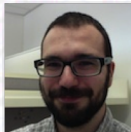


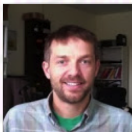
# Learning Molecular Fingerprints from the Graph Up



David Duvenaud, Dougal Maclaurin,



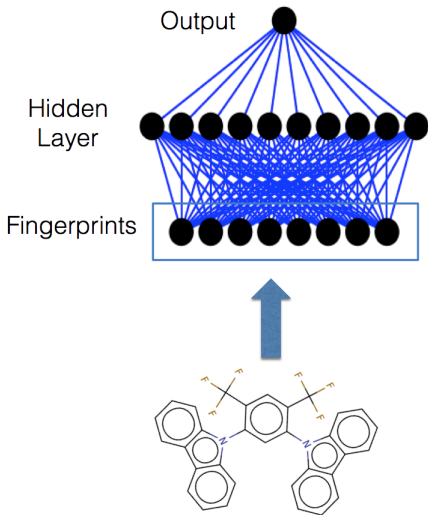
Jorge Aguilera-Iparraguirre, Rafael Gómez-Bombarelli,



Timothy Hirzel, Alán Aspuru-Guzik, Ryan P. Adams

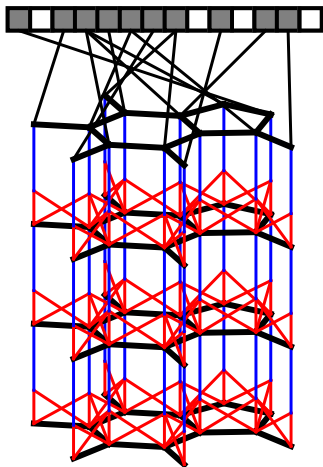
# Motivation

- Want to do regression on molecules
- For virtual screening of drugs, materials, etc.
- Problem: Molecules can be any size and shape
- Only know how to learn from fixed-size examples.
- How to take a molecule in and produce a fixed-size vector?



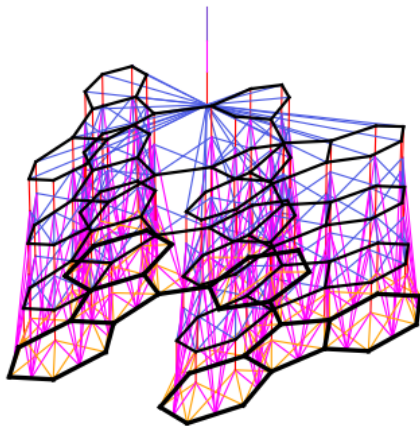
# Circular Fingerprints

- Standard method lists all substructures below a certain size
- Can do this by combining hashes of each atom with and bonded neighbors
- Hash value indexes into a fixed-sized vector
- Problem: can't optimize with gradients



# What would Ryan do?

- Maybe we can build a message-passing network
- same function is applied to each node (atom) and its neighbors
- Like a convolutional net
- At the top, add all node's vectors together
- If we use a softmax, this generalizes circular fingerprints



# Differentiable fingerprints

## Circular fingerprints

```

1: Input: molecule, radius  $R$ , fingerprint length  $S$ 
2: Initialize: fingerprint vector  $\mathbf{f} \leftarrow \mathbf{0}_S$ 
3: for each atom  $a$  in molecule do
4:    $\mathbf{r}_a \leftarrow g(a)$   $\triangleright$  lookup atom features
5: for  $L = 1$  to  $R$  do  $\triangleright$  for each layer
6:   for each atom  $a$  in molecule do
7:      $\mathbf{r}_1 \dots \mathbf{r}_N = \text{neighbors}(a)$ 
8:      $\mathbf{v} \leftarrow [\mathbf{r}_a, \mathbf{r}_1, \dots, \mathbf{r}_N]$   $\triangleright$  concatenate
9:      $\mathbf{r}_a \leftarrow \text{hash}(\mathbf{v})$   $\triangleright$  hash function
10:     $i \leftarrow \text{mod}(r_a, S)$   $\triangleright$  convert to index
11:     $\mathbf{f}_i \leftarrow 1$   $\triangleright$  Write 1 at index
12: Return: binary vector  $\mathbf{f}$ 
  
```

## Neural graph fingerprints

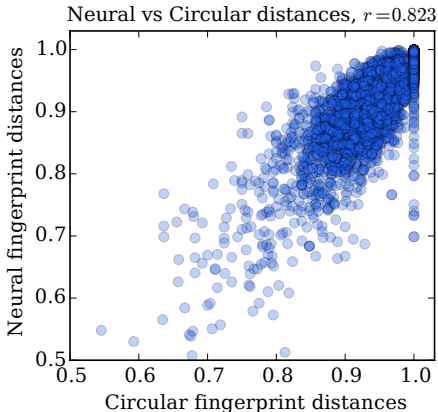
```

1: Input: molecule, radius  $R$ , weights  $H_1^1 \dots H_R^5$ , output weights  $W_1 \dots W_R$ 
2: Initialize: fingerprint vector  $\mathbf{f} \leftarrow \mathbf{0}_S$ 
3: for each atom  $a$  in molecule do
4:    $\mathbf{r}_a \leftarrow g(a)$   $\triangleright$  lookup atom features
5: for  $L = 1$  to  $R$  do  $\triangleright$  for each layer
6:   for each atom  $a$  in molecule do
7:      $\mathbf{r}_1 \dots \mathbf{r}_N = \text{neighbors}(a)$ 
8:      $\mathbf{v} \leftarrow \mathbf{r}_a + \sum_{i=1}^N \mathbf{r}_i$   $\triangleright$  sum
9:      $\mathbf{r}_a \leftarrow \sigma(\mathbf{v} H_L^N)$   $\triangleright$  smooth function
10:     $\mathbf{i} \leftarrow \text{softmax}(\mathbf{r}_a W_L)$   $\triangleright$  sparsify
11:     $\mathbf{f} \leftarrow \mathbf{f} + \mathbf{i}$   $\triangleright$  add to fingerprint
12: Return: real-valued vector  $\mathbf{f}$ 
  
```

Every non-differentiable operation is replaced with a differentiable analog.

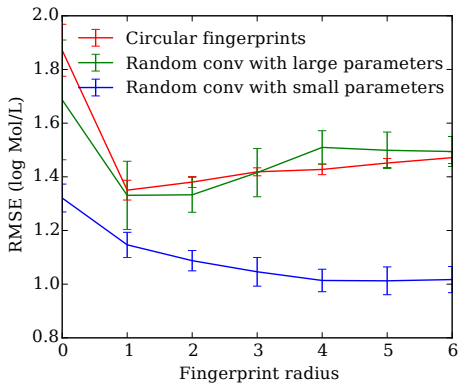
# Generalizing Circular Fingerprints

- If we generalize existing fingerprints, we can't not win (unless we overfit)
- large random weights makes neural nets act like hash functions
- Looked at similarities between pairwise distances.



# Generalizing Circular Fingerprints

- If we generalize existing fingerprints, we can't not win (unless we overfit)
- large random weights makes neural nets act like hash functions
- Looked at performance of random weights.



# Performance

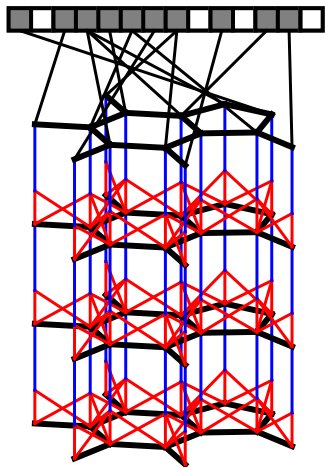
Dataset Units	Solubility log Mol/L	Drug efficacy EC <sub>50</sub> in nM	Photovoltaic efficiency percent
Predict mean	4.29 ± 0.40	1.47 ± 0.07	6.40 ± 0.09
Circular FPs + linear layer	1.84 ± 0.08	<b>1.13 ± 0.03</b>	2.62 ± 0.07
Circular FPs + neural net	1.40 ± 0.15	1.24 ± 0.03	2.04 ± 0.07
Neural FPs + linear layer	0.74 ± 0.09	<b>1.16 ± 0.03</b>	2.71 ± 0.13
Neural FPs + neural net	<b>0.53 ± 0.07</b>	<b>1.17 ± 0.03</b>	<b>1.44 ± 0.11</b>

- Could also try varying depth of neural net on top (used one hidden layer here)



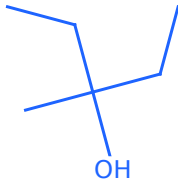
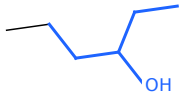
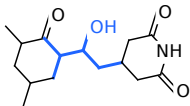
# Interpretability

- Circular fingerprints activate for a single substructure
- No generalization
- No notion of similarity
- Let's put a linear layer on top of neural fingerprints and examine which fragments activate most predictive features.

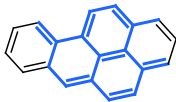
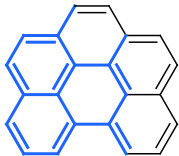
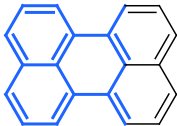


# Interpretability: Solubility

Fragments activating feature most predictive of solubility:

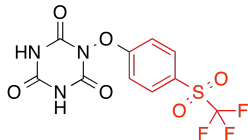
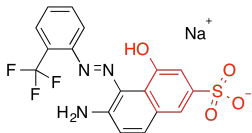
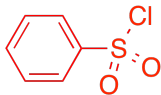


most predictive of insolubility:

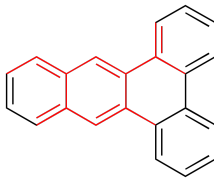
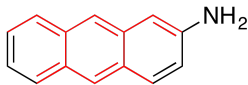
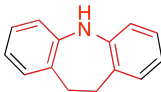


# Interpretability: Toxicity

Fragments most activated by toxicity feature on SR-MMP dataset:

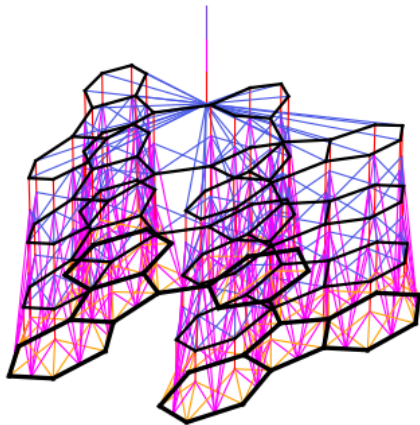


Fragments most activated by toxicity feature on NR-AHR dataset:



# Future Work

- Limitation: Slow because of so many weight transforms
- Could use low-rank weight matrices
- Limitation: All features are local
- Could learn to “parse” molecules
- But how to take gradients?



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