DISCUSSION LOG

Sikang Yan

University of Kaiserslautern yan@rhrk.uni-kl.de

May 5, 2019

THEORY

In our cloth simulation, we follow the precedure written by Rohmer et al.. We consider to begin with the *Defomation gradient* \mathbf{F} , which is defined by

$$\mathbf{F} = \frac{\partial \mathbf{x}}{\partial \mathbf{X}},\tag{1}$$

where the ${\bf x}$ denotes the deformed vector and the ${\bf X}$ denotes the reference vector.

Since we have no further information about the mapping from ${\bf X}$ to ${\bf x}$, we use the vector $({\bf u_1},{\bf u_2})$ and $(\overline{{\bf u_1}},\overline{{\bf u_2}})$ to approximate the Defomation gradient, which is defined as

$$\mathbf{F} = \left[\mathbf{u}_{1}, \mathbf{u}_{2}\right] \left[\overline{\mathbf{u}_{1}}, \overline{\mathbf{u}_{2}}\right]^{-1}, \tag{2}$$

Attention should be paid especially:

- eq.(2) characrize only the 2D deformation of each triangle.
- in Rohmer et al. **F** is symbolised as **T**.

Sikang Yan (TUK)

Short title

May 5, 2019

2/26

We provide here our code preceed with concrete data:

• faces(i,j) is the jth vertex of the ith triangle, here we choose the face(0,0), face(0,1), face(0,2) as examples and calculate the VecT and VecR for face(0,0).

cloth_vec

$$VecT = el_1 VertT_1 - el_1 VertT_2$$
; $el_1 VertT_1 - el_1 VertT_3$ (3)

$$VecR = el_1 VertR_1 - el_1 VertR_2$$
; $el_1 VertR_1 - el_1 VertR_3$ (4)

cloth_vec

$$VecT = [0.771842 - 0.0144887 \ 6.39045] - [0.780121 - 0.0186188 \ 6.37318]$$
 (5)

$$[0.771842 - 0.0144887 \ 6.39045] - [0.737177 - 0.00912791 \ 6.39292]$$

$$VecR = [0.759919 - 0.015194 \ 6.38401] - [0.767822 - 0.0212492 \ 6.3669];$$
 (7)

$$[0.7599190.015194\ 6.38401] - [0.726977\ -0.00749985\ 6.38692]$$

(8)

(9) 4/26

such that

cloth_vec

$$VecT = [-0.0079 \ 0.0061 \ 0.0171 \ 0.0329 \ -0.0077 \ -0.0029];$$
 (10)

$$VecR = [-0.0083 \ 0.0041 \ 0.0173 \ 0.0347 \ -0.0054 \ -0.0025];$$
 (11)

(12)

where the first 3 entries of VecR is the vector $\mathbf{u_1}$ and the last 3 entries of VecR is the vector $\mathbf{u_2}$. VecT analogiously.

cloth_eig_2D

we use here Eigen :: Map to transform the vector VecT and VecR to 2 * 2 2D deformation gradient \mathbf{F} .

$$\mathbf{F} = \begin{bmatrix} -0.0083 & 0.0347 \\ 0.0041 & -0.0054 \end{bmatrix} \begin{bmatrix} -0.0079 & 0.0329 \\ 0.0061 & -0.0077 \end{bmatrix}^{-1}$$
(13)

Sikang Yan (TUK) Short title May 5, 2019 6/26

hence the F has a rotation information R and a stretch information U,

$$F = RU. (14)$$

we use $\mathbf{F}^T\mathbf{F}$ to eliminate the ratotion information to obtain det $\mathbf{R}=1$

$$\mathbf{F}^{T}\mathbf{F} = (\mathbf{R}\mathbf{U})^{T}\mathbf{R}\mathbf{U} \tag{15}$$

$$=\mathbf{U}^{T}\mathbf{R}^{T}\mathbf{R}\mathbf{U} \tag{16}$$

$$=\mathbf{U}^2\tag{17}$$

$$=\mathbf{C} \tag{18}$$

and using decomposition, if we have the form

$$\mathbf{C} = \lambda_1^2 \mathbf{v}_1 \mathbf{v}_1^T + \lambda_2^2 \mathbf{v}_2 \mathbf{v}_2^T \tag{19}$$

then we could obtain the **U** by applying

$$\mathbf{U} = \lambda_1 \mathbf{v}_1 \mathbf{v}_1^T + \lambda_2 \mathbf{v}_2 \mathbf{v}_2^T \tag{20}$$

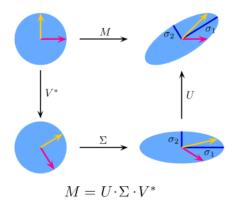


Figure: Singular Value Decomposition SVD

the main backdraw of Rohmer et al. is that this is only applied for 2D problem, thus we need a new algorithm, which can also take the consideration for the vertical deformation. Therefore, the *Kabisch Algorithm* is introduced.

Kabisch Algorithm

Let ${\bf P}$ denotes the points set of template frame, and ${\bf Q}$ denotes the points set of reference frame. The *optimal rotation matrix* ${\bf R}$ can be calculted as

$$\mathbf{R} = \mathbf{V} \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & d \end{bmatrix} \mathbf{U}^{T}$$
 (21)

where \mathbf{V} and \mathbf{U} and the SVD of cross-covariance matrix \mathbf{H} , which is determined by

Theorem (cross-covariance matrix)

$$\mathbf{H} = \mathbf{P}^{T} \mathbf{Q} \tag{22}$$

and $d = \det \mathbf{V} \mathbf{U}^T$

The matrix ${\bf H}$ is derived from the *orthogonal Procrustes problem*[?]. It is defined as the least-squares problem of transforming a given matrix ${\bf P}$ into a given matrix ${\bf Q}$ by an orthogonal transformation matrix ${\bf R}$, such that the sums of squares of the residual matrix ${\bf E}=\Omega{\bf P}-{\bf Q}$ is a minimum

$$\mathbf{R} = \underset{\Omega}{\operatorname{arg \, min}} \| \mathbf{\Omega} \mathbf{P} - \mathbf{Q} \|_{F} \quad \text{subject to} \quad \mathbf{\Omega}^{T} \mathbf{\Omega} = \mathbf{I}, \tag{23}$$

where $\|\cdot\|_F$ is the Frobenius norm. This problem is equivalent to find the nearest orthogonal matrix \mathbf{R} to a given matrix $\mathbf{H} = \mathbf{P}^T \mathbf{Q}$ [?], which most closely maps \mathbf{P} to \mathbf{Q} . Thus, we use \mathbf{H} to approximate the deformation gradient \mathbf{F} in Eq. (??)

$$\widetilde{\mathbf{F}} = \mathbf{H}.$$
 (24)

The cross-covariance matrix discribe the covariance of one process with the other at pairs of time points and measure of similarity. We use therefore the cross-covariance matrix ${\bf H}$ to approximate our deformation gradient ${\bf F}$.

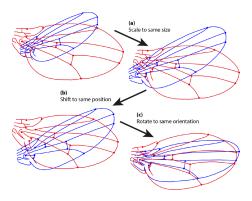


Figure: Procrustes superimposition

Sikang Yan (TUK) Short title May 5, 2019 11/26

Let i be the all index set of the nearst vertice of vertex I in the template frame and \bar{i} be the all index set of the nearst vertice of vertex I in the template frame. Process define

$$\mathbf{P} = \begin{bmatrix} \vec{x}_1 \ \vec{y}_1 \ \vec{z}_1 \\ \vec{x}_2 \ \vec{y}_2 \ \vec{z}_2 \\ \vdots \\ \vec{x}_N \ \vec{y}_N \ \vec{z}_N \end{bmatrix} \quad 1, 2, \dots, N \in i$$
 (25)

$$\mathbf{Q} = \begin{bmatrix} \overline{\vec{x}}_1 & \overline{\vec{y}}_1 & \overline{\vec{z}}_1 \\ \overline{\vec{x}}_2 & \overline{\vec{y}}_2 & \overline{\vec{z}}_2 \end{bmatrix} \quad 1, 2, \dots, N \in \overline{i}$$

$$(26)$$

and we apply to obtain the deformation gradient \mathbf{F} of vertex I

$$\mathbf{F} = \mathbf{P}^{T} \mathbf{Q} \tag{27}$$

Sikang Yan (TUK)

Short title

May 5, 2019

12/26

Whereas the deformation gradient measures the local deformation, the spacial velocity gradient L describes the rate of deformation, given by

$$\mathbf{L} = \operatorname{grad} \mathbf{v} = \dot{\mathbf{F}} \mathbf{F}^{-1}, \tag{28}$$

where v denotes the *velocity* of the material point X, and F denotes the material time derivative of deformation gradient **F**.

Analogically, we apply the polar decomposition on the spacial velocity gradient L[?], and obtain

$$\mathbf{L} = \mathbf{D} + \mathbf{W}. \tag{29}$$

Thus, we could decompose the tensor L into its symmetric part D and skew-symmetric part W

$$\mathbf{D} = \frac{1}{2} (\mathbf{L} + \mathbf{L}^T), \tag{30}$$

$$\mathbf{W} = \frac{1}{2} (\mathbf{L} - \mathbf{L}^T). \tag{31}$$

$$\mathbf{W} = \frac{1}{2} (\mathbf{L} - \mathbf{L}^T). \tag{31}$$

where **D** is called the *rate of strain tensor* and **W** is called the *rate of* rotation tensor.

Assuming $d\mathbf{x}$ is a material line element in the current configuration, the rate of change of its length $\dot{\epsilon}_{ii}$ and angle $\dot{\gamma}_{ii}$ is measured by means of **D**[?].

$$\dot{\epsilon}_{ii} = \mathbf{e}_i \mathbf{D} \mathbf{e}_i = D_{ii} \tag{32}$$

$$\dot{\gamma}_{ij} = 2\mathbf{e}_i \mathbf{D} \mathbf{e}_j = D_{ij} \tag{33}$$

where D_{ii} are the ij-entries of **D**. Additionally, if **D** has the same base $\mathbf{e_1}, \mathbf{e_2}, \mathbf{e_3}$ as in eq.(20), than

$$D_{11} = \frac{\dot{\lambda}_1}{\lambda_1}$$

$$D_{22} = \frac{\dot{\lambda}_2}{\lambda_3}$$

$$D_{33} = \frac{\dot{\lambda}_2}{\lambda_3}$$

$$(34)$$

$$(35)$$

$$D_{22} = \frac{\lambda_2}{\lambda_3} \tag{35}$$

$$D_{33} = \frac{\dot{\lambda}_2}{\lambda_3} \tag{36}$$

May 5, 2019

14 / 26

from 0-2 EigNorm1 8759 NaN, Problem:: 26278 has -0 eigenvalues, can't be squre. So I use a if(isnan) and define idx=0. add lambda1,2,3 for all, which is in debug

Sikang Yan (TUK) Short title May 5, 2019 15 / 26

save the backsite of clothes using 1-2, 1-3, 1-4. NOt much differences from colormap, need a new color map??? save lambda1 for 1,74, they are different, but slightly. lambda2 has more differences do also for lambda3

check color run application in loop consider the kr to ring 1-2 1-3 ... 1-4 2-5 ... 72-75 tensor flow add neighbor2x

Neo Hook matrial

Sikang Yan (TUK)

```
please refer \label{lem:http://web.mit.edu/abeyaratne/Volumes/RCA_Vol_II.pdf} $p68-70$ $\lambda$ and $\mathbf{D}$ relationship remedy Neighbor2x
```

Sikang Yan (TUK)

 $\label{lem:matrix_example.cpp} $$ add func to calculate D and L ,think timestep is to small 2-3 $$ $$ $$ http://www.continuummechanics.org/velocitygradient.html 0.006 1/200 $$ think should use less 2% points for KDtree $$$

19 / 26

it is because the date set has isolated points: but I thought it doesn't matter, it influence only the colormap.

thoese points can be deleted during the optimazation.

calculate D using kd-tree.

ask Ali the offical video about clothing deforamtion.

need to be emphasised that we focus on the CR(next time step)

Llbreoffice Draw A1
Dornisch Friday. monday presentation
paper send to him
add results
add smooth not finish yet. need to connect opengl and calculation

 Sikang Yan (TUK)
 Short title
 May 5, 2019
 21/26

setcolor at end correct colormap



Figure: colormap

the erro is by interpolation, how to change it? because meshlab using a unknown function? dont draw bevor calucution glMapBuffer gluPMAPBUFFER

add new reulsts using new colormap, have seen red add defalut color as pink for all vertices add smooth: problem negative values cannot be root squre... add colormap for D, based on t not on t+deltaT tried to pass calculated datas direct to opengl class -¿?, so I directly read the ply file from output. no color? didn't find the glMapBuffer.

Sikang Yan (TUK) Short title

IT is actu. a normalizeation (Rohmer) change Gamma to 1/2.5 0.1, 0.2, 0.5, 0.75, 1, 1.5, 2, 3

new evaluatet

add python for pic, need rotation

- tensor density https://www.revolvy.com/page/Tensor-density
- openFoam limited

```
visply
slerp
https:
//github.com/cmu462/Scotty3D/wiki/Linear-Blend-Skinning
```

26 / 26