

CS 560 HW 3: Maximum-Subarray Problem and

Question 1

Develop a python function to solve textbook (CLRS) Exercises 4.1-5:

Use the following ideas to develop a non-recursive, linear-time algorithm for the maximum-subarray problem. Start at the left end of the array, and progress toward the right, keeping track of the maximum subarray seen so far. Knowing a maximum subarray of $A[1 \dots j]$, extend the answer to find a maximum subarray ending at index $j + 1$ by using the following observation: a maximum subarray of $A[1 \dots j + 1]$ is either a maximum subarray of $A[1 \dots j]$ or a subarray $A[i \dots j + 1]$, for some $1 \leq i \leq j + 1$. Determine a maximum subarray of form $A[i \dots j + 1]$ in constant time based on knowing a maximum subarray ending at index j .

Question 2

CLRS Exercise 4.5-1: use the master method to give tight asymptotic bounds for the following recurrences.

- $T(n) = 2T(n/4) + 1$.
- $T(n) = 2T(n/4) + \sqrt{n}$
- $T(n) = 2T(n/4) + n$.
- $T(n) = 2T(n/4) + n^2$.

Question 3

CLRS Exercise 4.5-3: Use the master method to show that the solution to the binary-search recurrence $T(n) = T(n/2) + \Theta(1)$ is $T(n) = \Theta(\lg n)$.