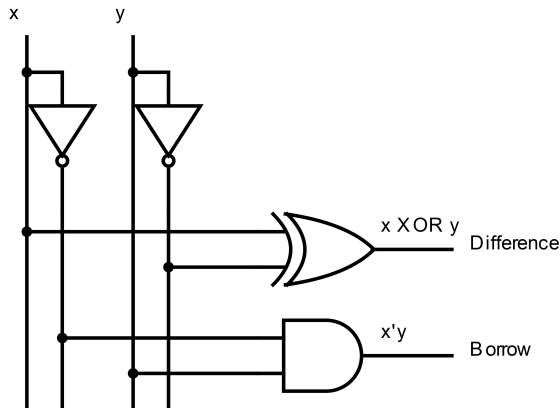


1. Design a half-subtractor circuit with input x and y and outputs D (Difference) and B_{out} (Borrow) which performs $x - y$.

x	y	D	B_{out}
0	0	0	0
0	1	1	1
1	0	1	0
1	1	0	0

$$\left. \begin{array}{l} D = x \oplus y \\ B_{out} = x'y \end{array} \right\}$$


2. Design a full-subtractor circuit with three inputs, x , y , and B_{prev} , which performs $x - y - B_{prev}$.

B_{prev}	x	y	D	B_{out}
0	0	0	0	0
0	0	1	1	1
0	1	0	1	0
0	1	1	0	0
1	0	0	1	1
1	0	1	0	1
1	1	0	0	0
1	1	1	1	1

(D) xy

	00	01	11	10
0	0	1	0	1
1	1	0	1	0

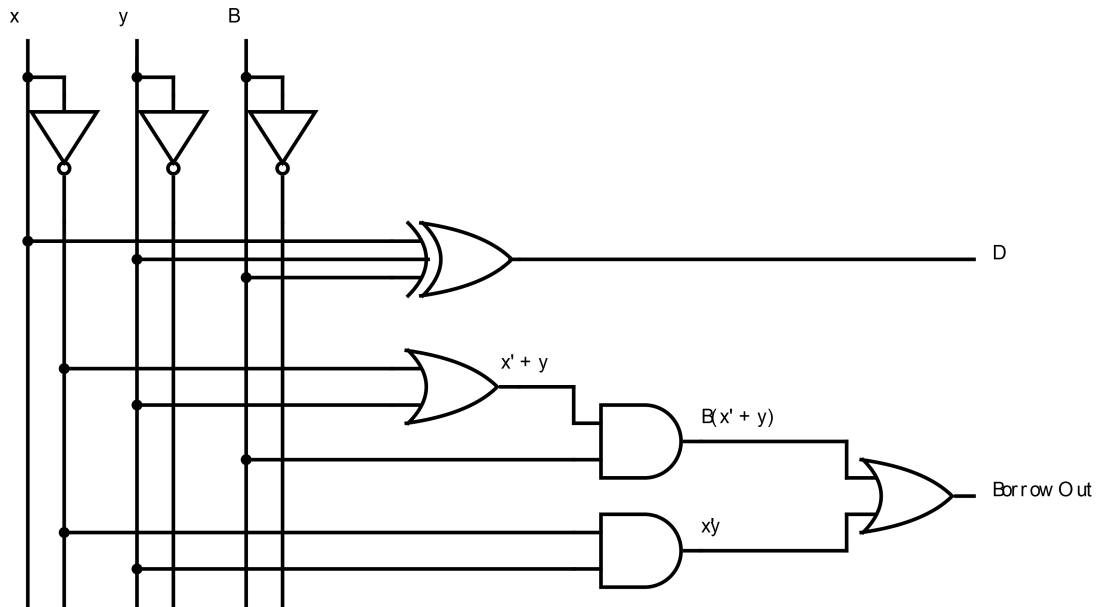
(B_{out}) xy

	00	01	11	10
0	0	1	0	0
1	1	1	1	0

¹The package used for drawing kmaps does not support diagonal groups. I have used regular a regular 4x2 group in this case, however it should be observed to be representative of XOR, not a larger implicant.

$$\therefore D = x \oplus y \oplus B_{prev}$$

$$\begin{aligned}\therefore B_{out} &= x'y + B_{prev}x' + B_{prev}y \\ &= B_{prev}(x' + y) + x'y\end{aligned}$$



¹The application used to draw these circuits has issues rendering text. I apologize for any inconvenience..