

1. Merge Sort

Input: array type int not sorted

Output: array type int sorted

```

function mergeSort(array){
    declare and initialize n = length of array;
    if(n <=1) return;
    declare and initialize mid = n/2;
    declare and initialize leftArray with length = mid;
    declare and initialize rightArray with length = n - mid;
    declare and initialize type int i =0, j = 0;

    while(i <n){
        if(i < mid)
            leftArray at i = array at i;
            increment i by 1;
        else
            rightArray at j = array at i;
            increment i by 1;
            increment j by 1;
        }
        use recursive mergeSort(leftArray);
        use recursive mergeSort(rightArray);
        call funtion merge(leftArray, rightArray, array);
    }

```

$\Rightarrow O(1) + O(2^1) + O(2^2) + \dots + O(2^k)$
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Input: 3 arrays type int: leftArray, rightArray, array

Output: array (the result from merging leftArray and rightArray)

```

funtion merge(leftArray, rightArray, array){
    declare and initialize index, leftIndex, rightIndex = 0;
    declare and initialize length of leftArray = array.length/2;
    decalre and initialize length of rightArray = array.length - leftSide;

    while(leftIndex < length of leftArray && rightIndex < length of rightArray){
        if(leftArray at leftIndex < rightArray at rightIndex)
            array at index = leftArray at leftIndex;
            increment index by 1;
            increment leftIndex by 1;
        else
            array at index = rightArray at rightIndex;
            increment index by 1;
            increment rightIndex by 1;
        }

    while(leftIndex < length of leftArray)
        array at index = leftArray at leftIndex;
        increment index by 1;
        increment leftIndex by 1;
    while(rightIndex < length of rightArray){
        array at index = rightArray at rightIndex;
        increment index by 1;
        increment rightIndex by 1;
    }
}

```

$$T(n) = O(1) + 4 * (O(1) + O(2^1) + O(2^2) + \dots + O(2^k)) + 6 * (O(n/2) + O(n/4) + O(n/8) + \dots + O(2)) = O(n \log n).$$