

1. Compute the residues of the following problems
 - (a) $43 \bmod 5$
 - (b) $21 \bmod 5$
 - (c) $43 \bmod 7$
 - (d) $21 \bmod 7$
 - (e) $43 \bmod 11$
 - (f) $21 \bmod 11$
 - (g) $43 \bmod 13$
 - (h) $21 \bmod 13$
 - (i) $43 \bmod 17$
 - (j) $21 \bmod 17$
2. Find the GCD for the following sets of values
 - (a) 23480 and 32400
 - (b) 73847 and 25094
 - (c) 123456789 and 987654321
3. Find the inverse for each of these values
 - (a) $13^{-1} \bmod 461$
 - (b) $2^{-1} \bmod 991$
 - (c) $1086^{-1} \bmod 1087$
4. Solve the following set of congruences:
$$\begin{aligned}x &\equiv 1 \bmod 3 \\x &\equiv 4 \bmod 5 \\x &\equiv 5 \bmod 7\end{aligned}$$
5. Can you think of a clever way to find a solution to this system?
$$\begin{aligned}x &\equiv 2 \bmod 3 \\x &\equiv 4 \bmod 5 \\x &\equiv 6 \bmod 7\end{aligned}$$