

**TUGAS KECIL 2 IF2211 STRATEGI ALGORITMA:**  
**IMPLEMENTASI CONVEX HULL untuk VISUALISASI TES *LINEAR SEPARABILITY***  
***DATASET* dengan ALGORITMA *DIVIDE AND CONQUER***



Dibuat oleh :

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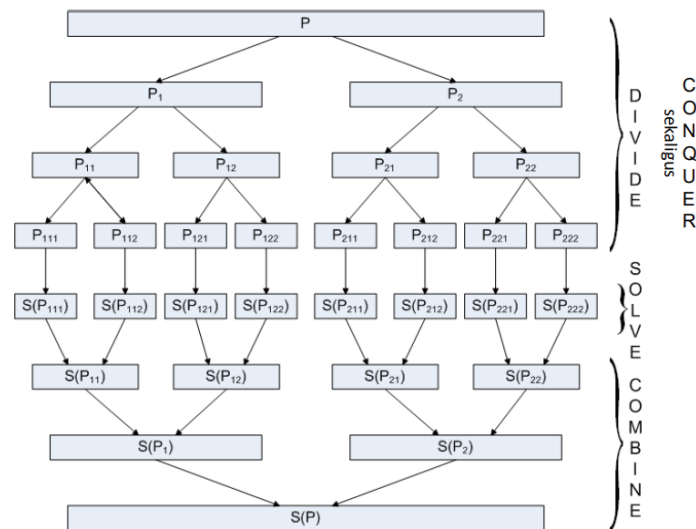
PROGRAM STUDI TEKNIK INFORMATIKA  
SEKOLAH TEKNIK ELEKTRO DAN INFORMATIKA  
INSTITUT TEKNOLOGI BANDUNG  
BANDUNG

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## A. Algoritma Divide and Conquer

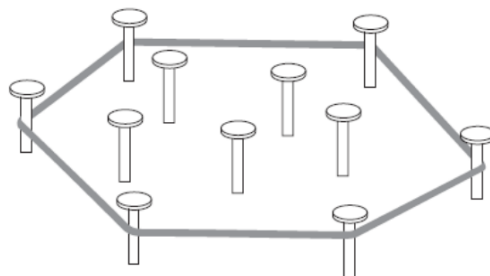
### 1. Definisi

Divide and Conquer adalah suatu algoritma yang membagi sebuah persoalan menjadi beberapa sub-persoalan yang memiliki kemiripan dengan persoalan semula namun berukuran lebih kecil. Algoritma ini melakukan dua buah aksi penting, yaitu conquer(solve) dan combine. Conquer menyelesaikan masing masing sub-persoalan dan combine adalah menggabungkan solusi masing masing sub-persoalan sehingga membentuk solusi persoalan semula. Berikut ilustrasi dari algoritma Divide and Conquer.



### 2. Implementasi Algoritma Divide and Conquer untuk menyelesaikan masalah *Convex Hull*

Convex hull adalah salah satu permasalahan yang berkaitan dengan bidang geometri komputasional. Convex hull ini didefinisikan sebagai himpunan titik terkecil yang mengandung koordinat yang sifatnya convex. Suatu koordinat bisa dikatakan convex apabila 2 buah titik sembarang pada semua segmen garis berakhir pada kedua titik tersebut terdapat pada koordinat tersebut.



Pada permasalahan ini, terdapat beberapa algoritma yang dapat digunakan seperti, algoritma *Graham Scan*, algoritma, *Jarvis's March*, dan algoritma *Quickhull*. Pada tugas kecil 2 ini, saya menggunakan algoritma *Quickhull* dan menggunakan konsep strategi Divide and Conquer. Berikut merupakan langkah langkah untuk mencari *Convex Hull* dengan menggunakan algoritma *Quickhull* :

1. Cari titik maksimum(kanan) dan minimum(kiri) dari suatu set of titik.
2. Setelah didapatkan titik titik yang saling berkaitan maka partisi set of titik dibagi menjadi dua dengan menggunakan determinan, apabila nilai determinan bernilai minus, maka set titik tersebut berada di segmen kiri(bawah) S1 dan apabila nilai determinan bernilai positif, maka set titik tersebut berada di segmen kanan(atas) S2.
3. Kumpulan titik pada S1 akan membentuk convex hull bagian bawah, dan kumpulan titik pada S2 akan membentuk convex hull bagian atas. S merupakan hasil gabungan (merge) dari S1 dan S2.
4. Sebelum dilakukan penggabungan pada S1 dan S2. diterapkan algoritma divide and conquer pada S1 dan S2, dalam program saya menggunakan algoritma quickhull dengan menggunakan fungsi quickhull\_kiri dan quickhull\_kanan, secara rekursif sampai tidak ada lagi titik yang bisa diproses lagi.
5. Hasil dari langkah ke-4 dilakukan penggabungan antara hasil rekursif S1 dan hasil rekursif S2 yang menjadi hasil penggabungan S.
6. Setelah proses 5 selesai, maka S akan menghasilkan bentuk Convex Hull yang terbentuk dari titik-titik pembentuk convex hull

## B. Kode Program

Fungsi Determinan	Fungsi Maxmin
<pre># fungsi untuk menghitung determinan dari 3 titik def determinan(titik1, titik2, titik3):     return (titik1[0] * titik2[1]) + (titik1[1] * titik3[0]) + (titik2[0] * titik3[1]) - (titik3[0] * titik2[1]) - (titik3[1] * titik1[0]) - (titik2[0] * titik1[1])</pre>	<pre># fungsi untuk mengembalikan nilai minimum dan maksimum dari suatu list titik def maxmin(list_titik):     minimum = list_titik[0]     maximum = list_titik[0]      for titik in list_titik:         if(titik[0] &lt;= minimum[0]):             minimum = titik         if(titik[0] &gt;= maximum[0]):             maximum = titik     return minimum,maximum</pre>
Fungsi Angle	Fungsi bagiSisi

```
# fungsi untuk mencari sudut
def angle(A,B,C):
    Ax, Ay = A[0]-B[0], A[1]-B[1]
    Cx, Cy = C[0]-B[0], C[1]-B[1]
    a = atan2(Ay, Ax)
    c = atan2(Cy, Cx)
    if a < 0: a += pi*2
    if c < 0: c += pi*2
    return (pi*2 + c - a) if a > c else (c - a)
```

```
# fungsi untuk membagi 2 sisi kiri
atau kanan dimana:
# kalo determinannya < 0 -> berada
di sisi kiri
# kalo determinannya > 0 -> berada
di sisi kanan
def bagiSisi(points,min,max):
    kiri = []
    kanan = []
    for titik in points:
        if(not((titik[0] == min[0])
and (titik[1] == min[1])) and
not((titik[0] == max[0]) and
(titik[1] == max[1]))):

if(determinan(min,max,titik)>0):
            kanan.append(titik)

if(determinan(min,max,titik)<0):
            kiri.append(titik)

    return kiri,kanan
```

Fungsi cariIndeks

```
def cariIndeks(titik,coordinate):
    i = 0
    for a in titik:
        if(coordinate[0] == a[0] and coordinate[1] == a[1]):
            return i
        else:
            i += 1
```

Fungsi merge

```
# Fungsi untuk menyatukan 2 buah list
def merge(list1, list2):
    for x in list2:
        list1.append(x)
    return list1
```

Fungsi quickhull\_kiri

Fungsi quickhull\_kanan

```
# setelah dibagi sisi maka tiap sisi melakukan quickhull
def quickhull_kiri(kiri,min_absis,max_absis,titik):
    if(len(kiri) == 0):
        result = [[cariIndeks(titik,min_absis),cariIndeks(titik,max_absis)]]
        return result
    else:
        sudut = 0
        temp = kiri[0]
        for coordinate in kiri:
            if(sudut < angle(coordinate,min_absis,max_absis)):
                sudut = angle(coordinate,min_absis,max_absis)
                temp = coordinate
        kiri_baru1,_ = bagiSisi(kiri,min_absis,temp)
        kiri_baru2,_ = bagiSisi(kiri,temp,max_absis)
        # bagian yang rekursi
        result1 = quickhull_kiri(kiri_baru1,min_absis,temp,titik)
        result2 = quickhull_kiri(kiri_baru2,temp,max_absis,titik)
        return merge(result1, result2)
```

```
def quickhull_kanan(kanan,min_absis,max_absis,titik):
    if(len(kanan)==0):
        result = [[cariIndeks(titik,min_absis),cariIndeks(titik,max_absis)]]
        return result
    else:
        sudut = 0
        temp = kanan[0]
        for coordinate in kanan:
            if(sudut < angle(max_absis,min_absis,coordinate)):
                sudut = angle(max_absis,min_absis,coordinate)
                temp = coordinate
        _,kanan_baru1 = bagiSisi(kanan,min_absis,temp)
        _,kanan_baru2 = bagiSisi(kanan,temp,max_absis)
        # bagian yagn rekursi
        result1 = quickhull_kanan(kanan_baru1,min_absis,temp,titik)
        result2 = quickhull_kanan(kanan_baru2,temp,max_absis,titik)
        return merge(result1, result2)
```

## Fungsi myhull

```
# setelah melakukan quickhull pada masing masing sisi, maka dilakukan penggabungan antara
# quickhull kiri dan kanan
def myHull(titik):
    result = []
    min_absis,max_absis = maxmin(titik)
    kiri,kanan = bagiSisi(titik,min_absis,max_absis)
    result_kiri = quickhull_kiri(kiri,min_absis,max_absis,titik)
    result_kanan = quickhull_kanan(kanan,min_absis,max_absis,titik)
    result = merge(result_kanan, result_kiri)
    return result
```

## convexhull.py

### Keseluruhan:

```
convexhull.py > @ bagiSisi
1 from math import atan2, pi
2
3 def determinan(titik1, titik2, titik3):
4     return (titik1[0] * titik2[1]) + (titik1[1] * titik3[0]) + (titik2[0] * titik3[1]) - (titik3[0] * titik2[1]) - (titik3[1] * titik1[0]) - (titik2[0] * titik1[1])
5
6 def maxmin(list_titik):
7     minimum = list_titik[0]
8     maximum = list_titik[0]
9
10    for titik in list_titik:
11        if(titik[0] <= minimum[0]):
12            minimum = titik
13        if(titik[0] >= maximum[0]):
14            maximum = titik
15    return minimum,maximum
16
17 def angle(A,B,C):
18     Ax, Ay = A[0]-B[0], A[1]-B[1]
19     Cx, Cy = C[0]-B[0], C[1]-B[1]
20     a = atan2(Ay, Ax)
21     c = atan2(Cy, Cx)
22     if a < 0: a += pi*2
23     if c < 0: c += pi*2
24     return (pi*2 + c - a) if a > c else (c - a)
25
26 def bagiSisi(points,min,max):
27     kiri = []
28     kanan = []
29     for titik in points:
30         if(not((titik[0] == min[0]) and (titik[1] == min[1])) and not((titik[0] == max[0]) and (titik[1] == max[1]))):
31             if(determinan(min,max,titik)>0):
32                 kanan.append(titik)
33             if(determinan(min,max,titik)<0):
34                 kiri.append(titik)
35
36     return kiri,kanan
37
38 def cariIndeks(titik,coordinate):
39     i = 0
40     for a in titik:
41         if(coordinate[0] == a[0] and coordinate[1] == a[1]):
42             return i
43         else:
44             i += 1
45
46 def merge(list1, list2):
47     for x in list2:
48         list1.append(x)
```

```
45
46 def merge(list1, list2):
47     for x in list2:
48         list1.append(x)
49     return list1
50
51 def quickhull_kiri(kiri,min_absis,max_absis,titik):
52     #print("min absis",min_absis,"max_absis",max_absis)
53     if(len(kiri) == 0):
54         result = [[cariIndeks(titik,min_absis),cariIndeks(titik,max_absis)]]
55         return result
56     else:
57         sudut = 0
58         temp = kiri[0]
59         for coordinate in kiri:
60             #print("sudut untuk koordinat",angle(coordinate,min_absis,max_absis),coordinate)
61             if(sudut < angle(coordinate,min_absis,max_absis)):
62                 sudut = angle(coordinate,min_absis,max_absis)
63                 temp = coordinate
64         kiri_baru1,_ = bagiSisi(kiri,min_absis,temp)
65         kiri_baru2,_ = bagiSisi(kiri,temp,max_absis)
66         #print("kiri temp,temp")
67         #print("kiri kiri baru")
68         #print(kiri_baru1,kiri_baru2)
69         result1 = quickhull_kiri(kiri_baru1,min_absis,temp,titik)
70         result2 = quickhull_kiri(kiri_baru2,temp,max_absis,titik)
71         return merge(result1, result2)
72
73 def quickhull_kanan(kanan,min_absis,max_absis,titik):
74     if(len(kanan)==0):
75         result = [[cariIndeks(titik,min_absis),cariIndeks(titik,max_absis)]]
76         return result
77     else:
78         sudut = 0
79         temp = kanan[0]
80         for coordinate in kanan:
81             if(sudut < angle(max_absis,min_absis,coordinate)):
82                 sudut = angle(max_absis,min_absis,coordinate)
83                 temp = coordinate
84         _,kanan_baru1 = bagiSisi(kanan,min_absis,temp)
85         _,kanan_baru2 = bagiSisi(kanan,temp,max_absis)
86         result1 = quickhull_kanan(kanan_baru1,min_absis,temp,titik)
87         result2 = quickhull_kanan(kanan_baru2,temp,max_absis,titik)
88         return merge(result1, result2)
89
90 def myHull(titik):
91     result = []
```

```
90 def myHull(titik):
91     result = []
92     min_abis,max_abis = maxmin(titik)
93     kiri,kanan = bagisisi(titik,min_abis,max_abis)
94     result_kiri = quickhull_kiri(kiri,min_abis,max_abis,titik)
95     result_kanan = quickhull_kanan(kanan,min_abis,max_abis,titik)
96     result = merge(result_kanan, result_kiri)
97     return result
```

## main.py

```
main.py > ...
1  import matplotlib.pyplot as plt
2  from sklearn import datasets
3  from convexhull import myHull
4  import pandas as pd
5
6  x = True
7  while x:
8      print("Berikut daftar dataset yang bisa digunakan: ")
9      print("1. Iris")
10     print("2. Breast Cancer")
11     print("3. Wine")
12     pilihan = int(input("Pilihan Dataset: "))
13
14     if(pilihan >= 1 and pilihan<= 3):
15         if(pilihan == 1):
16             data = datasets.load_iris()
17         elif(pilihan == 2):
18             data = datasets.load_breast_cancer()
19         elif(pilihan == 3):
20             data = datasets.load_wine()
21
22         df = pd.DataFrame(data.data, columns=data.feature_names)
23         df['Target'] = pd.DataFrame(data.target)
24         jumlahAttribut = len(data.feature_names)
25
26         print(" ")
27         print("Berikut daftar attribute: ")
28         for i in range(jumlahAttribut):
29             print(str(i+1) + "." + data.feature_names[i])
30         x = int(input("Pilihan attribute x: "))
31         y = int(input("Pilihan attribute y: "))
32
33         if ((x>=1 and x<= jumlahAttribut) and (y>=1 and y <= jumlahAttribut) and (x != y)):
34             plt.figure(figsize = (10, 6))
35             label = len(df['Target'].unique())
36             colors = ['b','r','g']
37
38             plt.title(str(data.feature_names[x-1])+" vs "+str(data.feature_names[y-1]))
39             plt.xlabel(data.feature_names[x-1])
40             plt.ylabel(data.feature_names[y-1])
41
42             for i in range(label):
43                 bucket = df[df['Target'] == i]
44                 bucket = bucket.iloc[:,[x-1,y-1]].values
45                 hull = myHull(bucket) #implementasi convexhull
46                 plt.scatter(bucket[:, 0], bucket[:, 1], label=data.target_names[i], color=colors[i])
47                 for simplex in hull:
48                     plt.plot(bucket[simplex, 0], bucket[simplex, 1], color=colors[i])
49             plt.legend()
50             plt.show()
51             plt.close('all')
52         else:
53             print("invalid attribute")
54     else:
55         print("Masukan Salah")
56
57     endState = input("\nMau coba dataset yang lain? (Y/N): ")
58     if endState.upper() != "Y":
59         x = False
60
61
```



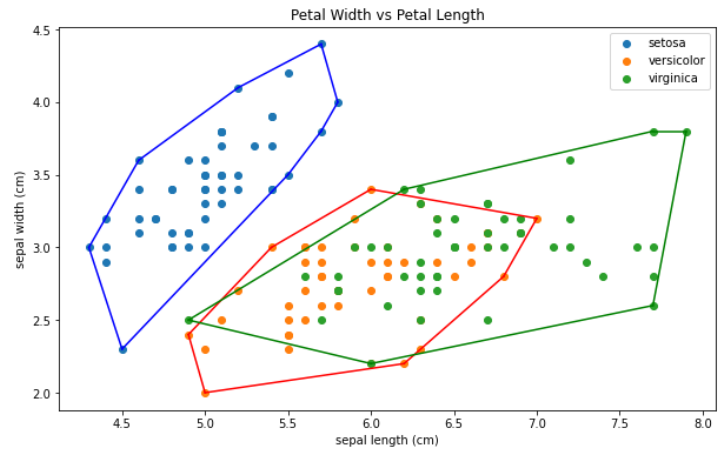
## C. Screenshot

### Dataset Iris:

```
import matplotlib.pyplot as plt
from sklearn import datasets
import pandas as pd
import matplotlib.pyplot as plt

data = datasets.load_iris()
df = pd.DataFrame(data.data, columns=data.feature_names)
df['Target'] = pd.DataFrame(data.target)
print(df.shape)
print(df.head())

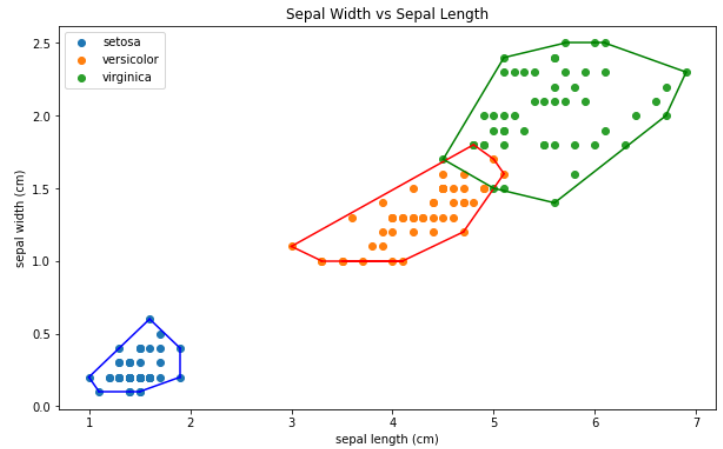
plt.figure(figsize = (10, 6))
colors = ['b','r','g']
plt.title('Petal Width vs Petal Length')
plt.xlabel(data.feature_names[0])
plt.ylabel(data.feature_names[1])
for i in range(len(data.target_names)):
    bucket = df[df['Target'] == i]
    bucket = bucket.iloc[:,[0,1]].values
    hull = myHull(bucket)
    plt.scatter(bucket[:, 0], bucket[:, 1], label=data.target_names[i])
    for simplex in hull:
        plt.plot(bucket[simplex, 0], bucket[simplex, 1], colors[i])
plt.legend()
```



```
import matplotlib.pyplot as plt
from sklearn import datasets
import pandas as pd
import matplotlib.pyplot as plt

data = datasets.load_iris()
df = pd.DataFrame(data.data, columns=data.feature_names)
df['Target'] = pd.DataFrame(data.target)
print(df.shape)
print(df.head())

plt.figure(figsize = (10, 6))
colors = ['b','r','g']
plt.title('Sepal Width vs Sepal Length')
plt.xlabel(data.feature_names[0])
plt.ylabel(data.feature_names[1])
for i in range(len(data.target_names)):
    bucket = df[df['Target'] == i]
    bucket = bucket.iloc[:,[2,3]].values
    hull = myHull(bucket)
    plt.scatter(bucket[:, 0], bucket[:, 1], label=data.target_names[i])
    for simplex in hull:
        plt.plot(bucket[simplex, 0], bucket[simplex, 1], colors[i])
plt.legend()
```

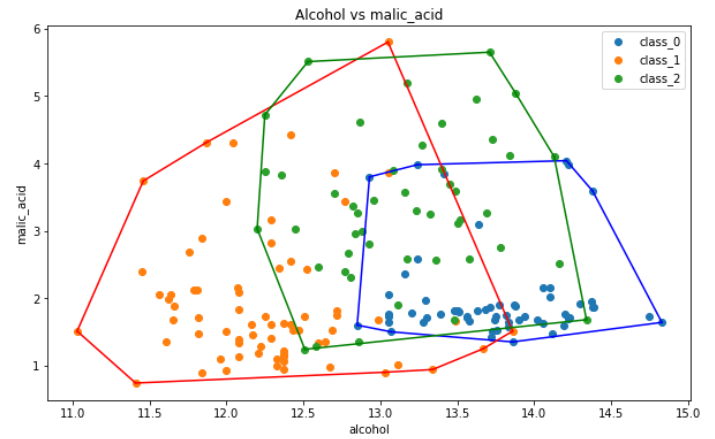


## Dataset Wine:

```
import matplotlib.pyplot as plt
from sklearn import datasets
import pandas as pd
import matplotlib.pyplot as plt

data = datasets.load_wine()
df = pd.DataFrame(data.data, columns=data.feature_names)
df['Target'] = pd.DataFrame(data.target)
print(df.shape)
print(df.head())

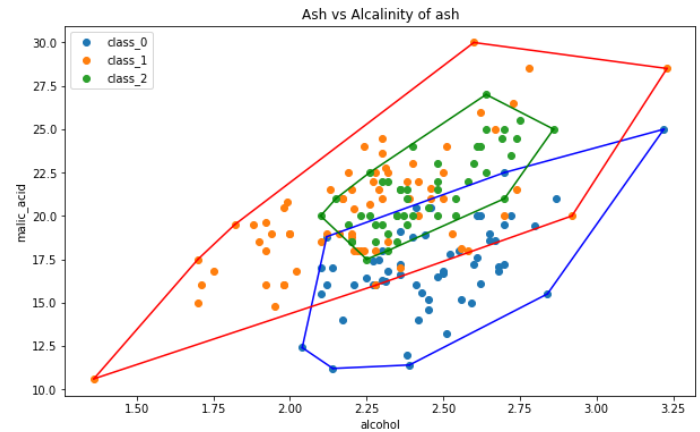
plt.figure(figsize = (10, 6))
colors = ['b','r','g']
plt.title('Alcohol vs malic_acid')
plt.xlabel(data.feature_names[0])
plt.ylabel(data.feature_names[1])
for i in range(len(data.target_names)):
    bucket = df[df['Target'] == i]
    bucket = bucket.iloc[:,0,1].values
    hull = myHull(bucket)
    plt.scatter(bucket[:, 0], bucket[:, 1], label=data.target_names[i])
    for simplex in hull:
        plt.plot(bucket[simplex, 0], bucket[simplex, 1], colors[i])
plt.legend()
```



```
import matplotlib.pyplot as plt
from sklearn import datasets
import pandas as pd
import matplotlib.pyplot as plt

data = datasets.load_wine()
df = pd.DataFrame(data.data, columns=data.feature_names)
df['Target'] = pd.DataFrame(data.target)
print(df.shape)
print(df.head())

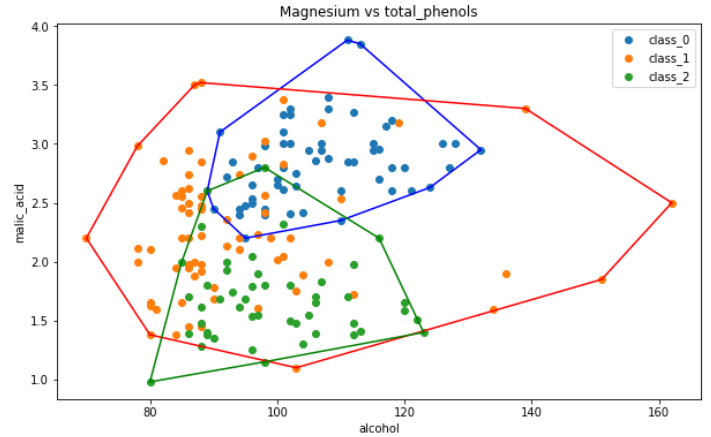
plt.figure(figsize = (10, 6))
colors = ['b','r','g']
plt.title('Ash vs Alcalinity of ash')
plt.xlabel(data.feature_names[0])
plt.ylabel(data.feature_names[1])
for i in range(len(data.target_names)):
    bucket = df[df['Target'] == i]
    bucket = bucket.iloc[:,2,3].values
    hull = myHull(bucket)
    plt.scatter(bucket[:, 0], bucket[:, 1], label=data.target_names[i])
    for simplex in hull:
        plt.plot(bucket[simplex, 0], bucket[simplex, 1], colors[i])
plt.legend()
```



```
import matplotlib.pyplot as plt
from sklearn import datasets
import pandas as pd
import matplotlib.pyplot as plt

data = datasets.load_wine()
df = pd.DataFrame(data.data, columns=data.feature_names)
df['Target'] = pd.DataFrame(data.target)
print(df.shape)
print(df.head())

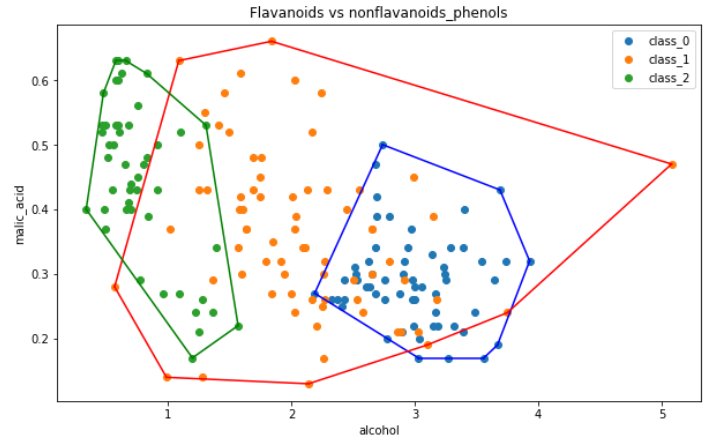
plt.figure(figsize = (10, 6))
colors = ['b','r','g']
plt.title('Magnesium vs total_phenols')
plt.xlabel(data.feature_names[0])
plt.ylabel(data.feature_names[1])
for i in range(len(data.target_names)):
    bucket = df[df['Target'] == i]
    bucket = bucket.iloc[:,4,5].values
    hull = myHull(bucket)
    plt.scatter(bucket[:, 0], bucket[:, 1], label=data.target_names[i])
    for simplex in hull:
        plt.plot(bucket[simplex, 0], bucket[simplex, 1], colors[i])
plt.legend()
```



```
import matplotlib.pyplot as plt
from sklearn import datasets
import pandas as pd
import matplotlib.pyplot as plt

data = datasets.load_wine()
df = pd.DataFrame(data.data, columns=data.feature_names)
df['Target'] = pd.DataFrame(data.target)
print(df.shape)
print(df.head())

plt.figure(figsize = (10, 6))
colors = ['b','r','g']
plt.title('Flavanoids vs nonflavanoids_phenols')
plt.xlabel(data.feature_names[0])
plt.ylabel(data.feature_names[1])
for i in range(len(data.target_names)):
    bucket = df[df['Target'] == i]
    bucket = bucket.iloc[:,6,7].values
    hull = myHull(bucket)
    plt.scatter(bucket[:, 0], bucket[:, 1], label=data.target_names[i])
    for simplex in hull:
        plt.plot(bucket[simplex, 0], bucket[simplex, 1], colors[i])
plt.legend()
```

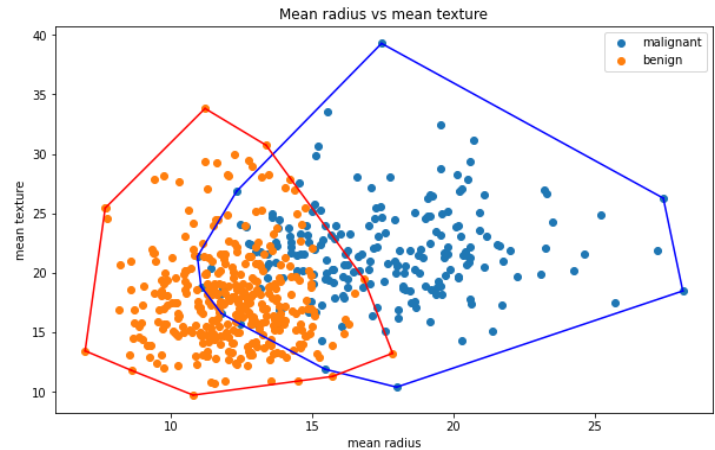


## Dataset Cancerbreast:

```
import matplotlib.pyplot as plt
from sklearn import datasets
import pandas as pd
import matplotlib.pyplot as plt

data = datasets.load_breast_cancer()
df = pd.DataFrame(data.data, columns=data.feature_names)
df['Target'] = pd.DataFrame(data.target)
print(df.shape)
print(df.head())

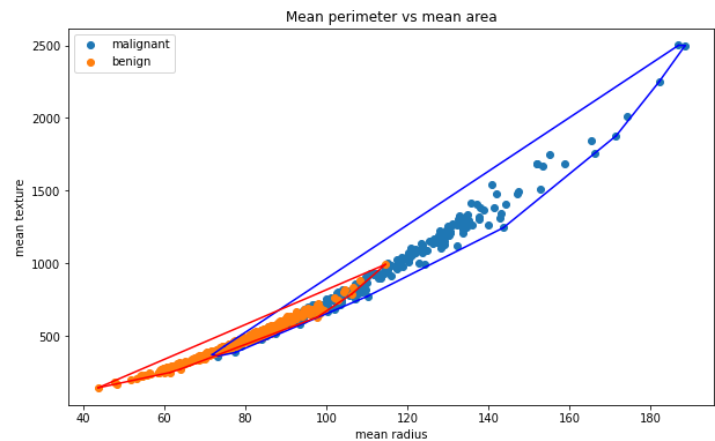
plt.figure(figsize = (10, 6))
colors = ['b','r','g']
plt.title('Mean radius vs mean texture')
plt.xlabel(data.feature_names[0])
plt.ylabel(data.feature_names[1])
for i in range(len(data.target_names)):
    bucket = df[df['Target'] == i]
    bucket = bucket.iloc[:,[0,1]].values
    hull = myHull(bucket)
    plt.scatter(bucket[:, 0], bucket[:, 1], label=data.target_names[i])
    for simplex in hull:
        plt.plot(bucket[simplex, 0], bucket[simplex, 1], colors[i])
plt.legend()
```



```
import matplotlib.pyplot as plt
from sklearn import datasets
import pandas as pd
import matplotlib.pyplot as plt

data = datasets.load_breast_cancer()
df = pd.DataFrame(data.data, columns=data.feature_names)
df['Target'] = pd.DataFrame(data.target)
print(df.shape)
print(df.head())

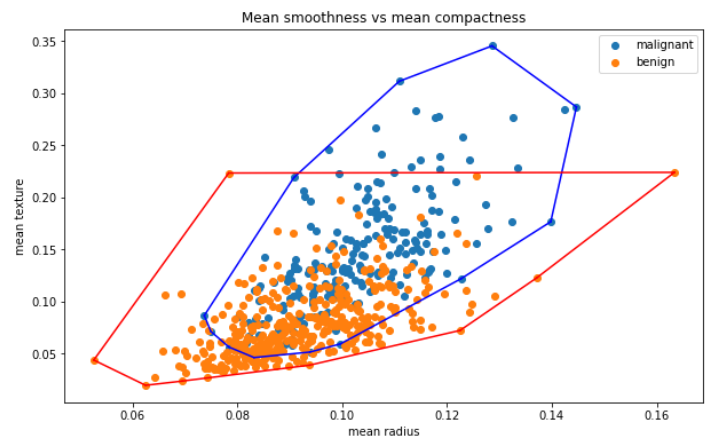
plt.figure(figsize = (10, 6))
colors = ['b','r','g']
plt.title('Mean perimeter vs mean area')
plt.xlabel(data.feature_names[0])
plt.ylabel(data.feature_names[1])
for i in range(len(data.target_names)):
    bucket = df[df['Target'] == i]
    bucket = bucket.iloc[:,[2,3]].values
    hull = myHull(bucket)
    plt.scatter(bucket[:, 0], bucket[:, 1], label=data.target_names[i])
    for simplex in hull:
        plt.plot(bucket[simplex, 0], bucket[simplex, 1], colors[i])
plt.legend()
```



```
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df = pd.DataFrame(data.data, columns=data.feature_names)
df['Target'] = pd.DataFrame(data.target)
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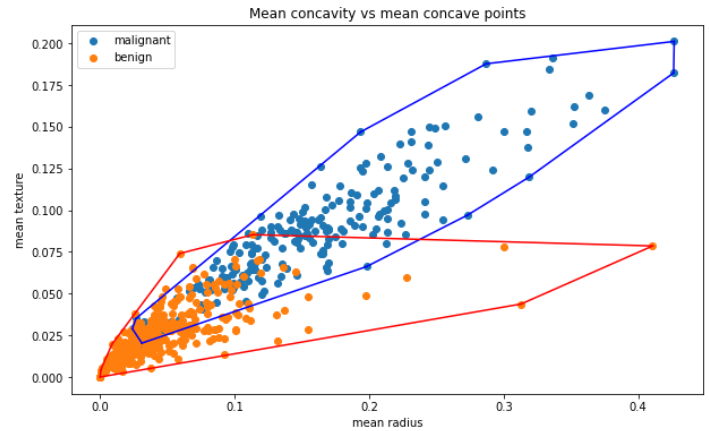
plt.figure(figsize = (10, 6))
colors = ['b','r','g']
plt.title('Mean smoothness vs mean compactness')
plt.xlabel(data.feature_names[0])
plt.ylabel(data.feature_names[1])
for i in range(len(data.target_names)):
    bucket = df[df['Target'] == i]
    bucket = bucket.iloc[:,[4,5]].values
    hull = myHull(bucket)
    plt.scatter(bucket[:, 0], bucket[:, 1], label=data.target_names[i])
    for simplex in hull:
        plt.plot(bucket[simplex, 0], bucket[simplex, 1], colors[i])
plt.legend()
```



```
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from sklearn import datasets
import pandas as pd
import matplotlib.pyplot as plt

data = datasets.load_breast_cancer()
df = pd.DataFrame(data.data, columns=data.feature_names)
df['Target'] = pd.DataFrame(data.target)
print(df.shape)
print(df.head())

plt.figure(figsize = (10, 6))
colors = ['b', 'r', 'g']
plt.title('Mean concavity vs mean concave points')
plt.xlabel(data.feature_names[0])
plt.ylabel(data.feature_names[1])
for i in range(len(data.target_names)):
    bucket = df[df['Target'] == i]
    bucket = bucket.iloc[:, [6, 7]].values
    hull = myHull(bucket)
    plt.scatter(bucket[:, 0], bucket[:, 1], label=data.target_names[i])
    for simplex in hull:
        plt.plot(bucket[simplex, 0], bucket[simplex, 1], colors[i])
plt.legend()
```



#### D. Alamat Drive dan Link Github

Link Drive :

Link Github: [https://github.com/kibare/13520111\\_Tucil2](https://github.com/kibare/13520111_Tucil2)

#### E. CHECKLIST

Point	YA	TIDAK
1. Pustaka myConvexHull berhasil dibuat dan tidak ada kesalahan	✓	
2. Convex hull yang dihasilkan sudah benar	✓	
3. Pustaka myConvexHull dapat digunakan untuk menampilkan convex hull setiap label dengan warna yang berbeda	✓	
4. <b>Bonus:</b> program dapat menerima input dan menuliskan output untuk dataset lainnya	✓	