Approximation Bounds for Hierarchical Clustering

Algorithm	This paper's Reward Objective	Dasgupta's Cost Objective
Single Linkage	Flail: $\frac{1}{\Omega(n^{1/3})}$ [Thm. 10]	Line: $\Omega(\frac{n}{\log n})$ [Thm. 11]
28	$\Omega(n^{1/3})$ [ ]	$\log n$

Clique Star:  $\Omega(n^{1/3})$  [Thm. 13] Clique Star:  $(1/2 + \delta)$  [Thm. 12] Average Linkage

Double Star:  $\frac{1}{\Omega(n)}$  [Thm. 14]

Complete Linkage

Line:  $\Omega(\frac{n}{\log n})$  [Thm. 15] Double Star:  $\frac{1}{\Omega(\sqrt{n})}$  [Thm. 16] Cycle Star:  $\Omega(\sqrt{n})$  [Thm. 17] Bisecting k-Means