

$$1 + 1 + (n+2)(2 + (n-1)/2 + 1)(6)$$

$$3n^2 + 21n + 33$$

$$3n^2 + 21n + 33 \leq O(n^3)$$

$$c = 57, n_0 = 1 \Rightarrow 57 \leq 57$$

Therefore it belongs to $O(n^3)$ by def

Pseudocode

(i) Alternate Algorithm

sorted_disk sort_alternate(disk-state &begorSwap) {
 int numberSwap = 0
 disk-state state = begorSwap

for (int i = 0; i < Size + 1; i++)

$(n-1)/2 + 1$

1
3
1

$n-2/2 + 1$

1
3
1
1

1

```

{
    if (i % 2 == 0)
    {
        for (int currentIndex = 0; currentIndex < Size - 1; currentIndex = currentIndex + 2)
        {
            if (state.get(currentIndex) != state.get(currentIndex + 1))
            {
                if (state.get(currentIndex) == DISK_DARK && state.get(currentIndex + 1) == DISK_LIGHT)
                {
                    swap
                    numberSwap++
                }
            }
        }
    }
    else
    {
        for (int currentIndex = 0; currentIndex < Size - 2; currentIndex = currentIndex + 2)
        {
            if (state.get(currentIndex) != state.get(currentIndex + 1))
            {
                if (state.get(currentIndex) == DISK_DARK && state.get(currentIndex + 1) == DISK_LIGHT)
                {
                    state.swap(currentIndex)
                    numberSwap++
                }
            }
        }
    }
}
return sorted_disk(disk-state(state), numberSwap)
    
```

② Lawnmower Algorithm

```

sorted - disks sort_lawnmower(const disk_state & before)
{
    int number_swap = 0
    disk_state state = before
    for (int i = 0; i < SIZE / 2; i++)
    {
        int current_index = 0
        while (current_index + 1 < Size)
        {
            if (state.get(current_index) != state.get(current_index + 1))
            {
                if (state.get(current_index) == DISK DARK && state.get(current_index + 1) == 0)
                {
                    swap(current_index)
                    number_swap++
                }
            }
            current_index++
        }
        while (current_index > 0)
        {
            if (state.get(current_index - 1) != state.get(current_index))
            {
                if (state.get(current_index) == DISK DARK && state.get(current_index - 1) == 0)
                {
                    swap(current_index - 1)
                    number_swap++
                }
            }
            current_index--
        }
    }
    return
}

```

$$3 + (((n/2) + 1) * (7n + 8) * (7n + 7))$$