```
1import java.util.Comparator;
10 / * *
11 * {@code SortingMachine} represented as a {@code Queue} and an array (using an
12 * embedding of heap sort), with implementations of primary methods.
13 *
14 * @param <T>
15 *
                type of {@code SortingMachine} entries
16 * @mathdefinitions 
17 * IS TOTAL PREORDER (
18 *
     r: binary relation on T
19 * ) : boolean is
20 * for all x, y, z: T
21 *
     ((r(x, y) or r(y, x)) and
22 *
       (if (r(x, y) \text{ and } r(y, z)) then r(x, z)))
23 *
24 * SUBTREE IS HEAP (
25 * a: string of T,
26 *
      start: integer,
27 *
     stop: integer,
28 *
     r: binary relation on T
29 * ) : boolean is
30 * [the subtree of a (when a is interpreted as a complete binary tree) rooted
      at index start and only through entry stop of a satisfies the heap
      ordering property according to the relation r]
33 *
34 * SUBTREE ARRAY ENTRIES (
35 * a: string of T,
36 *
     start: integer,
37 *
     stop: integer
38 \star ) : finite multiset of T is
39 * [the multiset of entries in a that belong to the subtree of a
40 *
      (when a is interpreted as a complete binary tree) rooted at
41 *
      index start and only through entry stop]
42 * 
43 * @convention 
44 * IS TOTAL PREORDER([relation computed by $this.machineOrder.compare method] and
45 * if $this.insertionMode then
46 *
      $this.heapSize = 0
47 * else
48 *
     $this.entries = <> and
49 *
      for all i: integer
50 *
          where (0 \le i \text{ and } i \le |\$\text{this.heap}|)
         ([entry at position i in $this.heap is not null]) and
51 *
52 *
       SUBTREE IS HEAP($this.heap, 0, $this.heapSize - 1,
         [relation computed by $this.machineOrder.compare method]) and
       0 <= $this.heapSize <= |$this.heap|</pre>
55 * 
56 * @correspondence 
57 * if $this.insertionMode then
58 * this = (true, $this.machineOrder, multiset entries($this.entries))
59 * else
60 * this = (false, $this.machineOrder, multiset entries($this.heap[0,
 $this.heapSize)))
61 * 
62 *
63 * @author Gabe Azzarita
64 * @author Ty Fredrick
65 *
```

```
66 */
 67 public class SortingMachine5a<T> extends SortingMachineSecondary<T> {
 69
 70
       * Private members ------
 71
 72
 73
      /**
       * Order.
 74
 75
 76
      private Comparator<T> machineOrder;
 77
 78
      /**
 79
      * Insertion mode.
 80
 81
      private boolean insertionMode;
 82
 83
      * Entries.
 84
 85
86
      private Queue<T> entries;
 87
      /**
 88
       * Heap.
 89
      * /
 90
 91
     private T[] heap;
 92
 93
      /**
      * Heap size.
 94
 95
 96
     private int heapSize;
 97
 98
99
       * Exchanges entries at indices {@code i} and {@code j} of {@code array}.
100
101
       * @param <T>
102
                    type of array entries
       * @param array
103
104
                    the array whose entries are to be exchanged
105
       * @param i
106
                    one index
107
      * @param j
108
                   the other index
       * @updates array
109
       * @requires 0 <= i < |array| and 0 <= j < |array|
110
111
       * @ensures array = [#array with entries at indices i and j exchanged]
112
       * /
113
     private static <T> void exchangeEntries(T[] array, int i, int j) {
114
          assert array != null : "Violation of: array is not null";
          assert 0 <= i : "Violation of: 0 <= i";</pre>
115
116
          assert i < array.length : "Violation of: i < |array|";</pre>
          assert 0 <= j : "Violation of: 0 <= j";</pre>
117
118
          assert j < array.length : "Violation of: j < |array|";</pre>
119
         if (i != j) {
120
121
              T tmp = array[i];
              array[i] = array[j];
122
123
              array[j] = tmp;
124
          }
```

```
125
126
      }
127
128
129
       * Given an array that represents a complete binary tree and an index
130
       * referring to the root of a subtree that would be a heap except for its
131
       * root, sifts the root down to turn that whole subtree into a heap.
132
133
       * @param <T>
134
                    type of array entries
135
       * @param array
136
                     the complete binary tree
       * @param top
137
                     the index of the root of the "subtree"
138
139
      * @param last
140
                     the index of the last entry in the heap
       * @param order
141
142
                    total preorder for sorting
       * @updates array
143
144
       * @requires 
145
       * 0 <= top and last < |array| and
       * for all i: integer
146
147
             where (0 \le i \text{ and } i \le |\text{array}|)
148
           ([entry at position i in array is not null]) and
149
        * [subtree rooted at {@code top} is a complete binary tree] and
       * SUBTREE IS HEAP(array, 2 * top + 1, last,
150
151
             [relation computed by order.compare method]) and
       * SUBTREE IS HEAP(array, 2 * top + 2, last,
152
153
              [relation computed by order.compare method]) and
154
       * IS TOTAL PREORDER([relation computed by order.compare method])
155
       * 
156
       * @ensures 
157
       * SUBTREE IS HEAP(array, top, last,
158
              [relation computed by order.compare method]) and
159
       * perms(array, #array) and
160
       * SUBTREE ARRAY ENTRIES(array, top, last) =
161
       * SUBTREE ARRAY ENTRIES (#array, top, last) and
162
       * [the other entries in array are the same as in #array]
163
        * 
164
        * /
165
       private static <T> void siftDown(T[] array, int top, int last,
166
               Comparator<T> order) {
167
           assert array != null : "Violation of: array is not null";
           assert order != null : "Violation of: order is not null";
168
169
           assert 0 <= top : "Violation of: 0 <= top";</pre>
170
           assert last < array.length : "Violation of: last < |array|";</pre>
171
           for (int i = 0; i < array.length; i++) {</pre>
               assert array[i] != null : ""
172
173
                       + "Violation of: all entries in array are not null";
174
175
           assert isHeap(array, 2 * top + 1, last, order) : ""
176
                   + "Violation of: SUBTREE IS HEAP(array, 2 * top + 1, last,"
177
                   + " [relation computed by order.compare method])";
178
           assert isHeap(array, 2 * top + 2, last, order) : ""
179
                   + "Violation of: SUBTREE IS HEAP(array, 2 * top + 2, last,"
180
                   + " [relation computed by order.compare method])";
181
            * Impractical to check last requires clause; no need to check the other
182
183
            * requires clause, because it must be true when using the array
```

```
184
            * representation for a complete binary tree.
185
186
187
           if (!isHeap(array, top, last, order)) {
188
               int leftIndex = 2 * top + 1;
189
               int rightIndex = 2 * top + 2;
190
191
               // if left doesn't exist neither will right
192
               if (leftIndex <= last) {</pre>
193
                   // check that right exists
194
                   if (rightIndex <= last) {</pre>
195
                       // swap root with smaller child and sift down
196
                       if (order.compare(array[rightIndex],
197
                               array[leftIndex]) > 0) {
198
                           exchangeEntries(array, top, leftIndex);
199
                           siftDown(array, leftIndex, last, order);
200
                       } else {
201
                           exchangeEntries(array, top, rightIndex);
202
                           siftDown(array, rightIndex, last, order);
203
                       }
204
                   } else {
205
                       // if left doesn't exist, exchange with left
206
                       exchangeEntries(array, top, leftIndex);
207
                       siftDown(array, leftIndex, last, order);
208
                   }
209
               }
210
211
           }
212
213
       }
214
215
216
        * Heapifies the subtree of the given array rooted at the given {@code top}.
217
218
       * @param <T>
219
                     type of array entries
       * @param array
220
221
                     the complete binary tree
222
        * @param top
223
                     the index of the root of the "subtree" to heapify
224
       * @param order
225
                     the total preorder for sorting
226
       * @updates array
227
       * @requires 
       * 0 <= top and
228
229
       * for all i: integer
230
            where (0 \le i \text{ and } i \le |array|)
231
           ([entry at position i in array is not null]) and
232
       * [subtree rooted at {@code top} is a complete binary tree] and
        * IS TOTAL PREORDER([relation computed by order.compare method])
233
        * 
234
235
       * @ensures 
236
        * SUBTREE IS HEAP(array, top, |array| - 1,
237
             [relation computed by order.compare method]) and
        * perms(array, #array)
238
       * 
239
       * /
240
241
       private static <T> void heapify(T[] array, int top, Comparator<T> order) {
242
           assert array != null : "Violation of: array is not null";
```

```
243
           assert order != null : "Violation of: order is not null";
244
           assert 0 <= top : "Violation of: 0 <= top";</pre>
245
           for (int i = 0; i < array.length; i++) {</pre>
246
               assert array[i] != null : ""
247
                       + "Violation of: all entries in array are not null";
248
           }
249
250
            * Impractical to check last requires clause; no need to check the other
251
            * requires clause, because it must be true when using the array
252
            * representation for a complete binary tree.
253
254
255
           int left = 2 * top + 1;
256
           int right = 2 * top + 2;
257
258
           // Make sure left and right "trees" exist
259
           if (right < array.length) {</pre>
260
               // if right exists, so does left
261
               heapify(array, left, order);
262
               heapify(array, right, order);
263
           } else if (left < array.length) {</pre>
264
               // else check if left exists
265
               heapify(array, left, order);
266
267
           // after heapifying left and right (if exist) sift down original root
268
           siftDown(array, top, array.length - 1, order);
269
270
           // *** you must use the recursive algorithm discussed in class ***
271
272
       }
273
       /**
274
275
        ^{\star} Constructs and returns an array representing a heap with the entries from
276
        * the given {@code Queue}.
277
       * @param <T>
278
279
                     type of {@code Queue} and array entries
280
       * @param q
281
                     the {@code Queue} with the entries for the heap
282
        * @param order
283
                    the total preorder for sorting
       * @return the array representation of a heap
284
285
       * @clears q
       * @requires IS TOTAL PREORDER([relation computed by order.compare method])
286
       * @ensures 
287
        * SUBTREE IS HEAP(buildHeap, 0, |buildHeap| - 1) and
288
289
        * perms(buildHeap, #q) and
290
        * for all i: integer
291
              where (0 \le i \text{ and } i \le |buildHeap|)
           ([entry at position i in buildHeap is not null]) and
292
293
        * 
294
        * /
295
       @SuppressWarnings("unchecked")
296
       private static <T> T[] buildHeap(Queue<T> q, Comparator<T> order) {
297
           assert q != null : "Violation of: q is not null";
298
           assert order != null : "Violation of: order is not null";
299
300
            * Impractical to check the requires clause.
301
```

```
302
303
304
            * With "new T[...]" in place of "new Object[...]" it does not compile;
305
            * as shown, it results in a warning about an unchecked cast, though it
306
            * cannot fail.
            * /
307
308
309
           T[] heap = (T[]) (new Object[q.length()]);
310
           int formerLength = q.length();
311
312
           for (int k = 0; k < formerLength; k++) {</pre>
313
               // dequeue item from queue and add to heap
314
               heap[k] = q.dequeue();
315
           }
316
317
           heapify(heap, 0, order);
318
           return heap;
319
      }
320
      /**
321
322
       * Checks if the subtree of the given {@code array} rooted at the given
323
       * {@code top} is a heap.
324
325
       * @param <T>
326
           type of array entries
       * @param array
327
328
                    the complete binary tree
       * @param top
329
330
                     the index of the root of the "subtree"
       * @param last
331
332
                     the index of the last entry in the heap
333
       * @param order
334
                    total preorder for sorting
335
       * @return true if the subtree of the given {@code array} rooted at the
336
                 given {@code top} is a heap; false otherwise
337
       * @requires 
338
       * 0 <= top and last < |array| and
339
       * for all i: integer
340
            where (0 \le i \text{ and } i \le |array|)
341
           ([entry at position i in array is not null]) and
342
        * [subtree rooted at {@code top} is a complete binary tree]
       * 
343
344
       * @ensures 
345
       * isHeap = SUBTREE IS HEAP(array, top, last,
346
              [relation computed by order.compare method])
347
        * 
348
        * /
349
       private static <T> boolean isHeap(T[] array, int top, int last,
350
               Comparator<T> order) {
           assert array != null : "Violation of: array is not null";
351
352
           assert 0 <= top : "Violation of: 0 <= top";</pre>
353
           assert last < array.length : "Violation of: last < |array|";</pre>
354
           for (int i = 0; i < array.length; i++) {</pre>
355
               assert array[i] != null : ""
356
                       + "Violation of: all entries in array are not null";
357
           }
358
359
            * No need to check the other requires clause, because it must be true
360
            * when using the Array representation for a complete binary tree.
```

```
* /
361
362
363
           int left = 2 * top + 1;
364
           int right = 2 * top + 2;
365
           boolean heapL = true;
366
           boolean heapR = true;
367
368
369
            * We can check for heap by making sure that both the left and right
370
            * children are smaller than the "root" and then checking that the left
371
            * and right are heaps
372
            * /
373
374
           // check if left exists, if it doesn't, neither will right
375
           if (left <= last) {</pre>
376
               heapL = (order.compare(array[top], array[left]) <= 0)</pre>
377
                        && isHeap(array, left, last, order);
378
                // if left is a heap, let's check the right side (if exists)
379
                if (heapL && (right <= last)) {</pre>
380
                    heapR = (order.compare(array[top], array[right]) <= 0)</pre>
381
                            && isHeap(array, right, last, order);
382
                }
383
384
           return heapL && heapR;
385
       }
386
       /**
387
        * Checks that the part of the convention repeated below holds for the
389
        * current representation.
390
391
        * @return true if the convention holds (or if assertion checking is off);
392
                  otherwise reports a violated assertion
393
        * @convention 
394
        * if $this.insertionMode then
395
           $this.heapSize = 0
396
        * else
397
            $this.entries = <> and
398
            for all i: integer
399
                where (0 \le i \text{ and } i \le |\$\text{this.heap}|)
400
              ([entry at position i in $this.heap is not null])
401
           SUBTREE IS HEAP($this.heap, 0, $this.heapSize - 1,
402
              [relation computed by $this.machineOrder.compare method]) and
403
            0 <= $this.heapSize <= |$this.heap|</pre>
404
        * 
        * /
405
406
       private boolean conventionHolds() {
407
           if (this.insertionMode) {
                assert this.heapSize == 0 : ""
408
409
                        + "Violation of: if $this.insertionMode then $this.heapSize = 0";
410
           } else {
                assert this.entries.length() == 0 : ""
411
                        + "Violation of: if not $this.insertionMode then $this.entries =
412
   <>";
413
                assert 0 <= this.heapSize : ""</pre>
                        + "Violation of: if not this.insertionMode then 0 <=
414
   $this.heapSize";
                assert this.heapSize <= this.heap.length : ""</pre>
415
                        + "Violation of: if not $this.insertionMode then"
416
                        + " $this.heapSize <= |$this.heap|";
417
```

next = this.queueIterator.next();

} else {

652

653

```
Tuesday, October 10, 2023, 2:56 PM
SortingMachine5a.java
654
                   next = SortingMachine5a.this.heap[this.arrayCurrentIndex];
655
                   this.arrayCurrentIndex++;
656
657
               assert SortingMachine5a.this.conventionHolds();
658
              return next;
659
          }
660
          @Override
661
662
         public void remove() {
663
              throw new UnsupportedOperationException(
                      "remove operation not supported");
664
665
          }
666
667
     }
668
669}
670
```