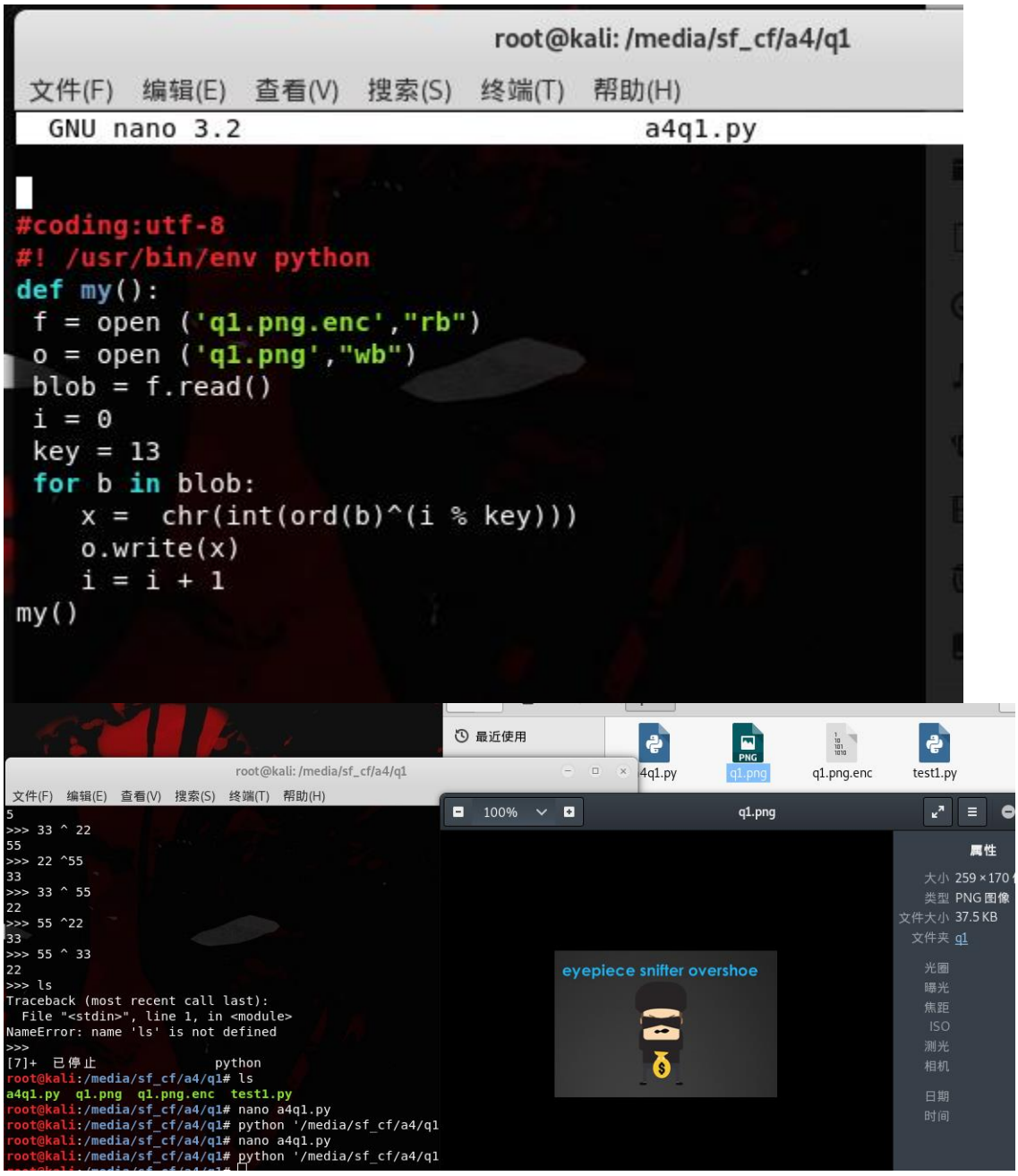
Q1.

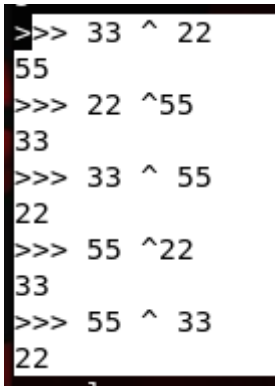


I don't think this is a good encryption scheme, even the key was kept secret.

Reason:

a^b=c,a^c=b,c^b=a.

e.g.

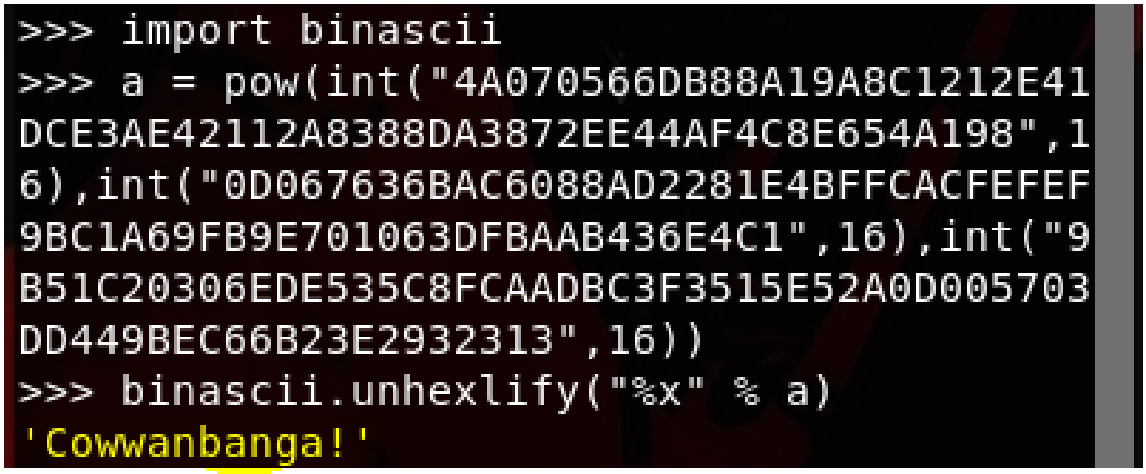


they can transform into each other.

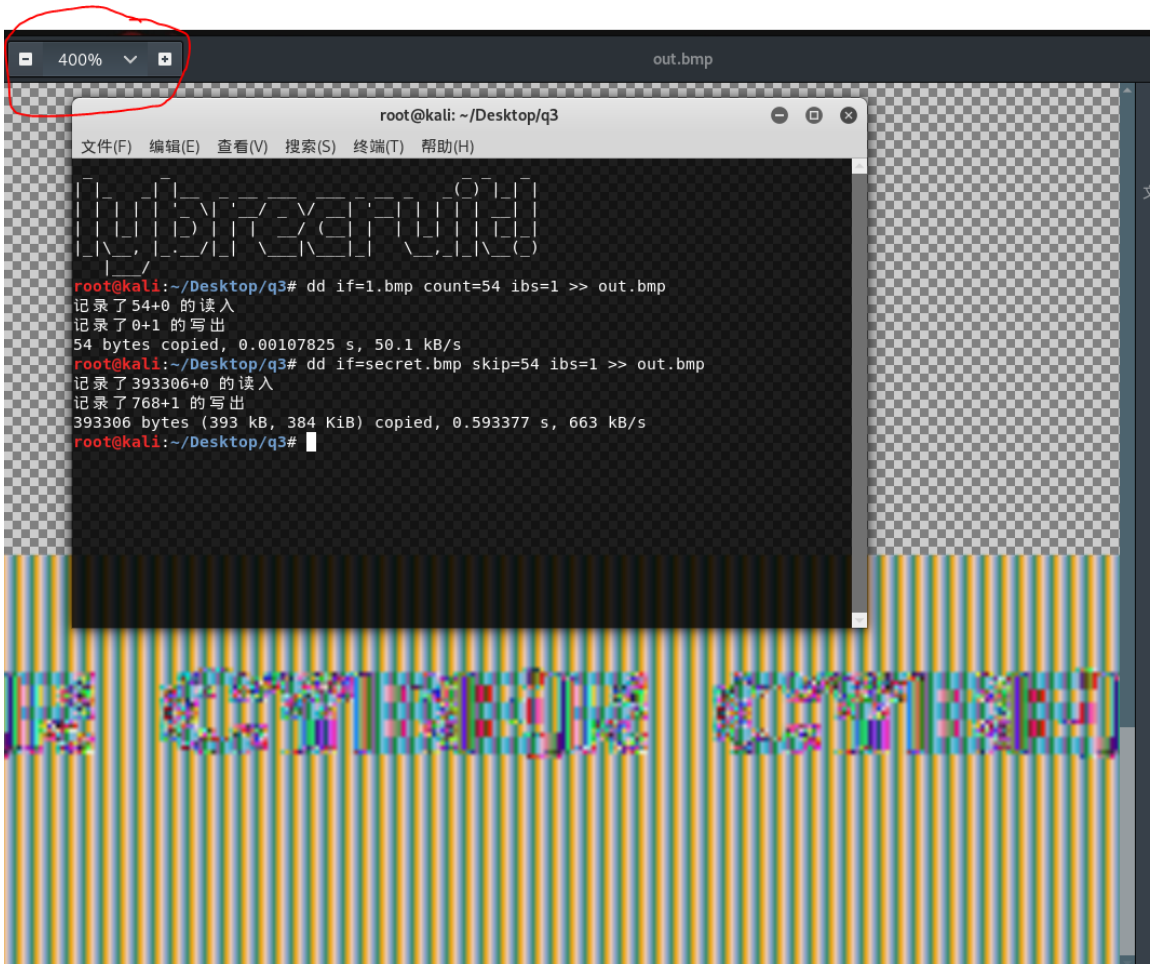
Brute force will use linear time to crack the cipher.

Unless the key is very large, it will cost more time (larger dictionary).

Q2.



Q3.



Q4.

We calculate the frequency of any single letter: using website:
(http://www.aihanyu.org/cncorpus/CpsTongji.aspx)

1		119	19.4127
2	T	69	11.2561
3	M	48	7.8303
4	O	45	7.3409
5	G	44	7.1778
6	L	42	6.8515
7	A	28	4.5677
8	I	28	4.5677
9	K	27	4.4046
10	F	22	3.5889
11	C	21	3.4258
12	Y	19	3.0995
13	,	17	2.7732
14	R	14	2.2838
15	U	13	2.1207
16	S	12	1.9576
17	H	10	1.6313
18	E	7	1.1419
19	D	5	0.8157
20	W	5	0.8157
21	X	5	0.8157
22	Z	5	0.8157
23	B	4	0.6525
24	Q	2	0.3263

.

The lecture shows that the most common letter in english is E.

In this scenes: E->T

And the most common letter: the

2	MIT	14	10.1449
3	GY	12	8.6957
4	CAL	11	7.971
5	OM	10	7.2464
6	CT	4	2.8986
7	ASS	2	1.4493
8	AUT	2	1.4493
9	CTKT	2	1.4493
10	HTKDGR	2	1.4493
11	IAR	2	1.4493
12	LTALGF	2	1.4493
13	MODTL	2	1.4493
14	OF	2	1.4493
15	OML	2	1.4493
16	ROKTEM	2	1.4493
17	THGEI	2	1.4493
18	UGOFU	2	1.4493
19	WL	2	1.4493
20	YGK	2	1.4493
21	ZTYGKT	2	1.4493

THE->MIT. This also confirmed e->t

t->m +19/-7

h->I +1/-27

e->t +15/-41

thus, there's not Caesar cipher or vigenere cipher.

Maybe substitution cipher

Get through www.wordfrequency.info

Looking at the word: AW**th**GKO**t**O**e**L
Use online tools: http://www.hanginghyena.com/hangmansolver
try to search as "??th???t? e?"
get the answer: authorities
now we get

a->A
u->W
o->G
r->K
i->O
s->L

ZeYore

b->Z
f->Y

ResHair

d->R
p->H

epoEh

c->E

beSief

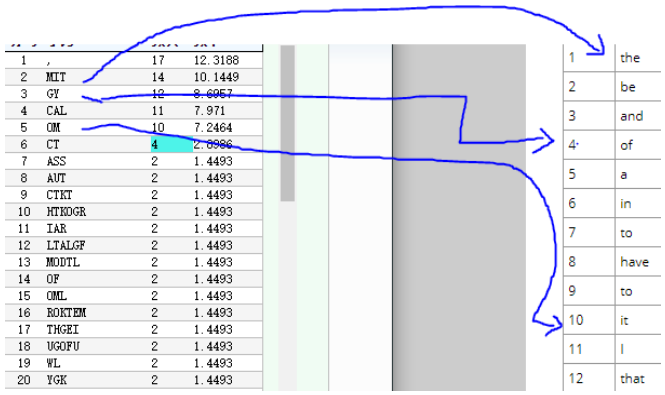
l->S

CisdoD

w->C
m->D

iFcredulitB

n->F
y->B
g->U
k->Q
v->X



1	,	17	12.3188
2	MIT	14	10.1449
3	GY	12	8.6957
4	CAL	11	7.971
5	OM	10	7.2464
6	CT	4	2.8986
7	ASS	2	1.4493
8	AUT	2	1.4493
9	CTKT	2	1.4493
10	MTKOGR	2	1.4493
11	IAR	2	1.4493
12	LTALGF	2	1.4493
13	MODTL	2	1.4493
14	OF	2	1.4493
15	OML	2	1.4493
16	ROKTEM	2	1.4493
17	THGEI	2	1.4493
18	UGOFU	2	1.4493
19	WL	2	1.4493
20	YGK	2	1.4493

1	the
2	be
3	and
4	of
5	a
6	in
7	to
8	have
9	to
10	it
11	I
12	that

according to existing keys, keep going, finally we can get:

it was the best of times, it was the worst of times, it was the age of wisdom, it was the age

of foolishness, it was the epoch of belief, it was the epoch of incredulity, it was the season of light, it was the season of darkness, it was the spring of hope, it was the winter of despair, we had everything before us, we had nothing before us, we were all going direct to heaven, we were all going direct the other way - in short, the period was so far like the present period, that some of its noisiest authorities insisted on its being received, for good or for evil, in the superlative degree of comparison only.

0	A	0	A
1	B	25	Z
2	C	4	E
3	D	17	R
4	E	19	T
5	F	24	Y
6	G	20	U
7	H	8	I
8	I	14	O
9	J		
10	K	16	Q
11	L	18	S
12	M	3	D
13	N	5	F
14	O	6	G
15	P	7	H
16	Q		
17	R		
18	S	11	L
19	T		
20	U	22	W
21	V	23	X
22	W	2	C
23	X		
24	Y	1	B
25	Z		

For encrypt: Y=(X+K) mod 26
0= 0+k mod 26 k= +-26
25 = 1+k mod 26 = 25 mod 26| -1 mod 26 => k = 24 | -2
4 = 2 + k mod 26 = 30mod26 | -22 mod 26 => k = 28 | -24
For decrypt: X= (Y - K) mod 26
0= 0-k mod 26 k= +-26
24=1-k mod 26 = 24mod26 | -2mod26=> k = -23 | 3
22 = 2-k mod 26 = 22mod26 | -4mod26=> k = -20 | 6
12=3-k mod 26=> k = -9 | 17
Sorry I can't find the key. Maybe the key is "the=>mit"?

Q5.

Q6.