real-valued map $\phi_{\xi_s} : \mathbb{R}^{m_2} \to \mathbb{R}$ is the optimal value of the second-stage problem defined by

$$\phi_{\xi_s}(t) := \min_{y_s \in Y} \left\{ q(\xi_s)^\top y_s : \ W(\xi_s) y_s \ge t \right\}, \ t \in \mathbb{R}^{m_2}, \tag{2}$$

where ξ_s is an arbitrarily realized scenario. The sets $X \subseteq \mathbb{R}^{n_1}$ and $Y \subseteq \mathbb{R}^{n_2}$ represent integer or binary restrictions on a subset of the decision variables x and y_s , respectively. The first-stage problem data comprise A, b, and c. The second-stage data are given by $T(\xi_s)$, $W(\xi_s)$, $h(\xi_s)$, and $q(\xi_s)$ (for dimensional

information refer to Table 1). Hereinafter, we use the simplified notations (T_s, W_s, h_s, q_s) . The SIP (1) can be rewritten in the extensive form

$$z = \min_{x, y_s} c^{\top} x + \sum_{s=1}^{r} \mathbb{P}(s)(q_j^{\top} y_s),$$
 (3a)

s.t.
$$Ax \ge b$$
, (3b)

$$T_s x + W_s y_s \ge h_s, \quad \forall s \in \{1, \dots, r\},$$
 (3c)

$$x \in X,\tag{3d}$$

$$y_s \in Y, \quad \forall s \in \{1, \dots, r\}.$$
 (3e)

Table 1 Summary of notations in SIP formulation

Sets: $X \subseteq \mathbb{R}^{n_1}$ $Y \subseteq \mathbb{R}^{n_2}$ $S = \{1, \dots, r\}$	first-stage polyhedral set (continuous, integer, binary) second-stage polyhedral set (continuous, integer, binary) index set of realizable scenarios
Scalas: $\boldsymbol{\xi}$ $z \in \mathbb{R}$ $r \in \mathbb{N}$ $s \in \mathcal{S}$ $\mathbb{P}(s) \in [0, 1]$	r.v. denoting scenario that realizes by one of the set $\{\xi_1, \dots, \xi_r\}$ optimal objective value of the SIP number of scenarios index denoting scenario probability that scenario s happens, i.e., $\mathbb{P}(s) \equiv \mathbb{P}[\boldsymbol{\xi} = \xi_s]$
Vectors: $x \in \mathbb{R}^{n_1}$ $c \in \mathbb{R}^{n_1}$ $b \in \mathbb{R}^{m_1}$ $y_s \in \mathbb{R}^{n_2}$ $q_s \equiv q(\xi_s) \in \mathbb{R}^{n_2}$ $h_s \equiv h(\xi_s) \in \mathbb{R}^{m_2}$	first-stage decision vector first-stage cost vector first-stage RHS vector second-stage decision vector under scenario ξ_s second-stage cost vector second-stage RHS vector
$\begin{aligned} & \textbf{Matrices:} \\ & A \in \mathbb{R}^{m_1 \times n_1} \\ & W_s \equiv W(\xi_s) \in \mathbb{R}^{m_2 \times n_2} \\ & T_s \equiv T(\xi_s) \in \mathbb{R}^{m_2 \times n_1} \end{aligned}$	first-stage constraint matrix corresponds to decision vector x second-stage constraint matrix corresponds to decision vector y_s second-stage constraint matrix corresponds to decision vector x
Functions: $\phi_{\xi_s}: \mathbb{R}^{m_2} \to \mathbb{R}$ $\mathcal{Q}: \mathbb{R}^{n_1} \to \mathbb{R}$	second stage program optimal value under the realization of scenario ξ_s recourse function (the expectation of $\phi\left(h(\boldsymbol{\xi})-T(\boldsymbol{\xi})x\right)$ over the r.v. $\boldsymbol{\xi}$)

2.2 Solution methods

$\it 2.2.1 \ Stage-wise \ decomposition \ algorithm$

$\it 2.2.2 \ Scenario-wise \ decomposition \ algorithm$

2.3 Software libraries

2.3.1 Modeling languages

2.3.2 Solvers

3 Summary of the test sets

3.1 Type of problems

 ${\bf Table~2}~{\bf Types~of~the~problems~in~SIPLIB~2.0}$

Problem name	Description	Main reference
DCAP	Dynamic capacity planning with stochastic demand	Ahmed and Garcia [4]
DCLP	Data center location problem	Kim et al. [19]
MPTSPs	Multi-path traveling salesman problem with stochastic travel costs	Tadei et al. [13]
SIZES	Optimal product substitution with stochastic demand	Jorjani et al. [15]
SMKP	Stochastic multiple knapsack problem	Angulo et al. [17]
SSLP	Stochastic server location problem	Ntaimo and Sen [20]
SUCW	Wind power stochastic unit commitment	Papavasiliou and Oren [18]

Table 3 Components of the problems in SIPLIB 2.0

	1st stage		2nd stage	
Problem	Variable	Constraint	Variable	Constraint
DCAP	\mathbb{C},\mathbb{B}	VBB ¹	\mathbb{B}	$\mathtt{PAR}^1,\mathtt{MO1}^1$
DCLP			\mathbb{C}	
MPTSPs	\mathbb{C}, \mathbb{B}	\mathtt{PAR}^2 , \mathtt{GEN}^1	\mathbb{B}	\mathtt{GEN}^2
SIZES	I	\mathtt{VBD}^1 , \mathtt{GEN}^2	\mathbb{B} , \mathbb{I}	${\tt IKN^1}$
SMKP	\mathbb{B}	\mathtt{KNA}^1	\mathbb{B}	\mathtt{KNA}^1
SSLP	\mathbb{B}	${\tt IVK}^1$, ${\tt GEN}^1$	\mathbb{C} , \mathbb{I}	GEN^2
SUCW	Ø		\mathbb{C}, \mathbb{B}	

3.2 Instance catalog

3.2.1 Instance naming rule

Table 4 Problem-specific instance naming rules

Problem	Instance name	Description
DCAP DCLP MPTSPs SIZES SMKP SSLP SUCW	MPTSPs_Dx_Ny_Sz SIZESz	node distribution strategy $\mathtt{D} \mathtt{x},$ number of nodes y, and number of scenarios z number of scenario is z

4 How to run a test, generate new instance, and convert to SMPS

We explain the structure of SIPLIB 2.0. We explain procedure to generate new instances with user-generated scenario data using Julia scripts. The problem-specific descriptions are given in Section 6. We explain how to convert Jump. Model-type object to SMPS files.

5 Implementation of SMPS Writer

We describe our Julia implementation, how to model SIP and generate SMPS files..

6 Problem descriptions

In this section, we introduce details for each problem in SIPLIB 2.0. We also explain the scenario data generation procedures. Due to limited access to the original data in reference papers, we selectively choose the methods from several available references and modify some of them without harming validity. Also, we guess some parameters about scenario generation to make the procedure clear.

6.1 DCAP: Dynamic capacity planning with stochastic demand

DCAP is the problem of determining a capacity expansion schedule for a set of resources, and the assignment of resource capacity to task with stochastic requirement over a multi-period planning horizon. In SIPLIB, 12 instances are available in SMPS format with the largest instance comprises of 500 scenarios correspond to the size of 9,012 rows and 18,018 columns. We refer to [4] for writing Julia scripts.

6.1.1 Mathematical formulation

We consider the problem of deciding the capacity expansion schedule for |R| resources over |T| time periods to satisfy the processing requirements of |N| tasks where R, T, and N denote set of resources, set of time periods, and set of tasks, respectively. We define decision variables: the first-stage continuous variable x_{it} for the capacity acquisition of resource i in period t and the second-stage binary variable y_{ijt}^s to indicate whether resource i is assigned to task j in period t under scenario s. Additional first-stage binary variable u_{it} is for logical constraint whether or not we decided to acquire more capacity of resource i in period t. Hence, for all resource $i \in M$ and time $t \in T$, $u_{it} = 1$ if $x_{it} > 0$, $u_{it} = 0$ otherwise.

Under the definition of the decision variables, the extensive form of DCAP is written below and the summarized notation is available in Table 5.

$$(\mathtt{DCAP}) \min \sum_{t \in T} \sum_{i \in R} (\alpha_{it} x_{it} + \beta_{it} u_{it}) + \sum_{s \in \mathcal{S}} \mathbb{P}(s) \sum_{t \in T} \sum_{i \in M \cup \{0\}} \sum_{j \in N} c^s_{ijt} y^s_{ij} \quad (4a)$$

s.t.
$$x_{it} \le Mu_{it}$$
, $\forall i \in R, \ \forall t \in T$, (4b)

$$\sum_{j \in N} d_{jt}^s y_{ijt}^s \le \sum_{\tau=1}^t x_{i\tau}, \quad \forall i \in R, \ \forall t \in T, \ \forall s \in \mathcal{S},$$
 (4c)

$$\sum_{i \in R \cup \{0\}} y_{ijt}^s = 1, \quad \forall j \in N, \ \forall t \in T, \ \forall s \in \mathcal{S},$$

$$\tag{4d}$$

$$x_{it} \ge 0, \quad \forall i \in R \cup \{0\}, \ \forall t \in T,$$
 (4e)

$$u_{it} \in \{0, 1\}, \quad \forall i \in R \cup \{0\}, \ \forall t \in T,$$
 (4f)

$$y_{ijt}^s \in \{0, 1\}, \quad \forall i \in R \cup \{0\}, \ \forall j \in N, \ \forall t \in T, \ \forall s \in \mathcal{S},$$
 (4g)

The objective function (4a) is to minimize total expected cost for the capacity expansion schedule. The first double summation denotes the expansion cost for resource i in period t where α_{it} and β_{it} are the variable and fixed cost, respectively. The second term in the objective function represents the expected assignment cost in period t over all scenario $s \in \mathcal{S}$. Note that a dummy resource i=0 is included with infinite capacity. The cost c_{0jt}^s denotes the penalty of failing to assign a resource to task j. The dummy resource enforces the complete recourse property, which ensures that there is a feasible second-stage assignment in all periods and all scenarios for any capacity acquisition schedule [4]. Constraint (4b) is the logical constraint containing a suitably large value M to define the cost for capacity expansion. Constraint (4c) reflects that the processing requirement of all tasks assigned to a resource in any period cannot exceed the installed capacity in that period under all scenarios. Constraint (4d) guarantees that each task needs to be assigned to exactly one resource in each period under all scenarios. Finally, constraints (4e)-(4g) restrict the space from which the variables take values.

Table 5 Notations for DCAP

Index sets: R N T S	index set of resources $(i \in R \cup \{0\}$ where 0 is a dummy resource with infinite capacity) index set of tasks $(j \in N)$ index set of time periods $(t \in T)$ index set of scenarios $(s \in \mathcal{S})$		
Parameters:			
$lpha_{it}$	variable cost for expanding capacity of resource i		
eta_{it}	fixed cost for expanding capacity of resource i		
c_{iit}^s	cost of processing task j using resource i in period t under scenario s		
d_{it}^{s}	processing requirement for task j in period t under scenario s		
$c_{ijt}^s \\ d_{jt}^s \\ \mathbb{P}(s)$	the probability of occurence of scenario s		
Decision varial	Decision variables:		
x_{it} (1 st stage)	capacity acquisition amount of resource i in period t		
u_{it} (1 st stage)	1 if capacity of resource i is expanded in period t , 0 otherwise		
y_{ijt}^s (2 nd stage)	1 if resource i is assigned to task j in period t under scenario s , 0 otherwise		

6.1.2 Scenario data generation

There are four factors that define the instance of DCAP: |R|, |N|, |T|, and |S|. Once we decide the factors by, $n_R = |R|$, $n_N = |N|$, $n_T = |T|$, and $n_S = |S|$, each instance is named by DCAP $_n n_N n_T n_S$. Since no original parameter is available, we randomly generate the parameters as long as they are valid. Let U be a continuous uniform random variable: $U \sim Unif(0,1)$. Then, the parameters are generated as follows:

$$\begin{aligned} &\alpha_{it} = 5U + 5, \quad \forall i \in R, \ \forall t \in T, \\ &\beta_{it} = 40U + 10, \quad \forall i \in R, \ \forall t \in T, \\ &c^s_{ijt} = 5U + 5, \quad \forall i \in R, \ \forall j \in N, \ \forall t \in T, \ \forall s \in \mathcal{S}, \\ &c^s_{0jt} = 500U + 500, \quad \forall j \in N, \ \forall t \in T, \ \forall s \in \mathcal{S}, \\ &d^s_{it} = U + 0.5, \quad \forall j \in N, \ \forall t \in T, \ \forall s \in \mathcal{S}. \end{aligned}$$

For the first-stage parameters α_{it} and β_{it} , we fix the random seed to make it deterministic.

6.2 DCLP: Data center location problem

6.2.1 Mathematical formulation

 $6.2.2\ Scenario\ data\ generation$

6.3 SMKP: Stochastic multiple knapsack problem

SMKP is a class of stochastic multiple binary knapsack problems. Unlike typical knapsack problems where the objective is to maximize total profits under the restriction of the weight capacity of each knapsack, SMKP is to minimize total weights while satisfying a certain required profit for each knapsack.

SIPLIB provides 30 instances of SMKP in total. The first-stage problems contain 240 binary variables and 50 knapsack constraints. The second-stage problems have 120 binary variables and 5 knapsack constraints. Each instance has 20 scenarios. We refer [17] for writing Julia script for SIPLIB 2.0 and explain the model throughout the following subsections.

6.3.1 Mathematical formulation

We have three types of items x, z, and y where the first two types are of the first-stage and the last one is of the second-stage with stochastic scenarios. For each type, we have |I| number of items where I is the index set of the items. Hence, we define the binary variables x_i, z_i , and y_i^s which are equal to 1 if the i^{th} item is decided to be included (s denotes scenario so only appears in y-type variables). We consider two types of knapsacks: one associated with x-type and z-type items (say xz-knapsack) and the other one with x-type and y-type items (say xy-knapsack). xz-knapsacks are indexed by $j \in J$ and xy-knapsacks are indexed by $k \in K$. Each knapsack has its own minimum level of profit that should be satisfied by the items of the associated types, e.g., the profit of the j^{th} xz-type knapsack is calculated based on the inclusion or exclusion of x-type and z-type items and should satisfy a certain requirement b_j . Bear in mind that the inclusion or exclusion of a certain item i affects all the associated knapsacks.

Each parameter c_i , d_i , and q_i^s denotes the gain of weight when including items of type x, z, and y, respectively. Here, c_i and d_i are deterministic and q_i^s is stochastic. Parameters a_{ji} , e_{ji} , t_{ki} , and w_{ki} are all deterministic and denote the profits for including items in the knapsacks. The RHS parameters b_j and h_k are the minimum levels of profit requirements for xz-knapsacks and xy-knapsacks, respectively.

The extensive form of ${\tt SMKP}$ is as follows and the notations used are summrized in Table 6.

$$(\texttt{SMKP}) \min \sum_{i \in I} (c_i x_i + d_i z_i) + \sum_{s \in \mathcal{S}} \mathbb{P}(s) \sum_{i \in I} q_i^s y_i^s$$
 (5a)

s.t.
$$\sum_{i \in I} a_{ji} x_i + \sum_{i \in I} e_{ji} z_i \ge b_j, \quad \forall j \in J,$$
 (5b)

$$\sum_{i \in I} t_{ki} x_i + \sum_{i \in I} w_{ki} y_i^s \ge h_k, \quad \forall k \in K, \ \forall s \in \mathcal{S},$$
 (5c)

$$x_i \in \{0, 1\}, \quad \forall i \in I, \tag{5d}$$

$$z_i \in \{0, 1\}, \quad \forall i \in I,$$
 (5e)

$$y_i^s \in \{0, 1\}, \quad \forall i \in I, \ \forall s \in \mathcal{S}.$$
 (5f)

The objective (5a) is to minimize the expected value of the total weights. Constraint (5b) ensures the minimum levels of profit requirements for all xz-knapsacks are satisfied. Constraint (5c) guarantees the minimum levels of

profit requirements are satisfied for all xy-knapsacks under every scenario. Constraints (5d)-(5f) are binary restriction of the decision variables.

Table 6 Notations for SMKP

```
Index sets:
                     index set of items for each type (i \in I)
J
                      index set of xz-knapsacks (j \in J)
                     index set of xy-knapsacks (k \in K)
K
\mathcal{S}
                     index set of scenarios (s \in \mathcal{S})
Parameters:
                      weight of the i^{\rm th} x-type item
                     weight of the i^{\rm th} z-type item
d_i
                     weight of the i^{\mathrm{th}} y-type item under scenario s
q_i^s
                     profit of the j^{\text{th}} xz-knapsack for including i^{\text{th}} x-type item
                     profit of the j^{\text{th}} xz-knapsack for including i^{\text{th}} z-type item
                     profit of the k^{\text{th}} xy-knapsack for including i^{\text{th}} x-type item
                     profit of the k^{\text{th}} xy-knapsack for including i^{\text{th}} y-type item
w_{ki}
                     minimum required profit for the j^{\text{th}} xz-knapsack
                     minimum required profit for the k^{\text{th}} xy-knapsack
h_{\iota}
\mathbb{P}(s)
                     the probability of occurence of scenario s
Decision variables:
x_i (1st stage)
                     1 if the i^{\text{th}} x-type item is decided to be included, 0 otherwise
z_i (1st stage)
                     1 if the i^{\mathrm{th}} z-type item is decided to be included, 0 otherwise
y_i^s (2<sup>nd</sup> stage)
                     1 if the i^{\mathrm{th}} y-type item is decided to be included under scenario s,\,0 otherwise
```

6.3.2 Scenario data generation

There are two factors that define the instance of SMKP: |I| and |S|. The sizes for another sets are fixed by |J| = 50 and |K| = 5 following [17]. Once we decide the factors by $n_I = |I|$, $n_S = |S|$, $n_T = |T|$, and $n_S = |S|$, each instance is named by SMKP_ n_I _ n_S . Again directly following [17], we randomly generate the parameters. Let U be a discrete uniform random variable: $U \sim Unif[1, 100]$. Then, the parameters are generated as follows:

$$\begin{aligned} c_i &= U, & \forall i \in I, \\ d_i &= U, & \forall i \in I, \\ q_i^s &= U, & \forall i \in I, \forall s \in \mathcal{S}, \\ a_{ji} &= U, & \forall j \in J, \forall i \in I, \\ e_{ji} &= U, & \forall j \in J, \forall i \in I, \\ t_{ki} &= U, & \forall k \in K, \forall i \in I, \\ w_{ki} &= U, & \forall k \in K, \forall i \in I, \\ b_j &= \frac{3}{4} \sum_{i \in I} \left(a_{ji} + e_{ji} \right), & \forall j \in J, \\ h_k &= \frac{3}{4} \sum_{i \in I} \left(t_{ji} + w_{ji} \right), & \forall k \in K. \end{aligned}$$

For the first-stage parameters, we fix the random seed to make it deterministic.

6.4 SSLP: Stochastic server location problem

SSLP is a class of problem that finds the optimal location of servers and the optimal allocation of clients to servers which maximizes the expected net income under uncertain presents of clients. SSLP finds applications in a variety of domains such as network design for electric power, internet services, telecommunications, and water distribution. SIPLIB provides 12 instances with varying number of clients, server locations, and scenarios in SMPS format. The largest instance includes 10 server locations, 50 clients, and 2,000 scenarios which corresponds to 120,001 constraints, 1,000,010 binary variables, and 20,000 continuous variables.

We refer to [20] for mathematical formulation and data generation forthcoming through the following subsections.

6.4.1 Mathematical formulation

(SSLP) min
$$\sum_{j \in J} c_j x_j - \sum_{s \in \mathcal{S}} \mathbb{P}(s) \left(\sum_{i \in I} \sum_{j \in J} q_{ij}^s y_{ij}^s - \sum_{j \in J} q_{0j}^s y_{0j}^s \right)$$
(6a)

s.t.
$$\sum_{j \in J} x_j \le v, \tag{6b}$$

$$\sum_{j \in J} x_j \ge w_z, \quad \forall z \in Z, \tag{6c}$$

$$\sum_{i \in I} d_{ij} y_{ij}^s - y_{0j}^s \le u x_j, \quad \forall j \in J, \ \frac{\forall i \in I,}{\forall i \in I}, \ \forall s \in \mathcal{S},$$
 (6d)

$$\sum_{i \in J} y_{ij}^s = h_i^s, \quad \forall i \in I, \ \forall s \in \mathcal{S},$$
 (6e)

$$x_j \in \{0, 1\}, \quad \forall j \in J, \tag{6f}$$

$$y_{ij}^s \in \{0, 1\}, \quad \forall i \in I, \ j \in J, \ s \in \mathcal{S},$$
 (6g)

$$y_{0j}^s \ge 0, \quad \forall j \in J, \ \forall s \in \mathcal{S}.$$
 (6h)

Table 7 Notations for SSLP

Index sets:		
I	index set of clients $(i \in I)$	
J	index set of servers $(j \in J)$	
Z	index set of zones $(z \in Z)$	
$\mathcal S$	index set of scenarios $(s \in \mathcal{S})$	
Parameters:		
c_j	cost of locating a server at location j	
	revenue from client i being served by server at location j under scenario s	
q_{ij}^s q_{0j}^s	rate of revenue loss for overflows that are not served due to limited server capacity under scenario s	
d_{ij}	resource demand of client i from server at location j	
u	server capacity	
v	upper bound on the total number of servers that can be located	
w_z	minimum number of servers to be located in zone z	
J_z	subset of server locations that belong to zone z	
h_i^s	1 if client i is present under scenario s , 0 otherwise	
$\mathbb{P}(s)$	probability of occurence for scenario s	
Decision variables:		
x_i (1 st stage)	1 if a server is located at site j , 0 otherwise	
y_{ij}^{s} (2 nd stage)	1 if client i is served by a server at location j under scenario s , 0 otherwise	
y_{ij}^s (2 nd stage) y_{0j}^s (2 nd stage)	non-negative amount of overflows that are not served due to limitations in server j 's capacity	

6.4.2 Scenario data generation

6.5 MPTSPs: Mutli-path Traveling Salesman Problem with Stochastic Travel Times

MPTSPs is a variant of the travelling salesman problem (TSP) where a set of paths exists between any two nodes and each path is chracterized by a random travel time.

In SIPLIB, only limited data (e.g., number of nodes, coordinates of nodes, generated travel times) are provided and no SMPS file is available. We mainly refer to [12] for deriving the mathematical formulation. Due to the malfunction of subtour breaking constraints in the reference model, we refer to another paper [14] to break subtours. Combining the two references, we construct the forthcoming single commodity flow-based formulation MPTSPs that is used for SIPLIB 2.0.

6.5.1 Mathematical formulation

We consider a two-stage SIP with recourse. The travel time oscillation e^k_{ij} by using path k between nodes i and j. We present each realization (scenario) of random travel time oscillation by e^s_{ijk} where s indicates the scenario. In MPTSPs, at the first stage, the decision-maker does not have any information about the travel time oscillation. The tour paths among the nodes, however, should be determined before the complete information is available. The first stage decision variable y_{ij} is represented by the selection of nodes i and j to be visited in a tour. In the second stage where the random travel time c^s_{ijk} are avilable, the paths k between each couple of nodes i and j under scenario s, x^s_{ijk} can be calculated.

Let N and K_{ij} , respectively, bethe finite set of nodes of the graph and the set of paths between the pair of nodes $i, j \in N$. We denote with S the set of

scenarios with associated equally distributed probability of each scenario $\mathbb{P}(s)$, i.e., $\mathbb{P}(s) \equiv 1/|\mathcal{S}|$. Each path $k \in K_{ij}$ between nodes $i, j \in N$ is chracterized by a non-negative estimation of the mean unit travel time \bar{c}_{ij} and a non-negative unit random travel time c_{ijk}^s under the scenario $s \in S$. Let $e_{ijk}^s \equiv c_{ijk}^s - \bar{c}_{ij}$ be the error on the travel time estimated for the path $k \in K_{ij}$ under time scenario $s \in S$.

The first stage binary variables $y_{ij}=1$ if node $j\in N$ is visited right after node $i\in N$, 0 otherwise. The second stage binary variables $x_{ijk}^s=1$ if path $k\in K_{ij}$ between nodes $i,j\in N$ is selected at the second stage, 0 otherwise. We have one more set of first stage variables ϕ_{ij} which is introduced to break the subtours [14]. The non-negative continuous variables ϕ_{ij} describe the flow of a single commodity to node 1 from every other nodes (without loss of generality, 1 is the starting node).

The extensive form of MPTSPs is as follows and the notations used are summrized in Table 8.

(MPTSPs) min
$$\sum_{i \in N} \sum_{j \in N} \bar{c}_{ij} y_{ij} + \sum_{s \in \mathcal{S}} \mathbb{P}(s) \sum_{i \in N} \sum_{j \in N} \sum_{k \in K_{ij}} e^s_{ijk} x^s_{ijk}$$
 (7a)

s.t.
$$\sum_{j \in N: j \neq i} y_{ij} = 1, \quad \forall i \in N,$$
 (7b)

$$\sum_{i \in N: i \neq j} y_{ij} = 1, \quad \forall j \in N, \tag{7c}$$

$$\sum_{j \in N} \phi_{lj} - \sum_{i \in N \setminus \{1\}} \phi_{il} = 1, \quad \forall l \in N \setminus \{1\},$$
 (7d)

$$\phi_{ij} \le (|N| - 1) y_{ij}, \quad \forall i \in N \setminus \{1\}, \ \forall j \in N,$$
 (7e)

$$\sum_{k \in K_{ij}} x_{ijk}^s = y_{ij}, \quad \forall i \in N, \ \forall j \in N, \ \forall s \in \mathcal{S},$$
 (7f)

$$x_{ijk}^s \in \{0, 1\}, \quad \forall i \in N, \ \forall j \in N, \ \forall k \in K_{ij}, \ \forall s \in \mathcal{S},$$
 (7g)

$$y_{ij} \in \{0, 1\}, \quad \forall i \in N, \ \forall j \in N,$$
 (7h)

$$\phi_{ij} \ge 0, \quad \forall i \in N, \ \forall j \in N.$$
 (7i)

The first sum in the objective function (7a) represents the first stage travel cost, while the second sum represents the recourse action, consisting in choosing the best path $k \in K_{ij}$ under scenario $s \in \mathcal{S}$. The constraints (7b) and (7c) form the assignment constraints and ensure that each node is visited only once. Given the fixed values of y_{ij} , constraint (7d) and (7e) form a network flow problem, and therefore the ϕ_{ij} values will be integer. In case the solutions of the above formulation contain at least one subtour, the constraints (7d) and (7e) are violated. Moreover, no tour can exist that does not contain node 1 by the two constraints. For more explanation on the subtour breaking mechanism accompanied with rigorous proof, refer to [16]. The constraint (7f) guarantees that path k between nodes i and j can be chosen at stage 2 only if nodes i and j were part of the tour fixed at stage 1. Finally, the constraints (7g)-(7i) restrict the space from which the variables take values.

Table 8 Notations for MPTSPs

Index sets: $N \\ K_{ij} \\ \mathcal{S}$	index set of nodes $(i, j, l \in N)$ index set of paths between nodes i and j $(k \in K_{ij})$ index set of scenarios $(s \in S)$		
Parameters:			
c_{ijk}^s	unit random travel time of path k between nodes i,j under scenario s		
$ar{c}_{ij}$	estimation of the mean unit travel time (expectation of c_{ijk}^s over all s and k)		
e_{ijk}^s	the error on the travel time on estimated for arc (i,j) and path k under scenario s		
$egin{array}{l} c_{ijk}^s \ ar{c}_{ij} \ e_{ijk}^s \ \mathbb{P}(s) \end{array}$	the probability of occurence of scenario s		
Decision variab	Decision variables:		
ϕ_{ij} (1 st stage)	the nonnegative real-valued flow on arc (i, j)		
y_{ij} (1 st stage) x_{ijk}^s (2 nd stage)	1 if path k between nodes $i,j\in N$ is selected at the second stage, 0 otherwise 1 if node j is visited just after node i , 0 otherwise		

6.5.2 Scenario data generation

We follow the scenario generation methods described through the references [11,12,13]. For MPTSPs, there are three mainly distinguished characteristics for each instance: the nodes partition strategy $(D \in \{D0, D1, D2, D3\}, \text{ explanation on each strategy is forthcoming), the number of nodes <math>(|N| \in \{2, 3, ...\})$, and the number of scenarios $(|S| \in \{1, 2, ...\})$. Another important charicteristic $|K_{ij}| \in \{1, 2, 3, ...\}$ is the number of paths for each edge which is fixed by 3 as a default following [13]. Once we decide D, |N|, and |S| by D = Dx, |N| = y, and |S| = z, each instance is named by MPTSPs_Dx_Ny_Sz.

The nodes are distributed in a circle with radius equal to r km. We use Cartesian coordinate system where the geometric center of the circle is (r,r). The nodes are distinguished by two subsets: central and suburban. If the Euclidean distance between a node and the geometric center is less than or equal to the half of the radius (r/2), then the node is of central type. Otherwise, if the Euclidean distance is greater than the half of the radius, the node is of suburban type. Each arc between any two nodes i and j is either homogeneous or heterogeneous. If the two nodes are of the same type of node, i.e., both are central or both are suburban, the type of the arc is homogeneous. Otherwise, the type of the arc is heterogeneous. Later, the travel time of each path between two nodes are affected by the type of arc.

The nodes are generated by one of the following distribution strategies:

- D0: All the nodes are *central*.
- D1: All the nodes are suburban.
- D2: 3/4 of the nodes are *central* and the remaining 1/4 are *suburban*.
- D3: 1/2 of the nodes are *central* and the remaining 1/2 are *suburban*.

Given D, |N| and |S|, the next procedure can be summarized as follows:

- 1. Generate |N| nodes based on the predetermined strategy D. Then, the nodes are generated by acceptance-rejection procedure with uniform random number generation. Again following [13], we fix r = 7km.
- 2. Calculate Euclidean distances between the nodes (EC_{ij}) .

3. We guess and fix the deterministic velocity profile by 40km/h for the central nodes and 80km/h for the suburban nodes: $v_{cntr} = 40$ and $v_{sbrb} = 80$.

- 4. Generate random travel times (c_{ijk}^s) for each scenario s.
 - The velocity for traveling arc (i, j) is affected by its arc type.
 - If the arc is homogeneous, the random travel time of all the paths are
 - generated only based on the corresponding velocity profile.
 If the arc is heterogeneous, $\left\lceil \frac{|K_{ij}|}{3} \right\rceil$ paths are generated based on $v_{cntr}=$ 40 and the remaining paths are generated based on $v_{sbrb} = 80$.
 - The velocities are distributed by $Unif(\frac{v}{2}, 2v)$ for $v = v_{cntr}, v_{sbrb}$.
 - In summary, if the arc (i, j) is homogeneous,

$$c_{ijk}^s \sim \begin{cases} \frac{EC_{ij}}{Unif(\frac{v_{cntr}}{2}, 2v_{cntr})} \text{ if } i, j \text{ are both } central, \\ \frac{EC_{ij}}{Unif(\frac{v_{sbrb}}{2}, 2v_{sbrb})} \text{ if } i, j \text{ are both } suburban, \end{cases} \forall k \in K_{ij}.$$

- Otherwise, if (i, j) is heterogeneous,

$$c_{ijk}^{s} \sim \begin{cases} \frac{EC_{ij}}{Unif(\frac{v_{entr}}{2}, 2v_{entr})} & \text{for } k \in \left\{1, \dots, \left\lceil \frac{|K_{ij}|}{3} \right\rceil \right\}, \\ \frac{EC_{ij}}{Unif(\frac{v_{sbrb}}{2}, 2v_{sbrb})} & \text{for } k \in \left\{ \left\lceil \frac{|K_{ij}|}{3} \right\rceil + 1, \dots, |K_{ij}| \right\}. \end{cases}$$

5. Finally, we multiply 3600 for each component of c_{ijk}^s to convert the unit from hours to seconds.

6.6 SIZES: Selection of an optimal subset of sizes

SIZES is a simplified version of the cutting stock problem with multi-period stochastic demand. In this problem, the term period can be exchangeably used with stage. The first period (first stage) demand is deterministic whereas demands for the other periods (stages) are stochastic with scenarios. We only consider the two-periods (i.e., two stage) model to follow [15] as well as the SIP of interest discussed in Section 2. In SIPLIB, only three instances are available in SMPS files. We refer to the mathematical formulation in [15] to construct Jump. Model. Due to some unclear explanations (or typo), we slightly modify the formulation and use it for SIPLIB 2.0.

6.6.1 Mathematical formulation

Table 9 Notations for SIZES

Index sets	
N	index set of items $(i, j \in N)$
T	index set of time periods $(t \in T)$
\mathcal{L}	index set of scenarios $(l \in \mathcal{L})$
Parameters	
d_{it}^l	demand for item i at time t under scenario l
p_i	unit production cost for item i
8	setup cost for producing any item
r	unit cutting cost
c_t^l	production capacity at time t under scenario l
$\mathbb{P}(l)$	the probability of occurence of scenario l
Decision variab	oles
y_{it} (1 st stage)	number of units of size i produced at time t
$x_{i,i}^l$ (2 nd stage)	number of units of size i cut to meet demand for smaller size j at time t under scenario l
$x_{ijt}^l $ (2 nd stage) $z_{it}^l $ (2 nd stage)	1 if we produce size i at time t under scenario l , 0 otherwise

(SIZES) min
$$\sum_{t \in T} \sum_{i \in N} p_i y_{it} + \sum_{l \in \mathcal{L}} \mathbb{P}(l) \sum_{t \in T} \left(\sum_{i \in N} s z_{it}^l + r \sum_{i \in N \setminus \{1\}} \sum_{j=1}^{i-1} x_{ijt}^l \right)$$
(8a)

s.t.
$$\sum_{i \in N} y_{it} \le c_t^l$$
, $\forall t \in T, \forall l \in \mathcal{L}$, (8b)

$$\sum_{i=j}^{|N|} x_{ijt}^l \ge d_{jt}^l, \quad \forall j \in N, \ \forall t \in T, \ \forall l \in \mathcal{L},$$
 (8c)

$$\sum_{t'=1}^{t} \sum_{j=1}^{i} x_{ijt'}^{l} \le \sum_{t'=1}^{t} y_{it'}, \quad \forall i \in N, \ \forall t \in T, \ \forall l \in \mathcal{L},$$
 (8d)

$$y_{it} \leq c_t^l z_{it}^l, \quad \forall i \in N, \ \forall t \in T, \ \forall l \in \mathcal{L},$$

$$y_{it} \in \mathbb{Z}_+, \quad \forall j \in N, \ \forall t \in T,$$

$$(8e)$$

$$y_{it} \in \mathbb{Z}_+, \quad \forall j \in N, \ \forall t \in T,$$
 (8f)

$$x_{ijt}^{l} \in \mathbb{Z}_{+}, \quad \forall i \in N, \ \forall j \in N, \ \forall t \in T, \ \forall l \in \mathcal{L},$$
 (8g)

$$z_{it}^l \in \{0, 1\}, \quad \forall i \in N, \ \forall t \in T, \ \forall l \in \mathcal{L}.$$
 (8h)

6.6.2 Scenario data generation

6.7 SUCW: Stochastic unit commitment problem with wind power

6.7.1 Mathematical formulation

$$\min \sum_{\sigma \in \mathcal{S}} \mathbb{P}(\sigma) \sum_{t \in T} \sum_{g \in G} \left(C_g^{fx} x_{gt}^{\sigma} + C_g^{up} u_{gt}^{\sigma} + C_g^{dn} v_{gt}^{\sigma} + \sum_{k \in K} C_{gk}^{mar} q_{gkt}^{\sigma} \right)$$
(9a)

s.t.
$$1 - x_{q(t-1)}^{\sigma} \ge u_{qt}^{\sigma}, \quad \forall \sigma \in \mathcal{S}, \ g \in G, \ t \in T,$$
 (9b)

$$x_{a(t-1)}^{\sigma} \ge v_{at}^{\sigma}, \quad \forall \sigma \in \mathcal{S}, \ g \in G, \ t \in T,$$
 (9c)

$$x_{gt}^{\sigma} - x_{g(t-1)}^{\sigma} = u_{gt}^{\sigma} - v_{gt}^{\sigma}, \quad \forall \sigma \in \mathcal{S}, \ g \in G, \ t \in T,$$

$$(9d)$$

$$x_{gt}^{\sigma} \ge \sum_{\tau = \max\{1, t - UT_{\sigma} + 1\}}^{t} u_{g\tau}^{\sigma}, \quad \forall \sigma \in \mathcal{S}, \ g \in G, \ t \in T,$$

$$(9e)$$

$$1 - x_{gt}^{\sigma} \ge \sum_{\tau = \max\{1, t - DT_o + 1\}}^{t} u_{g\tau}^{\sigma}, \quad \forall \sigma \in \mathcal{S}, \ g \in G, \ t \in T,$$

$$(9f)$$

$$-RD_g \le p_{gt}^{\sigma} - p_{g(t-1)}^{\sigma} \le RU_g - s_{gt}^{\sigma}, \quad \forall \sigma \in \mathcal{S}, \ g \in G, \ t \in T,$$
 (9g)

$$s_{gt}^{\sigma} \le RC_g x_{gt}^{\sigma}, \quad \forall \sigma \in \mathcal{S}, \ g \in G, \ t \in T,$$
 (9h)

$$\sum_{\sigma \in C} s_{gt}^{\sigma} \ge SR_t, \quad \forall \sigma \in \mathcal{S}, \ t \in T,$$
(9i)

$$p_{gt}^{\sigma} = P_g^{\min} x_{gt}^{\sigma} + \sum_{k \in K} q_{gkt}^{\sigma}, \quad \forall \sigma \in \mathcal{S}, \ g \in G, t \in T,$$

$$(9j)$$

$$p_{gt}^{\sigma} + s_{gt}^{\sigma} \le P_g^{\max} x_{gt}^{\sigma}, \quad \forall \sigma \in \mathcal{S}, \ g \in G, \ t \in T,$$
 (9k)

$$q_{gkt}^{\sigma} \le Q_{gk}^{\max} x_{gt}^{\sigma}, \quad \forall \sigma \in \mathcal{S}, \ g \in G, \ k \in K, \ t \in T,$$
 (91)

$$\sum_{g \in G} p_{gt}^{\sigma} = \sum_{n \in N} D_{nt}^{\sigma} - \sum_{w \in W} W_{wt}^{\sigma}, \quad \forall \sigma \in \mathcal{S}, \ t \in T,$$

$$(9m)$$

$$- \ F_l^{\max} \leq \sum_{g \in G} LSF_{lg} p_{gt}^{\sigma} - \sum_{n \in N} LSF_{ln} D_{nt}^{\sigma}$$

$$+ \sum_{w \in W} LSF_{lw} W_{wt}^{\sigma} \le F_l^{\max}, \quad \forall \sigma \in \mathcal{S}, \ l \in L, \ t \in T, \quad (9n)$$

$$x_{at}^{\sigma_1} = x_{at}^{\sigma_2}, \ u_{at}^{\sigma_1} = u_{at}^{\sigma_2}, \ v_{at}^{\sigma_1} = v_{at}^{\sigma_2}, \quad \forall \sigma_1, \sigma_2 \in \mathcal{S}, \ g \in G_s, \ t \in T,$$
 (90)

$$x_{q0}^{\sigma} = X_q^{\text{init}}, \quad \forall \sigma \in \mathcal{S}, \ g \in G,$$
 (9p)

$$x_{at}^{\sigma} = 1, \quad \forall \sigma \in \mathcal{S}, \ g \in G, \ t \in \{1, \dots, UT_{a}^{\text{init}}\},$$
 (9q)

$$x_{gt}^{\sigma} = 0, \quad \forall \sigma \in \mathcal{S}, \ g \in G, \ t \in \{1, \dots, DT_g^{\text{init}}\},$$
 (9r)

$$p_{q0}^{\sigma} = P_q^{\text{init}}, \quad \forall \sigma \in \mathcal{S}, \ g \in G,$$
 (9s)

$$x_{at}^{\sigma}, u_{at}^{\sigma}, v_{at}^{\sigma} \in \{0, 1\}, \quad \forall \sigma \in \mathcal{S}, \ g \in G, \ t \in T,$$
 (9t)

$$p_{at}^{\sigma}, q_{akt}^{\sigma}, s_{at}^{\sigma} \ge 0, \quad \forall \sigma \in \mathcal{S}, \ g \in G, \ t \in T.$$
 (9u)

Table 10 Notations for the SUCW

```
Index sets:
            index set of all generators (g \in G)
            index set of slow generators (g \in G_s)
G_s
G_f
            index set of fast generators (g \in G_f)
K
            index set of linear segments of the piece-wise linear power generation cost (k \in K)
L
            index set of transmission lines (l \in L)
N
            index set of buses (n \in N)
T
            index set of time periods (t \in T)
W
            index set of wind power generators (w \in W)
\mathcal{S}
            index set of scenarios (\sigma \in \mathcal{S})
Parameters:
C_g^{\rm up}
C_g^{\rm dn}
C_g^{\rm tx}
C_g^{\rm tx}
C_{gk}^{\rm mar}
X_g^{\rm init}
UT_g^{\rm init}
UT_g
DT_g^{\rm init}
            start-up cost of generator g
            shut-down cost of generator g
            fixed cost of operating the generator g
            k^{\mathrm{th}} marginal cost of production of generator g
            initial on/off status of generator g
            initial minimum uptime of generator g
            minimum uptime of generator g
            initial minimum downtime of generator g
            minimum downtime of generator g
            ramp-up limit of generator g
RU_g
RD_g
            ramp-down limit of generator g
RD_g
RC_g
P_g^{\text{init}}
P_g^{\text{min}}
P_g^{\text{max}}
Q_{gk}^{\text{max}}
            ramping capacity of generator g
            initial power output of generator g
            minimum power output of generator g
            maximum power output of generator g
            maximum power output of generator q with the k^{\text{th}} marginal cost
SR_t
            spinning reserve required at time t
F_{l}^{\max}
            maximum power flow of transmission line l
LSF_{ln}
            load-shift factor of transmission line l with respect to bus n
\mathbb{P}(\sigma)
            probability of scenario \sigma
\begin{array}{c} D_{nt}^{\sigma} \\ W_{wt}^{\sigma} \end{array}
            demand load at bus n at time t in scenario \sigma
            wind power generation from generator w at time t in scenario \sigma
Decision variables:
            on/off indicator of generator g at time t in scenario \sigma
            start-up indicator of generator g at time t in scenario \sigma
            shut-down indicator of generator g at time t in scenario \sigma
            power output of generator g at time t in scenario \sigma
            power output of generator g at time t with the k^{\rm th} marginal cost in scenario \sigma
            spinning reserve of generator g at time t in scenario \sigma
```

6.7.2 Scenario data generation

7 Solution report

8 Concluding remarks

(not finished yet) Any further contribution or suggestions for SIPLIB 2.0 are always welcomed. Better solutions than discovered so far, more functions, more

problems with Julia scripts for instance generation, more effective classification rules, etc.

References

- S. Ahmed, R. Garcia, N. Kong, L. Ntaimo, G. Parija, F. Qiu, S. Sen. SIPLIB: A Stochastic Integer Programming Test Problem Library. http://www.isye.gatech.edu/sahmed/siplib, 2015.
- SPS: Stochastic Programming Society (https://stoprog.org/what-stochastic-programming).
- 3. Introduction to Stochastic Programming, J. R. Birge, F. Louveaus.
- S. Ahmed and R. Garcia. "Dynamic Capacity Acquisition and Assignment under Uncertainty," Annals of Operations Research, vol.124, pp. 267-283, 2003.
- Kibaek Kim and Victor M. Zavala. "Algorithmic Innovations and Software for the Dual Decomposition Method applied to Stochastic Mixed-Integer Programs" Mathematical Programming Computation, 2015.
- 6. J.-P. Watson, D. L. Woodruff, and W. E. Hart, PySP: modeling and solving stochastic programs in Python, Mathematical Programming Computation, 2012.
- 7. SMI Stochastic Modeling Interface. https://github.com/coin-or/Smi
- Julia: A Fresh Approach to Numerical Computing. Jeff Bezanson, Alan Edelman, Stefan Karpinski and Viral B. Shah (2017) SIAM Review, 59: 6598.
- $9. \ \ JuMP-Julia \ for \ Mathematical \ Optimization, https://jump.readthedocs.io/en/latest/index.html$
- StructJuMP Parallel algebraic modeling framework for block structured optimization models in Julia, https://github.com/StructJuMP/StructJuMP.jl
- F. Maggioni, G. Perboli, and R. Tadei, The multi-path traveling salesman problem with stochastic travel socts: Building realistic instances for city ligistics applications, Transportation Research Procedia, 2014
- G. Perboli, L. Gobbato, and F. Maggioni, A progressive hedging method for the multipath travelling salesman problem with stochastic travel times, IMA Journal of Management Mathematics, 2017
- 13. R. Tadei, G. Perboli, and F. Perfetti, The multi-path traveling salesman problem with stochastic travel costs, EURO Journal on Transportation and Logistics, 2017
- Andre Langevin, Francois Soumis, and Jacques Desrosiers, Classification of travelling salesman problem formulations, Operations Research Letters, 1990
- 15. Soheila Jorjani, Carlton H. Scott, and David L. Woodruff, Selection of an optimal subset of sizes, International Journal of Production Research, 1999
- B. Gavish and S.C. Graves, The travelling salesman problem and related problems, Working paper GR-078-78, Operations Research Center, Massachusetts Institute of Technology, 1978
- Gustavo Angulo, Shabbir Ahmed, and Santanu S. Dey, Improving the integer L-shaped method, 2014.
- Anthony Papavasiliou and Shmuel S. Oren, Multiarea stochastic unit commitment for high wind penetration in a transmission constrained network, Operations Research, 2013
- Kibaek Kim, Fan Yang, Victor M. Zavala, and Andrew A. Chien, Data centers as dispatchable loads to harness stranded power, IEEE Transactions on sustainable energy, 2017
- Lewis Ntaimo and Suvrajeet Sen, The million-variable "March" for stochastic combinatorial optimization, Journal of Global Optimization, 2005
- 21. Koch et al., MIPLIB 2010, Mathmatical Programming Computation, 2011