

Line Representation and simple Transformation

Line Representation

Line can be represented mathematically by:

$$P = P_0 + tV$$

This means we have an initial point P_0 and on that point, we add some 'scaled' vector V .
Let our vector $V = [0.3, 0.4]$.

The length (Norm) of V is $\sqrt{(0.3)^2 + (0.4)^2} = 0.5$ units

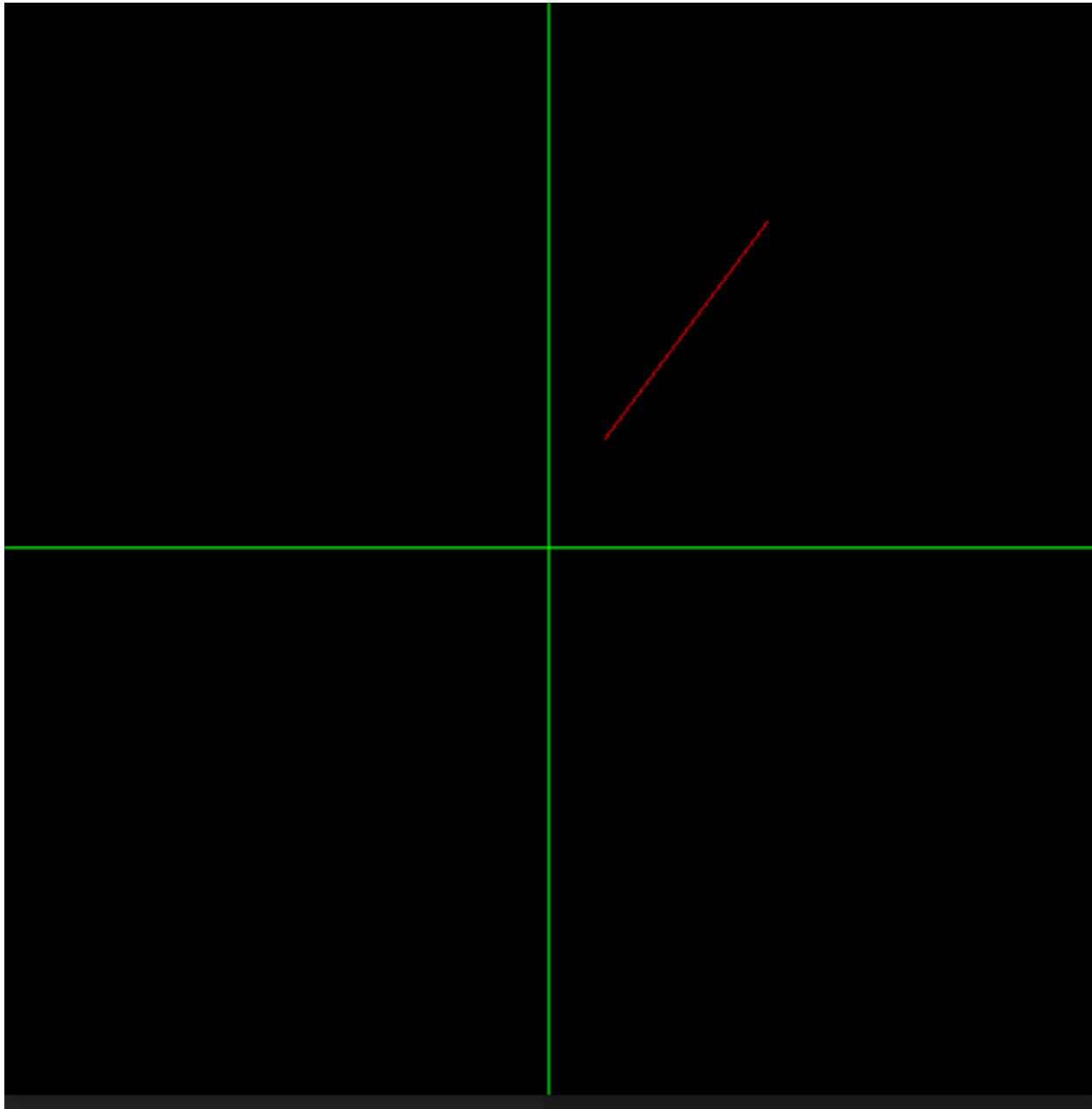
The direction of the vector is about 53 degree, calculated by tan inverse function.
Let the $P_0 = (0.1, 0.2)$

Now if we calculate $P = P_0 + tV$, for $t = 1$, we will get a line that starts from P_0 in a direction of 53' with length of 0.5 units

- a. If $t < 1$ and $t > 0$ then the line will be less than 0.5 units in length.
- b. If $t > 1$ then the line will be more than 0.5 units in length
- c. If $t < 0$ then the line will be drawn backwards.

Try to program this in PyOpenGL. Start with the basic.py file and follow the instructions.

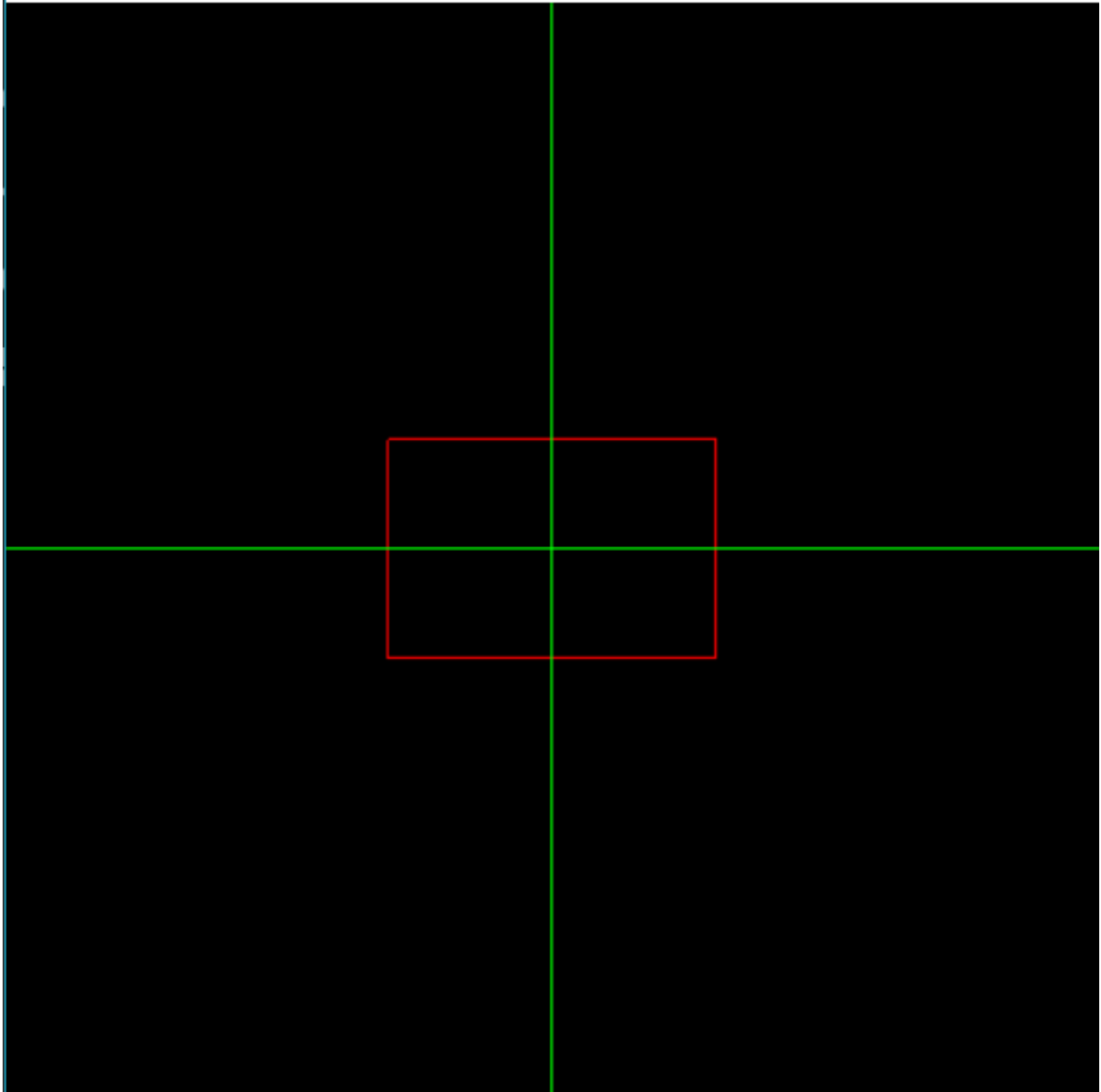
1. Create a numpy vector that contains $[0.3, 0.4]$
2. Create a point with numpy that is $(0.1, 0.2)$
3. Calculate P using $P = P_0 + tV$ with $t = 1$
4. Draw the line with PyOpenGL
5. Recalculate and draw the line with $t = 0.5$ and $t = 1.2$ and see the difference
6. Draw a grid line X-Axis and Y-Axis with different color



Exercise:

- a. Draw a rectangle by drawing four sides of the rectangles as a line. Its side must be a width of 0.6 and height of 0.4 units and the rectangle must be in the center. It might be easy for you if you first calculate on paper.

Here is a screenshot that is expected.



Transformation

Transformation is generally a change applied to a certain object. For example, change in size of an object, change in orientation (Rotation).

On this exercise, we will see a simple rotation of the box we drew on Exercise 1.

Import everything from transform.py in your exercise 1 python file.

In transform.py we have a function rotationMat function which returns a rotation matrix. A rotation matrix is a matrix that rotates an object along an axis when it is multiplied with the object's vertices.

Example. Let P be a point and M be a rotation matrix.
 $P \times M = P \text{ rotated}$

So to rotate an object, we simply need to multiply all our points with a rotation matrix. The rotationMat function in transform.py accepts parameters of degree by which we rotate an object.

Exercise 2:

Rotate the box you have made on Exercise 1

- Create a variable mat and assign it to rotation matrix of 60°
- Using np.dot function multiply the points of the box with mat
- Add .4 to all points and see what happens.

