

Introduction of Quantum Computing

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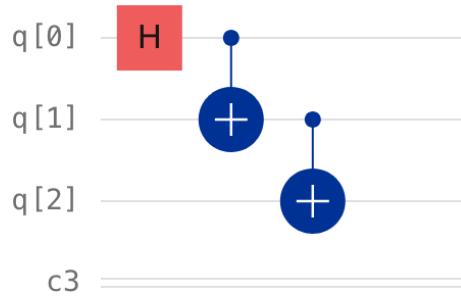
IBM Quantum Platform

Untitled circuit File Edit View Help Save file 

Operations   

H	\oplus	\oplus	\oplus	\otimes	I
T	S	Z	T^\dagger	S^\dagger	P
RZ	rz	$ 0\rangle$		•	if
\sqrt{X}	\sqrt{X}^\dagger	Y	RX	RY	RXX
RZZ	U	RCCX	RC3X		

Left alignment



IBM Quantum

Kifumi Numata



Qiskit Advocate, APAC Workforce and Education, IBM Quantum

Recent Activity:

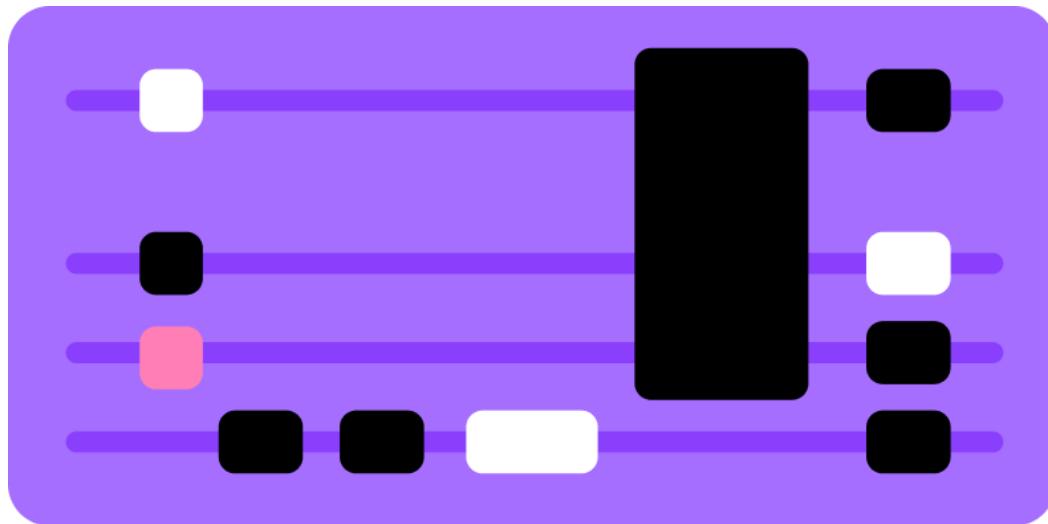
- Lectures at the University of Tokyo, etc.
- Lab creation of Qiskit Global Summer School, IBM Quantum Challenge
- Quantum Tokyo:
 - Local quantum community in Japan since 2020
- NICT Quantum Camp – Qiskit workshop since 2020
- Kawasaki Quantum Summer Camp since 2022



Introduction of Quantum Computing

- Qubits and quantum gates
- IBM Quantum Composer
- Introduction of Qiskit

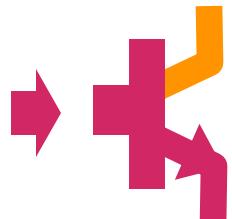
Qubits and quantum gates



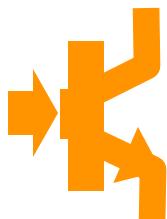
IBM Quantum

Computers perform calculations using bits.

Switch



Off



On

Bit

0

1

Character string

7

Bit string

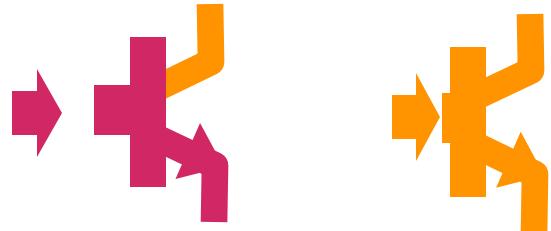
111

A

0100 0001



The bits in the computers
we always use are



either **0** or **1**

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The qubits in the quantum
computers use

both **0** and **1**
in superposition

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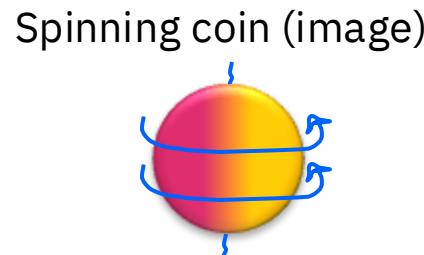


The bits in the computers
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The qubits in the quantum
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in superposition



When a measurement is made,
the state becomes either 0 or 1.

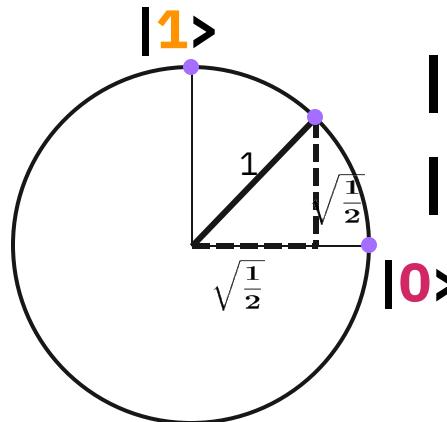
The bits in the computers
we always use are

either **0** or **1**

The qubits in the quantum
computers use

$$\alpha \times |0\rangle + \beta \times |1\rangle$$

“superposition” of $|0\rangle$ and $|1\rangle$.

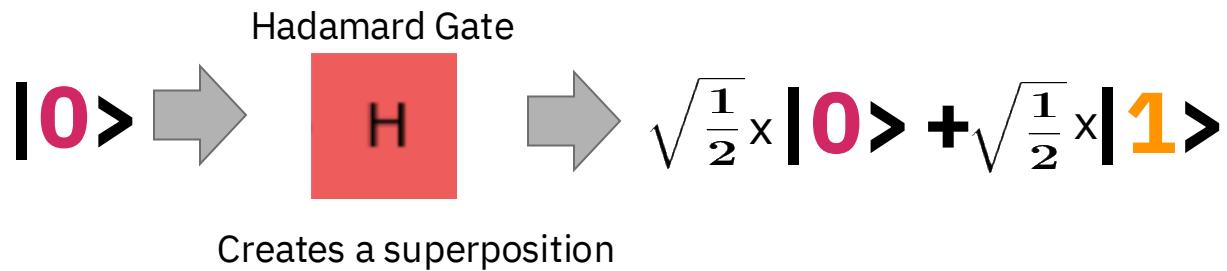


$$|0\rangle = 1 \times |0\rangle + 0 \times |1\rangle$$

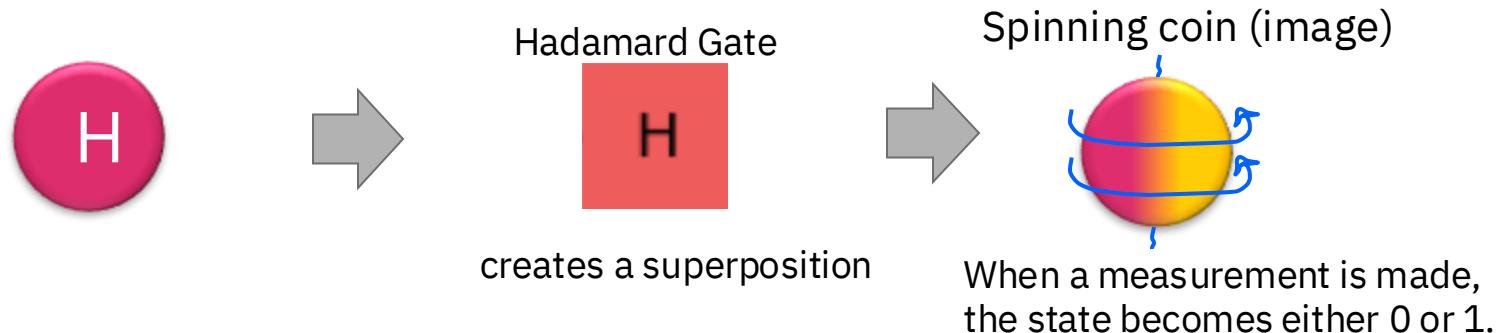
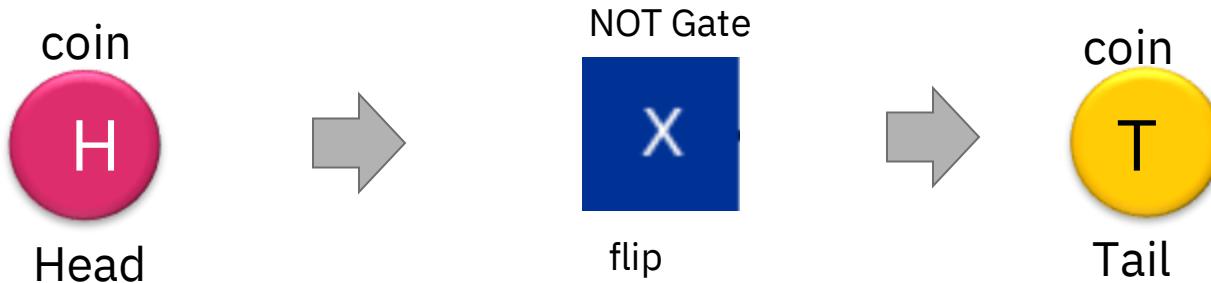
$$|1\rangle = 0 \times |0\rangle + 1 \times |1\rangle$$

$|>$ represents qubit.

The typical calculations in quantum computing



The typical calculations in quantum computing



Quantum Computers and its Mathematics

	Quantum computers	Mathematics	Computational representation
Data	Quantum states	Vector	$\begin{pmatrix} v_1 \\ \vdots \\ v_n \end{pmatrix}$: Column vector
Operation	Quantum gates (Quantum operators)	Matrix	$\begin{pmatrix} a_{11} & \cdots & a_{1n} \\ \vdots & \ddots & \vdots \\ a_{m1} & \cdots & a_{mn} \end{pmatrix}$

Single-qubit quantum state

An arbitrary quantum state can be represented as a linear combination of $|0\rangle$ and $|1\rangle$.

$$|\psi\rangle = \alpha|0\rangle + \beta|1\rangle$$

where α and β are complex numbers such that $|\alpha|^2 + |\beta|^2 = 1$.

$$|0\rangle = \begin{bmatrix} 1 \\ 0 \end{bmatrix} \quad \text{and} \quad |1\rangle = \begin{bmatrix} 0 \\ 1 \end{bmatrix}$$

Therefore, the arbitrary quantum state is also represented as

$$|\psi\rangle = \alpha \begin{bmatrix} 1 \\ 0 \end{bmatrix} + \beta \begin{bmatrix} 0 \\ 1 \end{bmatrix} = \begin{bmatrix} \alpha \\ \beta \end{bmatrix}.$$

$|\psi\rangle = \begin{bmatrix} \alpha \\ \beta \end{bmatrix}$ is also called the state vector.

Quantum Operators

Quantum states are transferred by the unitary operator U : $|\psi'\rangle = U|\psi\rangle$

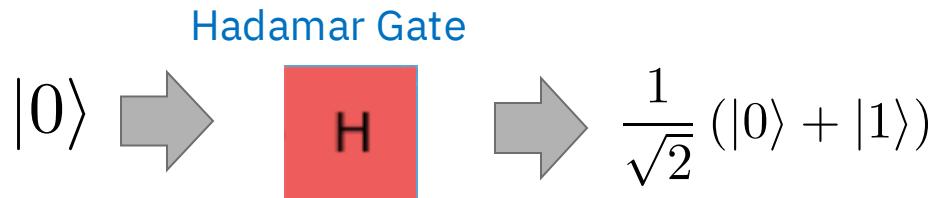


$$X = \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix},$$

$$X |0\rangle = \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix} \begin{bmatrix} 1 \\ 0 \end{bmatrix} = \begin{bmatrix} 0 \\ 1 \end{bmatrix} = |1\rangle$$

Quantum Operators

Quantum states are transferred by the unitary operator U : $|\psi'\rangle = U|\psi\rangle$

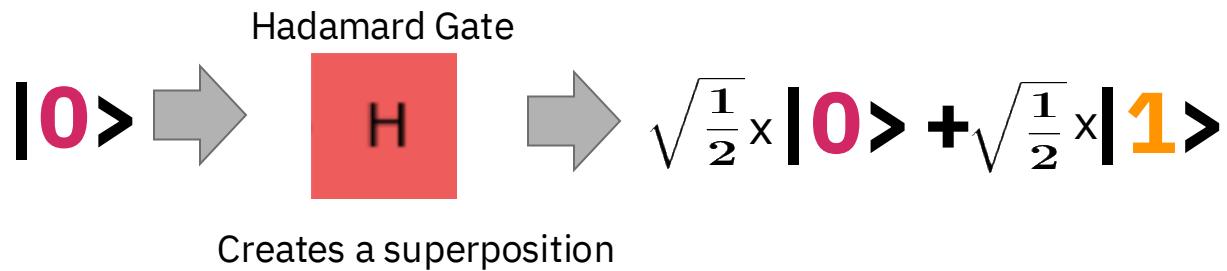


$$H = \frac{1}{\sqrt{2}} \begin{bmatrix} 1 & 1 \\ 1 & -1 \end{bmatrix},$$

$$H|0\rangle = \frac{1}{\sqrt{2}} \begin{bmatrix} 1 & 1 \\ 1 & -1 \end{bmatrix} \begin{bmatrix} 1 \\ 0 \end{bmatrix} = \frac{1}{\sqrt{2}} \begin{bmatrix} 1 \\ 1 \end{bmatrix} = \frac{1}{\sqrt{2}} \left(\begin{bmatrix} 1 \\ 0 \end{bmatrix} + \begin{bmatrix} 0 \\ 1 \end{bmatrix} \right) = \frac{1}{\sqrt{2}}(|0\rangle + |1\rangle)$$

$|0\rangle$ and $|1\rangle$ are measured with a 1/2 chance

The typical calculations in quantum computing



Hands-on: IBM Quantum Composer

<https://quantum.cloud.ibm.com/composer>

Short URL: ibm.biz/cmpsr25

The screenshot shows the IBM Quantum Platform interface. At the top, there's a navigation bar with 'IBM Quantum Platform' and a search icon. Below it is a menu bar with 'Untitled circuit', 'File', 'Edit', 'View', 'Help', 'Save file', 'Set up and run', and a gear icon.

The main area features a quantum circuit editor with four qubits labeled q[0] through q[3]. A toolbar above the circuit includes icons for various operations like H, T, RZ, and measurements. To the right of the circuit, there's an 'Inspect' button and a 'Left alignment' dropdown. The circuit currently contains an 'if' block on q[2].

On the far right, there's a code editor window titled 'OpenQASM 2.0' showing the corresponding QASM code:

```
1 OPENQASM 2.0;
2 include "qelib1.inc";
3
4 qreg q[4];
5 creg c[4];
6
7
```

Single-qubit circuit

The screenshot shows the Qiskit Terra interface. At the top, there's a toolbar with 'Untitled circuit', 'File', 'Edit', 'View', and a 'Visual' dropdown. Below the toolbar is a header with 'Operations', 'Left alignment', and an 'Inspect' toggle. On the left, there's a palette with a search bar and a grid of quantum gate icons. The main area shows a circuit with four qubits (q[0], q[1], q[2], q[3]) and one classical register (c4). The circuit currently has three gates: H on q[0], T on q[1], and RZ on q[2]. A red arrow points to the trash icon next to q[1].

1. Click q[1] and click a trash icon to clear it.
2. Repeat that to leave only q[0] to prepare a single qubit circuit.

[Open in Quantum Lab](#)

```
1 from qiskit import
2   QuantumCircuit
3 from numpy import
4
5 qreg_q = QuantumRe
6 creg_c = Classical
7 circuit = QuantumC
```

Single-qubit circuit

The screenshot shows the IBM Quantum Composer interface. On the left, the 'Quantum gates' panel displays a grid of quantum gate icons, with a red circle highlighting the Hadamard gate (H). A red arrow points from this icon towards the central 'Quantum Circuits' workspace. The central workspace shows a circuit diagram with a single qubit register q[0] and a classical register c4. A red arrow points from the circuit diagram towards the 'Qiskit code' panel on the right. The 'Qiskit code' panel contains the following auto-generated Python code:

```
1  from qiskit import QuantumRegister, ClassicalRegister,  
2      QuantumCircuit  
3  from numpy import pi  
4  
4  qreg_q = QuantumRegister(1, 'q')  
5  creg_c = ClassicalRegister(4, 'c')  
6  circuit = QuantumCircuit(qreg_q, creg_c)  
7  
8
```

Drag and drop the quantum gate with your mouse to create a quantum circuit.
On the right side, the code for Qiskit is auto-generated.

1. X gate (NOT gate)

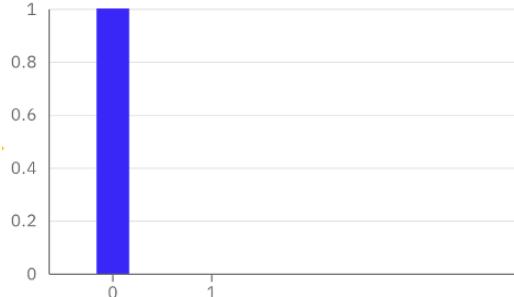
Try to build the circuits shown below.
And, let's check the changes in the bar graph.



Set the lower left graph
to “Statevector” of blue
bar.



The initial state is $|0\rangle$

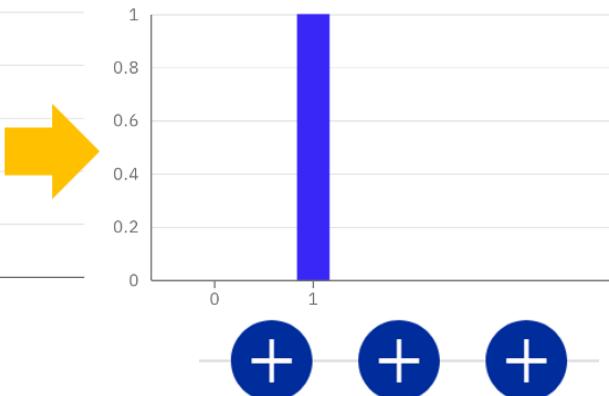
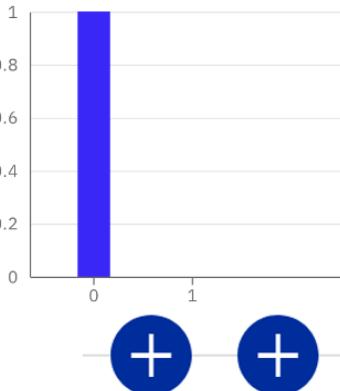
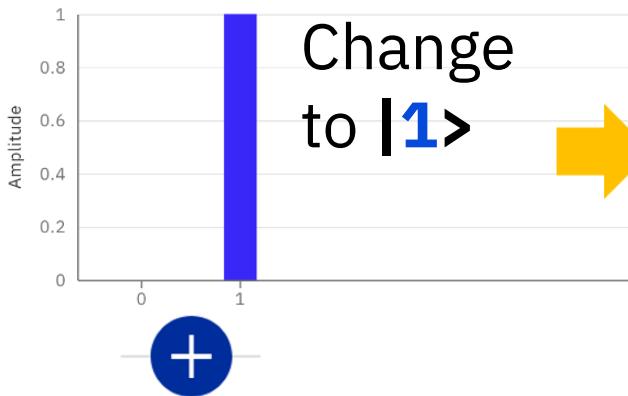


The bars in a statevector graph are the value of α and β , probability amplitude, of a quantum state, $\alpha|0\rangle + \beta|1\rangle$.

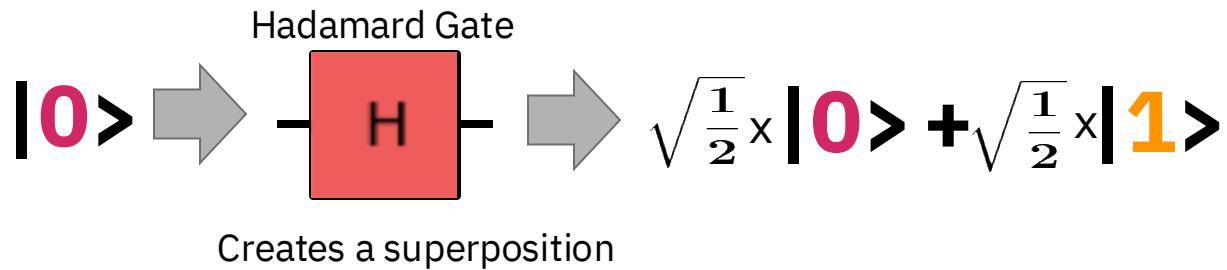
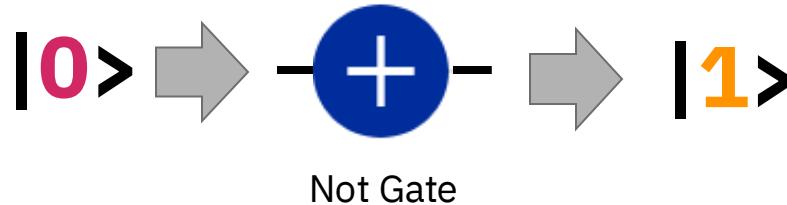
$$|0\rangle = 1 \times |0\rangle + 0 \times |1\rangle$$

$$|1\rangle = 0 \times |0\rangle + 1 \times |1\rangle$$

Change
to $|1\rangle$

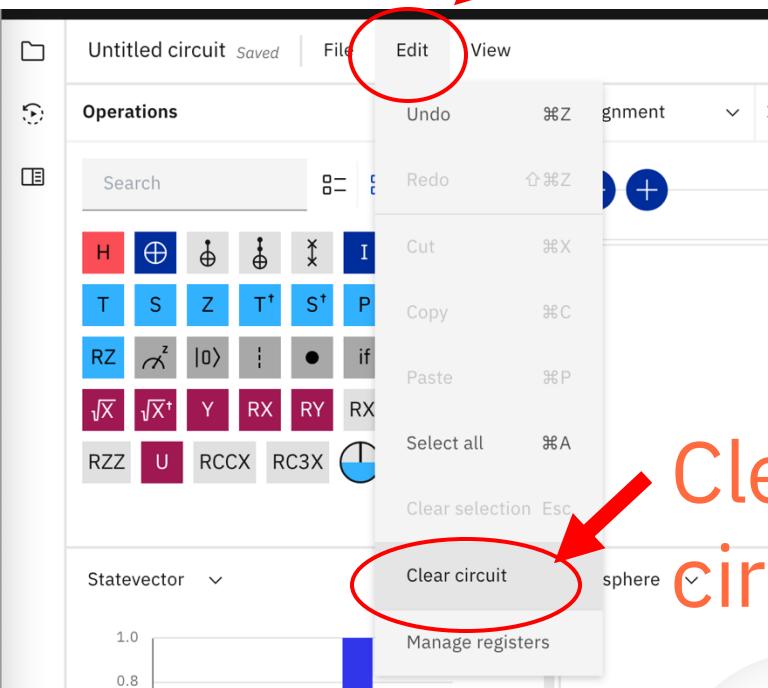


The typical calculations in quantum computing

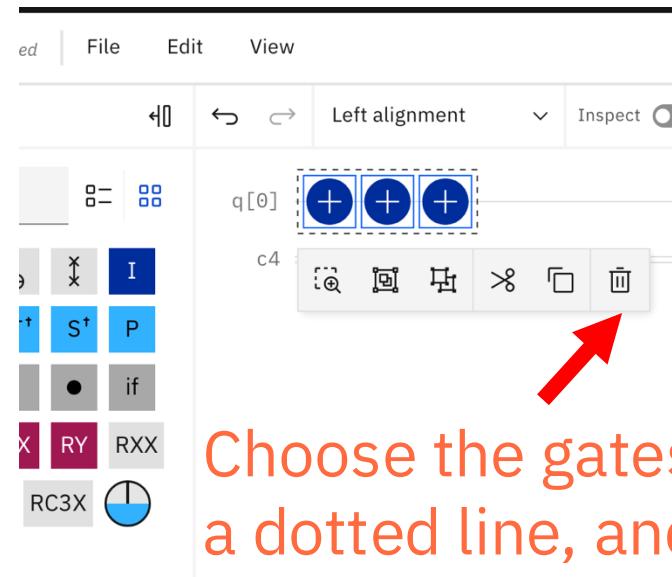


Remove the gates you put

Edit



OR



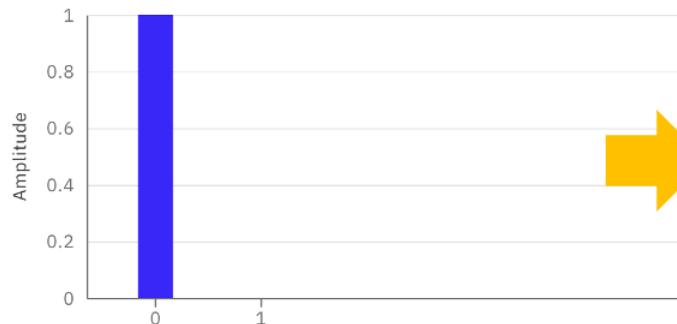
Clear
circuit

Choose the gates with
a dotted line, and
click the trash icon.

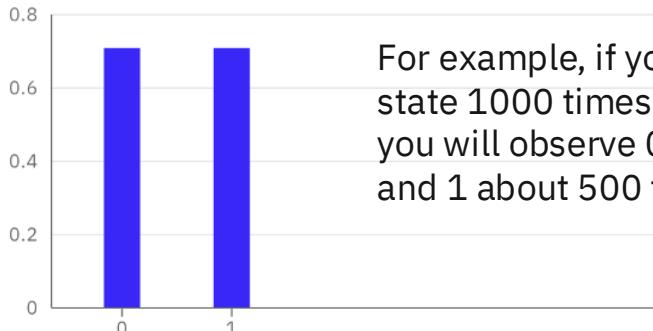
2. H gate

Try to build the circuits shown below. Let's check the changes in the bar graph.

2-1)



Superposition



For example, if you create the same state 1000 times and measure them, you will observe 0 about 500 times and 1 about 500 times.

$$|0\rangle = 1 \times |0\rangle + 0 \times |1\rangle$$

$$\begin{aligned} & 0.707 \times |0\rangle + 0.707 \times |1\rangle \\ &= \frac{1}{\sqrt{2}} \times |0\rangle + \frac{1}{\sqrt{2}} \times |1\rangle \end{aligned}$$

2. H gate

Try to build the circuits shown below. Let's check the changes in the bar graph.

2-1)



2-2)



2-3)



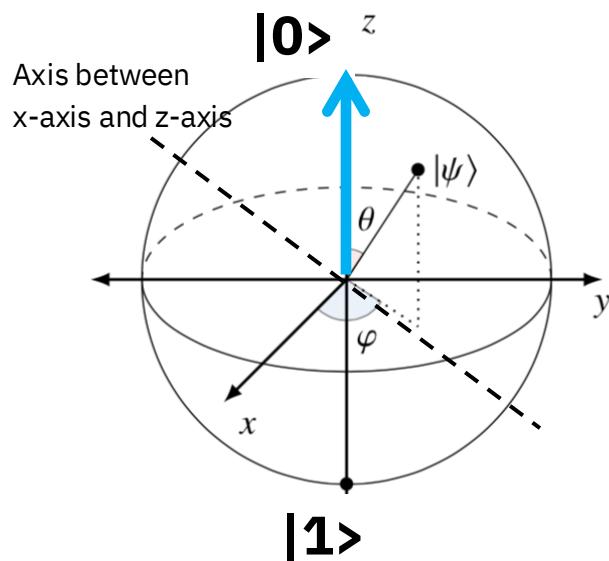
The typical calculations in quantum computing

$$|0\rangle \xleftarrow{\text{H}} \sqrt{\frac{1}{2}}|0\rangle + \sqrt{\frac{1}{2}}|1\rangle$$



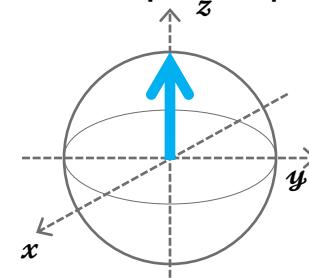
$$|1\rangle \xleftarrow{\text{H}} \sqrt{\frac{1}{2}}|0\rangle - \sqrt{\frac{1}{2}}|1\rangle$$

Bloch sphere

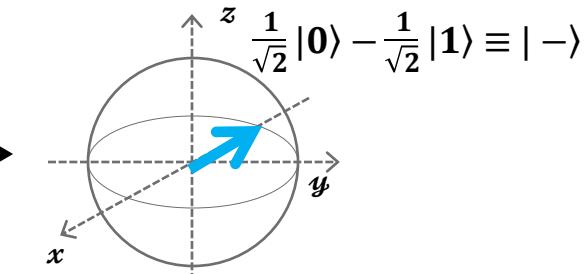
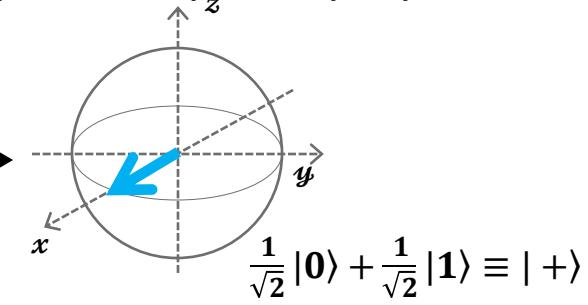


A pure quantum state is a vector pointing from the center to a point on the sphere of radius 1.

North pole: $|0\rangle$

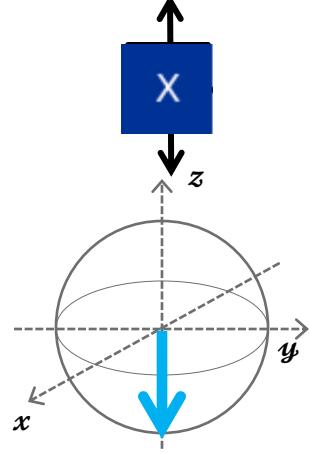


Equator: equal superposition

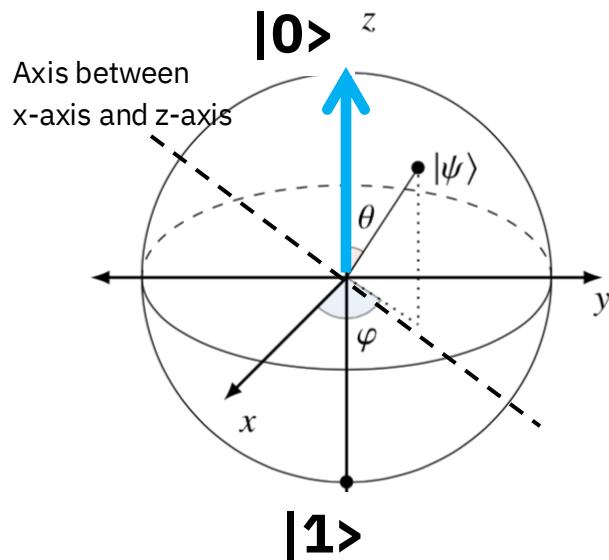


South pole: $|1\rangle$

South pole: $|1\rangle$

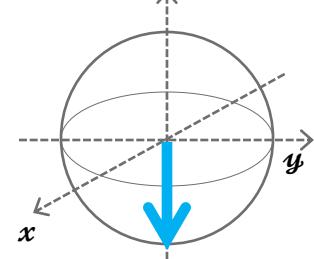
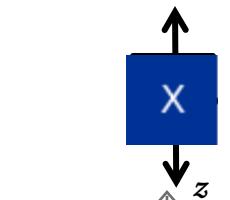
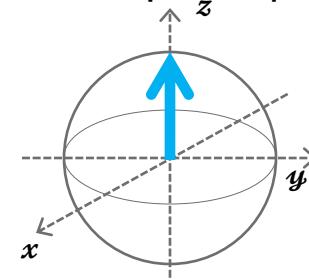


Bloch sphere



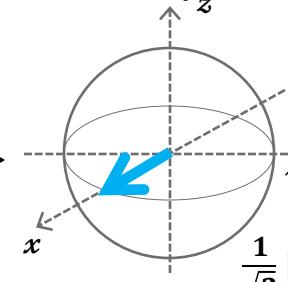
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North pole: $|0\rangle$

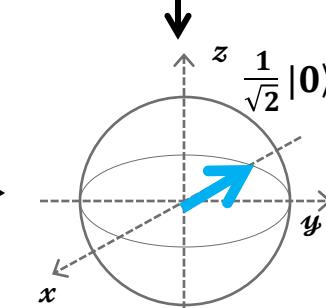
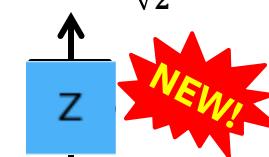


South pole: $|1\rangle$

Equator: equal superposition



$$\frac{1}{\sqrt{2}}|0\rangle + \frac{1}{\sqrt{2}}|1\rangle \equiv |+\rangle$$



$$\frac{1}{\sqrt{2}}|0\rangle - \frac{1}{\sqrt{2}}|1\rangle \equiv |- \rangle$$

The typical calculations in quantum computing

$$\begin{array}{ccc} |\mathbf{0}\rangle & \xleftarrow{\text{H}} & \sqrt{\frac{1}{2}}|\mathbf{0}\rangle + \sqrt{\frac{1}{2}}|\mathbf{1}\rangle \\ & & \\ \begin{matrix} \uparrow \\ + \\ \downarrow \end{matrix} & & \begin{matrix} \uparrow \\ \text{Z} \\ \downarrow \end{matrix} \text{ NEW!} \\ |\mathbf{1}\rangle & \xleftarrow{\text{H}} & \sqrt{\frac{1}{2}}|\mathbf{0}\rangle - \sqrt{\frac{1}{2}}|\mathbf{1}\rangle \end{array}$$

3. Z gate

Try to build the circuits shown below. Let's check the changes in the bar graph.

3-1)



3-2)



3-3)



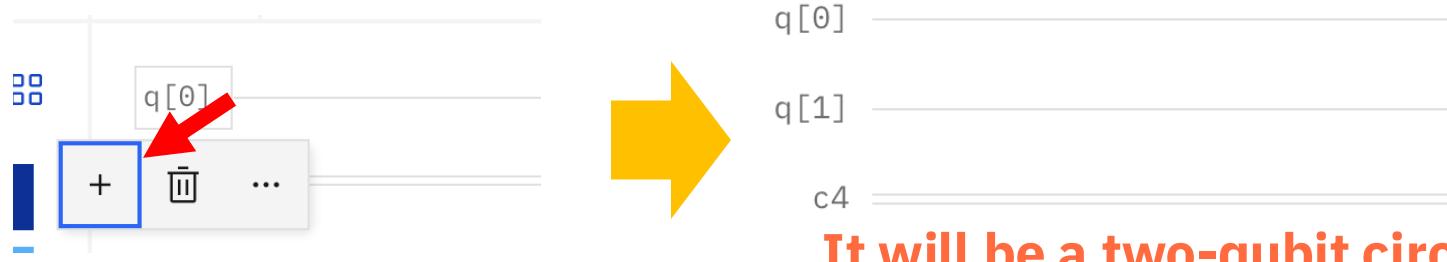
The typical calculations in quantum computing



Flips the sign of 1

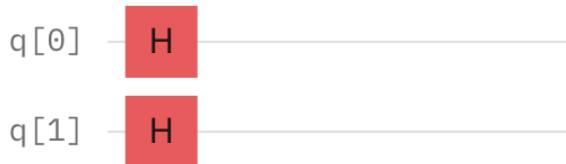
4. Quantum superposition

Click q[0] and then click the "+" icon to prepare a two qubit circuit.



Try to build the circuits shown below. Let's check the changes in the bar graph.

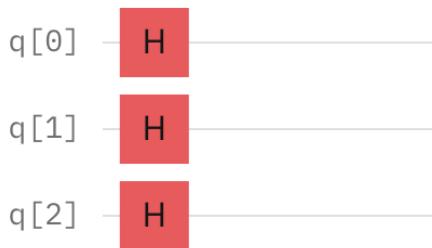
4-1)



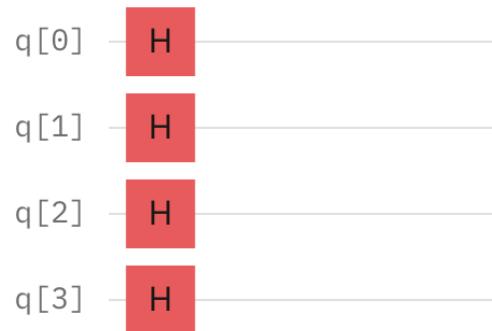
Click q[1] and then click the "+" icon to see the superposition state at 3-qubit, 4-qubit, and 5-qubit.



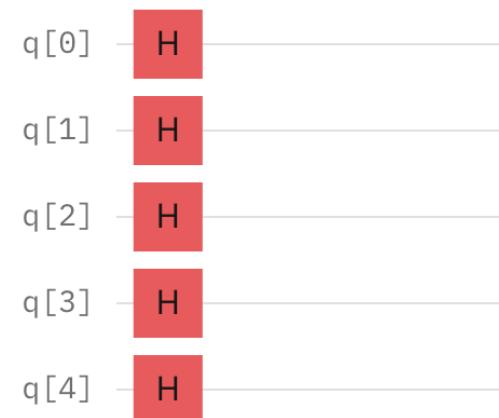
4-2)

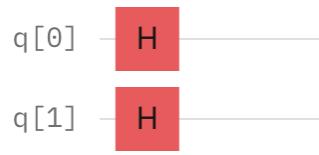
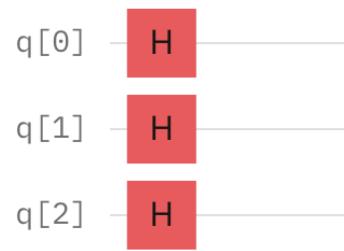
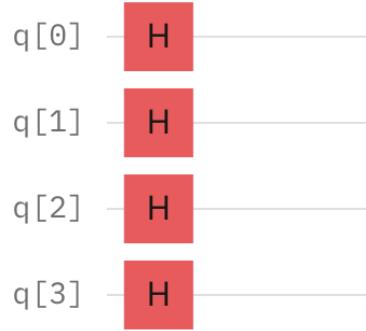
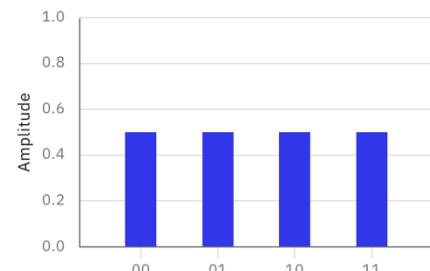
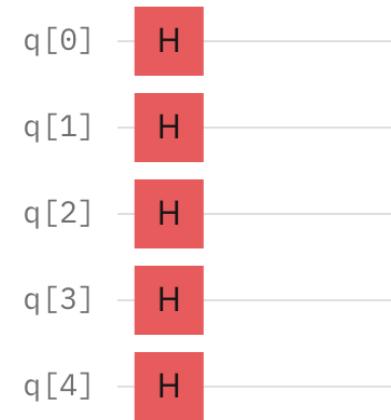


4-3)

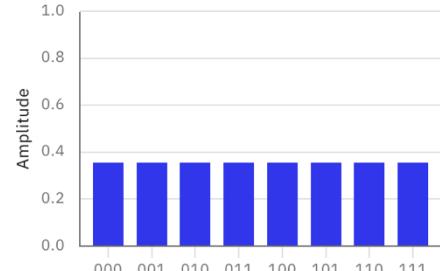


4-4)

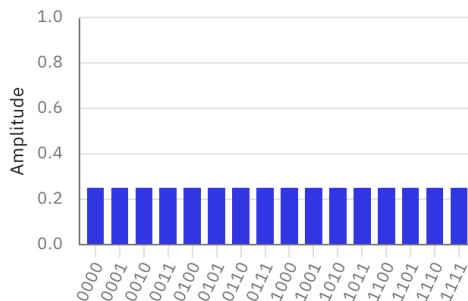


4-1)**4-2)****4-3)****4-4)**

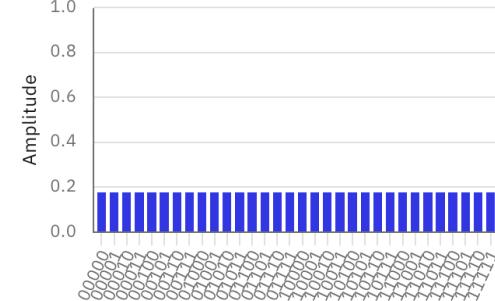
4 states



8 states



16 states

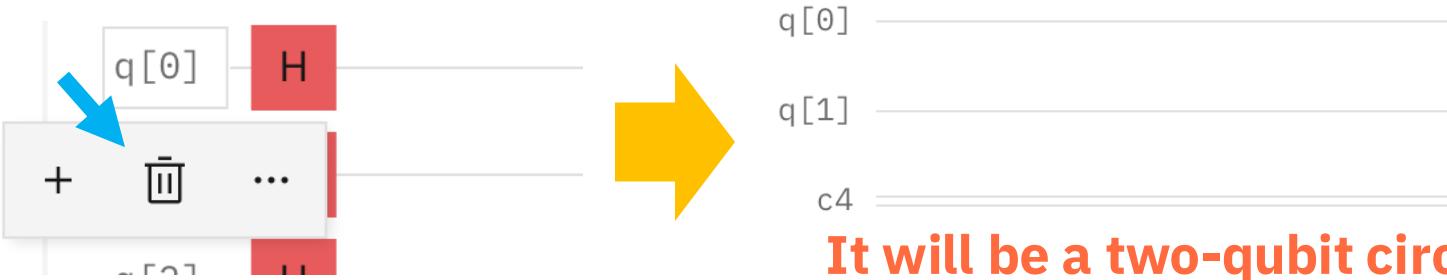


32 states

As the number of qubits (n) increases, we can see that the quantum state doubles to 2^n .

Go back to two qubit circuit again

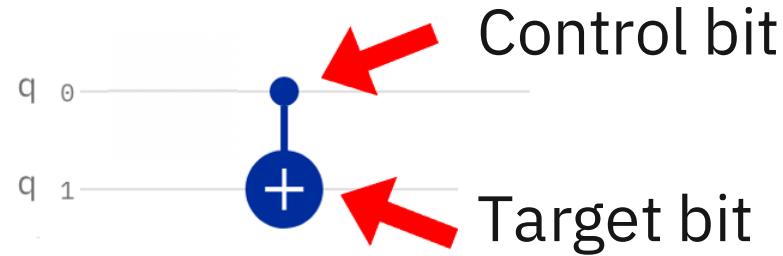
Click q[0], then click the trash icon, and repeat it to prepare the two qubit circuit.



It will be a two-qubit circuit

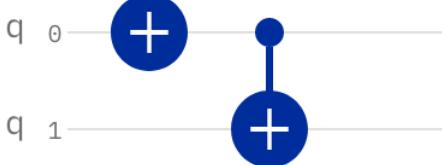
5. CNOT Gate (Control X-Gate)

CNOT gate flips the target bit only if the control bit is 1.



input		output	
Target bit	Control bit	Target bit	Control bit
0	0	0	0
1	0	1	0
0	1	1	1
1	1	0	1

5-1)



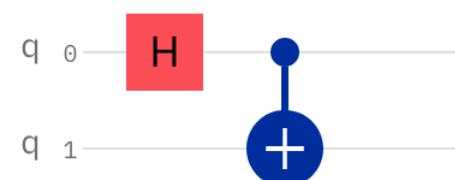
5-2)



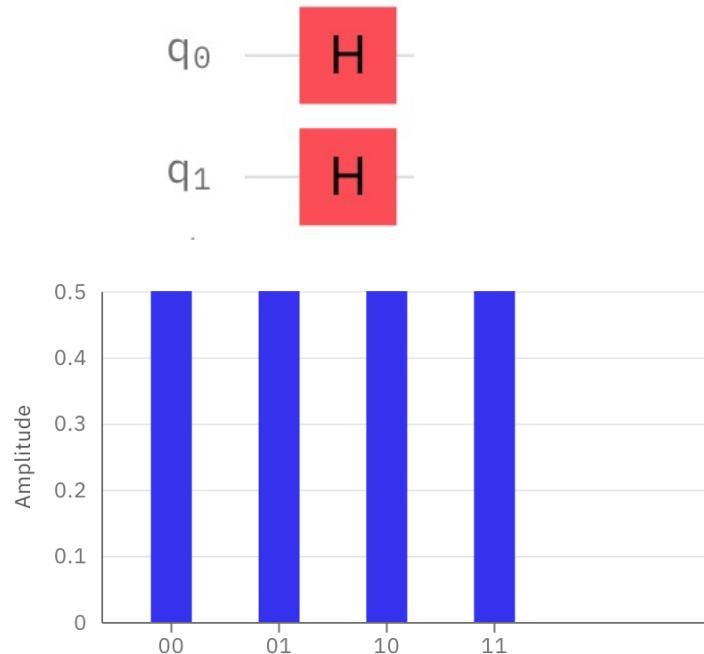
5-3)



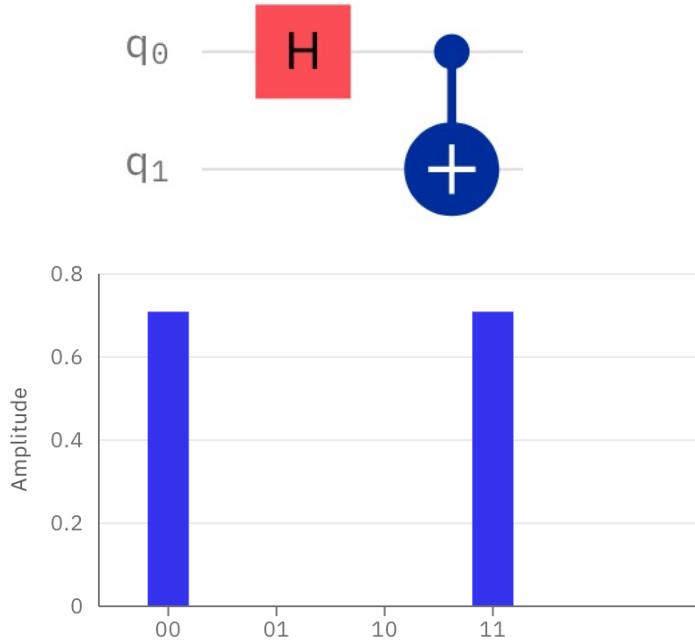
5-4)



Quantum superposition

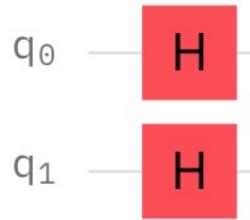


Quantum entanglement



CNOT gate makes entanglement.

Quantum superposition



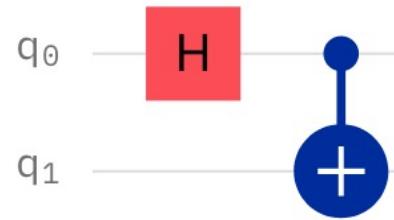
0 0 ... 25%

0 1 ... 25%

1 0 ... 25%

1 1 ... 25%

Quantum entanglement



0 0 ... 50%

0 1 ... 0%

1 0 ... 0%

1 1 ... 50%

If we know that one of the qubits is 0, then the other is also 0.

EPR Pair (Einstein-Podolsky-Rosen Pair)

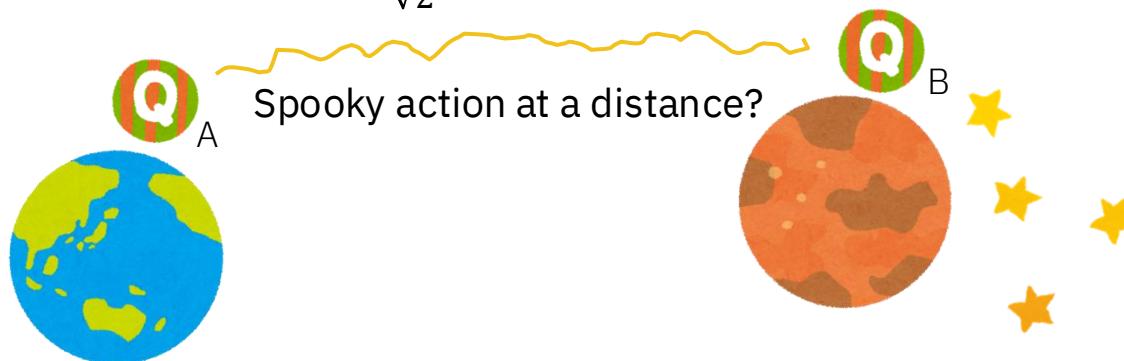
$$\text{EPR pair: } |\psi\rangle = \frac{1}{\sqrt{2}}(|00\rangle + |11\rangle)$$

More generally, two quantum states that are entangled are called **EPR (Einstein-Podolsky-Rosen) pair** after the EPR paradox.

EPR paradox: Suppose that quantum entangled pair are separated by a distance and one of them is observed.

What happens?

$$|\psi_{AB}\rangle = \frac{1}{\sqrt{2}}(|0_A 0_B\rangle + |1_A 1_B\rangle)$$



MAY 15, 1935 PHYSICAL REVIEW VOLUME 47

DESCRIPTION OF PHYSICAL REALITY

This investigation was carried out under the supervision of Professor C. Born, and I wish to thank him for his invaluable advice and assistance so freely given. I also take this opportunity to acknowledge the award of a Fellowship by the Royal Society of Canada, and to thank the University of Wisconsin and the Department of Physics for the privilege of working here.

"Can Quantum-Mechanical Description of Physical Reality Be Considered Complete?"

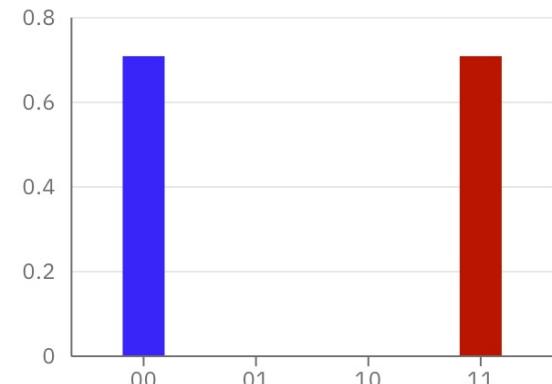
A. EINSTEIN, B. PODOLSKY AND N. ROSEN, Institute for Advanced Study, Princeton, New Jersey
(Received March 25, 1935)

In a complete theory there is an element corresponding to each element of reality. A sufficient condition for the quantum mechanics is not complete or (2) these two quantities cannot have simultaneous reality. Consideration of a physical quantity is the possibility of predicting it with certainty, without disturbing the system. In the problem of making predictions concerning a system on the basis of measurements made on another system that de or th "Can Quantum-
Mechanical
Description of
Physical Reality Be
Considered
Complete?"
form of experiment and measurement. It is the second question that we wish to consider here, as applied to quantum mechanics. seems to us that this criterion, while far from exhausting all possible ways of recognizing a physical reality, at least provides us with one

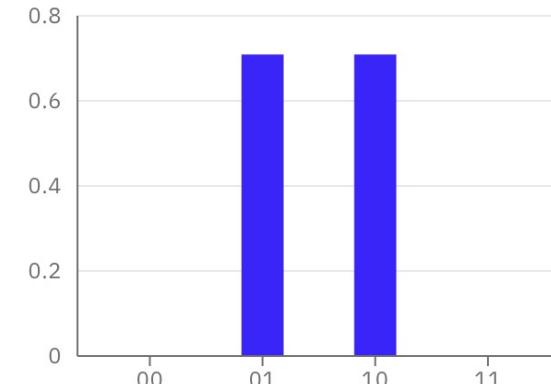
Advanced exercise

Let's build the entangled states of two qubits. There are many ways to make it.

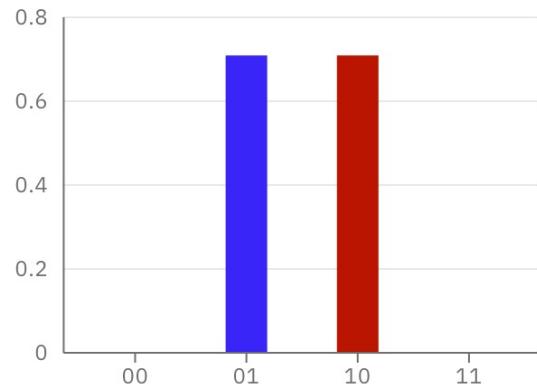
$$(1) \quad \frac{1}{\sqrt{2}}(|00\rangle - |11\rangle)$$



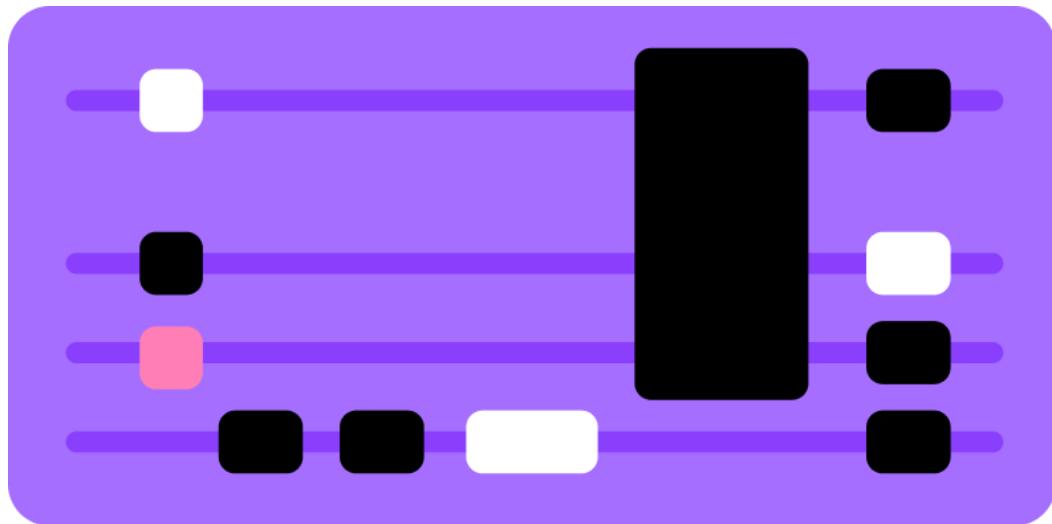
$$(2) \quad \frac{1}{\sqrt{2}}(|01\rangle + |10\rangle)$$



$$(3) \quad \frac{1}{\sqrt{2}}(|01\rangle - |10\rangle)$$



Before moving to Qiskit



IBM Quantum

Measurement

Measurement is forcing the qubit's state

$$\alpha|0\rangle + \beta|1\rangle \quad s.t. |\alpha|^2 + |\beta|^2 = 1$$

to $|0\rangle$ or $|1\rangle$ by observing it, where

$|\alpha|^2$ is the probability we will get $|0\rangle$ when we measure.

$|\beta|^2$ is the probability we will get $|1\rangle$ when we measure. (Born rule)

So, α and β are called probability amplitudes.

For example,

- $\frac{\sqrt{2}}{2}|0\rangle + \frac{\sqrt{2}}{2}|1\rangle$ has an equal probability of becoming $|0\rangle$ or $|1\rangle$
- $\frac{\sqrt{3}}{2}|0\rangle - \frac{1}{2}i|1\rangle$ has a 75% chance of becoming $|0\rangle$.

Typical single-qubit gates

Pauli gates: $X = \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}$, $Y = \begin{bmatrix} 0 & -i \\ i & 0 \end{bmatrix}$, $Z = \begin{bmatrix} 1 & 0 \\ 0 & -1 \end{bmatrix}$

Other typical single-qubit gates:

$$H = \frac{1}{\sqrt{2}} \begin{bmatrix} 1 & 1 \\ 1 & -1 \end{bmatrix}; \quad S = \begin{bmatrix} 1 & 0 \\ 0 & i \end{bmatrix}; \quad T = \begin{bmatrix} 1 & 0 \\ 0 & \exp(i\pi/4) \end{bmatrix}.$$

$$R_x(\theta) \equiv e^{-i\theta X/2} = \cos \frac{\theta}{2} I - i \sin \frac{\theta}{2} X = \begin{bmatrix} \cos \frac{\theta}{2} & -i \sin \frac{\theta}{2} \\ -i \sin \frac{\theta}{2} & \cos \frac{\theta}{2} \end{bmatrix}$$

$$R_y(\theta) \equiv e^{-i\theta Y/2} = \cos \frac{\theta}{2} I - i \sin \frac{\theta}{2} Y = \begin{bmatrix} \cos \frac{\theta}{2} & -\sin \frac{\theta}{2} \\ \sin \frac{\theta}{2} & \cos \frac{\theta}{2} \end{bmatrix}$$

$$R_z(\theta) \equiv e^{-i\theta Z/2} = \cos \frac{\theta}{2} I - i \sin \frac{\theta}{2} Z = \begin{bmatrix} e^{-i\theta/2} & 0 \\ 0 & e^{i\theta/2} \end{bmatrix}.$$

Notation of multiple systems

- A one-qubit system can be in the superposition of **two** states:

$$|0\rangle, |1\rangle$$

- A two-qubit system can be in the superposition of **2^2** states:

$$|0\rangle \otimes |0\rangle, |1\rangle \otimes |0\rangle, |0\rangle \otimes |1\rangle, |1\rangle \otimes |1\rangle$$

- An n-qubit system can be in the superposition of **2^n** states:

$$|0\rangle_{n-1} \otimes \cdots \otimes |0\rangle_0, |0\rangle_{n-1} \otimes \cdots \otimes |0\rangle_1 \otimes |1\rangle_0, \dots, |1\rangle_{n-1} \otimes \cdots \otimes |1\rangle_0$$

Notation of multiple systems

- A one-qubit system can be in the superposition of **two** states:

$$|0\rangle, |1\rangle$$

- A two-qubit system can be in the superposition of **2^2** states:

$$|0\rangle\otimes|0\rangle, |1\rangle\otimes|0\rangle, |0\rangle\otimes|1\rangle, |1\rangle\otimes|1\rangle$$

$$\equiv |0\rangle|0\rangle, |1\rangle|0\rangle, |0\rangle|1\rangle, |1\rangle|1\rangle$$

$$\equiv |00\rangle, |10\rangle, |01\rangle, |11\rangle$$

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Notation of multiple systems

- A one-qubit system can be in the superposition of **two** states:

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- An n-qubit system can be in the superposition of **2^n** states:

$$|0\rangle_{n-1}\otimes\cdots\otimes|0\rangle_0, |0\rangle_{n-1}\otimes\cdots\otimes|0\rangle_1\otimes|1\rangle_0, \dots, |1\rangle_{n-1}\otimes\cdots\otimes|1\rangle_0$$

$$\equiv |00\cdots 0\rangle, |0\cdots 01\rangle, \dots, |1\cdots 1\rangle$$

Tensor products

Tensor product of two vectors: multiply the right-hand vector by each component of the left-hand vector.

$$\begin{pmatrix} v_1 \\ \vdots \\ v_n \end{pmatrix} \otimes \begin{pmatrix} w_1 \\ \vdots \\ w_n \end{pmatrix} = \begin{pmatrix} v_1 \begin{pmatrix} w_1 \\ \vdots \\ w_n \end{pmatrix} \\ \vdots \\ v_n \begin{pmatrix} w_1 \\ \vdots \\ w_n \end{pmatrix} \end{pmatrix}$$

Tensor product of two matrices: multiply the right-hand matrix by each element of the left-hand matrix.

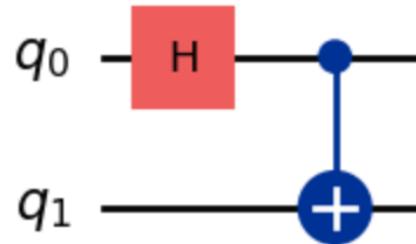
$$A \otimes B = \begin{pmatrix} A_{11}B & A_{12}B \\ A_{21}B & A_{22}B \end{pmatrix} = \begin{pmatrix} A_{11}B_{11} & A_{11}B_{12} & A_{12}B_{11} & A_{12}B_{12} \\ A_{11}B_{21} & A_{11}B_{22} & A_{12}B_{21} & A_{12}B_{22} \\ A_{21}B_{11} & A_{21}B_{12} & A_{22}B_{11} & A_{22}B_{12} \\ A_{21}B_{21} & A_{21}B_{22} & A_{22}B_{21} & A_{22}B_{22} \end{pmatrix}$$

A two-qubit state can be represented as the tensor product of two single-qubit states.

$$|00\rangle = |0\rangle \otimes |0\rangle = \begin{pmatrix} 1 \\ 0 \\ 0 \\ 0 \end{pmatrix} \otimes \begin{pmatrix} 1 \\ 0 \end{pmatrix} = \begin{pmatrix} 1 \\ 0 \\ 0 \\ 0 \end{pmatrix} \equiv |0\rangle, \quad |01\rangle = |0\rangle \otimes |1\rangle = \begin{pmatrix} 1 \\ 0 \\ 0 \\ 0 \end{pmatrix} \otimes \begin{pmatrix} 0 \\ 1 \end{pmatrix} = \begin{pmatrix} 0 \\ 1 \\ 0 \\ 0 \end{pmatrix} \equiv |1\rangle,$$

$$|10\rangle = |1\rangle \otimes |0\rangle = \begin{pmatrix} 0 \\ 1 \\ 0 \\ 0 \end{pmatrix} \otimes \begin{pmatrix} 1 \\ 0 \end{pmatrix} \equiv |2\rangle, \quad |11\rangle = |1\rangle \otimes |1\rangle = \begin{pmatrix} 0 \\ 1 \\ 0 \\ 0 \end{pmatrix} \otimes \begin{pmatrix} 0 \\ 1 \end{pmatrix} = \begin{pmatrix} 0 \\ 0 \\ 0 \\ 1 \end{pmatrix} \equiv |3\rangle$$

Entangled state



$$\begin{aligned}|0\rangle_1 \otimes |0\rangle_0 &\xrightarrow{I \otimes H} |0\rangle \otimes \frac{1}{\sqrt{2}}(|0\rangle + |1\rangle) \\&= \frac{1}{\sqrt{2}}(|00\rangle + |01\rangle) \\&\xrightarrow{CNOT} \frac{1}{\sqrt{2}}(|00\rangle + |11\rangle)\end{aligned}$$

An entangled state is a state $|\psi\rangle_{AB}$ consisting of quantum states $|\psi\rangle_A$ and $|\psi\rangle_B$ that cannot be represented by a tensor product of individual quantum states.

$$\begin{aligned}\frac{1}{\sqrt{2}}(|00\rangle + |11\rangle) &\neq (a_0|0\rangle + a_1|1\rangle) \otimes (b_0|0\rangle + b_1|1\rangle) \\&= a_0b_0|00\rangle + \underline{a_1b_0}|10\rangle + \underline{a_0b_1}|01\rangle + a_1b_1|11\rangle\end{aligned}$$

There is no coefficient which satisfies this equation. Therefore, this state is entangled state.

Qiskit hands-on

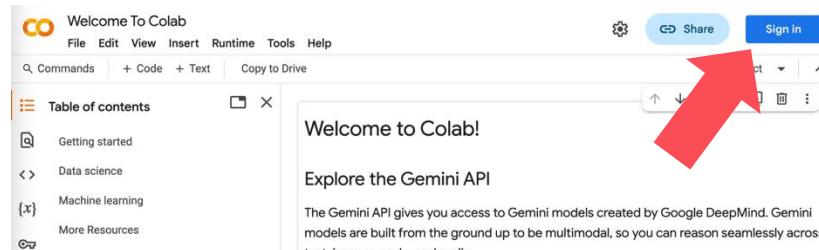
Please download the file, "[20251118_QLTP_IntroQC.ipynb](#)"
from URL: <https://ibm.ent.box.com/folder/351459863769>

Use Qiskit on Online lab environment

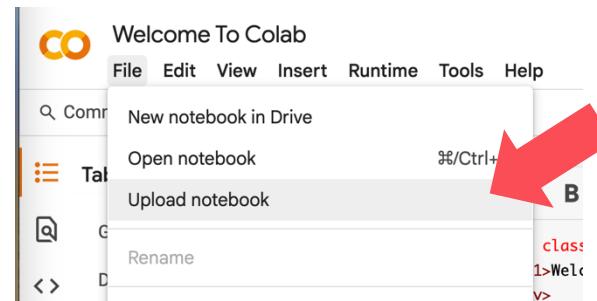
Reference: <https://quantum.cloud.ibm.com/docs/en/guides/online-lab-environments>

- (1) Go to Google Colab and Sign in it.

<https://colab.research.google.com/>



- (2) (next week) File → Upload notebook



You need to install Qiskit every time when you open new notebook.

Install and set up Qiskit 2.0 (macOS)

- Reference URL : <https://quantum.cloud.ibm.com/docs/en/guides/install-qiskit> (For non-macOS users, please refer this.)
- For those upgrading from version 0.x to 2.0: note that because Qiskit v2.0 uses a new packaging structure, you **cannot** use pip install -U qiskit to upgrade from any Qiskit 0.x version to 2.0.

1. Create a new virtual environment, using Python 3.8 or later.

```
python3 -m venv qiskit-venv
```

2. Activate the environment.

```
source qiskit-venv/bin/activate
```

3. Install Qiskit.

```
pip install qiskit
```

4. Install the necessary packages.

```
pip install qiskit-ibm-runtime  
pip install qiskit[visualization]  
pip install jupyter  
pip install qiskit-aer
```

zsh users need to put 'qiskit[visualization]' in single quotes.

5. With the following command, you can launch Jupyter notebook and start using Qiskit.

```
jupyter notebook
```

6. Try the first cell of [Hello world](#) by copy and paste, and execute it by “Shift”+“Enter”.

6. If you are not planning to use the environment immediately, use the deactivate command to leave it.

```
deactivate
```

IBM Quantum