

# Estimating General Equilibrium Spillovers of Large-Scale Shocks

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## Abstract

Large-scale financial and macroeconomic shocks directly affect some firms and households and indirectly impact others through general equilibrium spillovers. In this paper, I discuss econometric challenges that arise in the estimation of spillovers using quasi-experimental or experimental variation. Spillover estimates suffer from distinct sources of mechanical bias that are not solved by standard empirical tools. These biases are particularly common in financial and macroeconomic settings where there are many spillover channels and nonlinear effects. I offer guidance on how to detect and overcome mechanical biases. An application to a real-world credit shock highlights the magnitude of biases and suggested solutions.

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# I Introduction

Researchers in finance and macroeconomics are often interested in spillover effects: how shocks to some firms and households affect other parts of the economy. By quantifying spillovers, researchers can evaluate which general equilibrium channels need to be included in economic models and to what extent empirical estimates based on micro data are informative about other levels of aggregation. Spillovers are particularly important when researchers study large-scale financial and business cycle shocks because many firms and households are simultaneously affected and spillovers are large.

Consider why it is helpful to understand spillovers using two concrete examples at the regional level. An empirical literature estimates how regional house price shocks affect regional employment (Mian and Sufi 2014; Giroud and Mueller 2017). But a parameter required to calibrate macro-finance models is the direct effect of a house price change on an individual household (Guren et al. 2020). To convert regional estimates into the direct effect, we need to know the magnitude of regional spillovers after a housing shock. Another literature shows that firms with an unhealthy bank grow more slowly than other firms in the same region with a healthy bank (Bentolila et al. 2018). A regional policymaker may wonder how subsidizing the unhealthy bank will affect the entire regional economy, and so will need to understand regional spillovers after a banking shock. In both cases, estimates of regional spillovers would allow converting existing estimates to another level of aggregation, even if direct estimates at the desired level of aggregation are not readily available.

The traditional approach to measuring spillovers in finance and macroeconomics is to calibrate a fully specified, general equilibrium model of the economy. Such models can flexibly quantify spillovers operating among firms and households in the same region, sector, country, or any other group. A weakness of the model-based approach is that results depend on hard-to-verify assumptions about which general equilibrium channels exist. In this paper, I discuss the implementation of an alternative empirical approach: direct spillover estimation using quasi-experiments or experiments. This approach is becoming increasingly popular in finance and macroeconomics. It allows researchers to quantify spillovers operating within groups of firms and households using a regression framework.

This paper offers econometric guidance on how to implement direct spillover estimation. I point out two sources of mechanical bias that are likely to arise in finance and macroeconomics: multiple types of spillovers and mismeasured treatment status. I suggest practical solutions to investigating and overcoming these biases. I illustrate the relevance of the biases and proposed solutions with an application to a real-world credit shock. Finally, I argue that understanding spillovers through direct estimation can inform policy.

The paper begins with an empirical framework for direct spillover estimation. I henceforth use “firms” to describe the unit of direct treatment, but the framework applies equally when households or other entities are the directly treated units. A researcher studies whether a shock to a subset of firms (the “treatment”) generates spillovers onto other firms that are in the same “group” as treated firms. Firms that belong to the same group are in some way connected, for example because they are in the same region, production network, technology space, or any other type of grouping. The approach requires identification of a treatment that is exogenous both across individuals and across groups. A group can even constitute an entire country, so that the estimated spillovers operate at the country level, as long as a researcher can identify exogenous variation in treatment at the country level and at least one lower level of aggregation (e.g., regions, sectors, firms, or households).<sup>1</sup>

To directly estimate spillovers, the researcher includes the average treatment status of all other firms in the same group in the regression (the “leave-out mean”). For example, if the researcher is interested in regional spillovers, one regressor is the average treatment status of all other firms in the region. Direct spillover estimation using leave-out means has several attractive features. It is relatively easy to apply to existing research designs. It allows researchers to directly compare the magnitude of different types of spillovers, by simultaneously including multiple leave-out means in the regression. The method estimates a standard error on the spillover, which allows formal inference on whether spillovers are statistically significant.

Notwithstanding these advantages, I argue that direct spillover estimation raises difficult and underappreciated empirical challenges. I focus on two challenges that are common when researchers study large-scale financial and macroeconomic shocks: first, the presence of multiple types of spillovers and second, mismeasured treatment status due to nonlinearity or measurement error. These issues can mechanically bias estimates of both the spillover and direct effects, even if the (quasi-)experimental variation defining direct and group treatment status is truly exogenous and if there are no omitted variables correlated with treatment. Standard (quasi-)experimental tools (e.g., testing for sample balance and parallel trends) do not solve these issues. I discuss the two issues in turn.

First, I consider the case of multiple spillover types. Spillovers operate simultaneously across multiple groups after almost all large-scale shocks. For example, shocks to firms spill over to other firms through factor markets, product markets, input-output networks, common lenders, etc. To simplify the exposition, I center the conceptual discussion around the example of two groups, but I do not mean to imply that these groups cover all potential spillovers.<sup>2</sup> Consider then a

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<sup>1</sup>Recent work identifies exogenous country-level variation in fiscal and monetary policy using idiosyncratic decisions (Romer and Romer 2004, 2010; Wolf 2020), foreign events (Jiménez et al. 2012; Conley et al. 2021), asset prices around policy announcements (Cook and Hahn 1989; Gürkaynak et al. 2005; Nakamura and Steinsson 2018a), and large political upheavals (Fuchs-Schündeln 2008).

<sup>2</sup>Throughout the paper, I use regions and sectors as concrete examples for the two types of spillovers. But the leave-

shock to a subset of firms that simultaneously spills over to other firms in the same region (e.g., through wages, as directly treated firms hire more on local labor markets) and the same sector (e.g., through output prices, as directly treated firms raise production). Despite this empirical complexity, theoretical models typically do not account for all relevant spillover channels. For instance, urban models may include only a regional spillovers, while industrial organization models may exclusively focus on a sectoral spillover. Specialized researchers may then empirically test for only one potential spillover, without considering the other.

I show that testing for spillovers within only one group can severely bias spillover estimates if multiple types of spillovers determine the true outcome. Spillover estimates may even have the wrong sign, leading to a complete misinterpretation of general equilibrium forces. This bias may also occur if membership in the two spillover groups is orthogonal, so that the two leave-out means are uncorrelated. In that sense, bias due to multiple spillovers is distinct from standard concerns about omitting correlated variables from the specification and is usually not considered in applied papers. Intuitively, the bias occurs because directly treated firms are disproportionately in groups with high average treatment, which makes it difficult for empirical tests to differentiate between direct effect and spillover effect.

The second estimation issue I discuss is mismeasurement in direct treatment status, caused by either measurement error or nonlinear direct effects. I initially consider a modest degree of classical measurement error, as found in standard datasets (Bound and Krueger 1991). Such error can generate large spillover estimates, even if true spillovers are zero, because part of the true direct effect erroneously loads onto the spillover estimate. Measurement error can bias spillover estimates in either direction, depending on the underlying data-generation process. This bias is therefore distinct from standard measurement error bias in non-spillover settings, which always biases coefficients toward zero.

Another type of mismeasurement occurs if true direct effects depend nonlinearly on treatment status. Many financial shocks have this feature; for example, direct effects often only exist when individuals face hard liquidity, borrowing, or capital constraints (Brunnermeier and Sannikov 2014; Giroud and Mueller 2017, 2019; Cloyne et al. 2019). Researchers may not be aware of underlying nonlinearity and instead mismeasure treatment using a linear regressor. For concreteness, imagine a model where the true spillover is zero and the true direct effect only occurs for observations where the direct treatment variable is positive. I simulate such models and find that spillover estimates can be much larger than direct estimates, falsely suggesting that group-level effects are primarily driven by spillovers rather than direct treatment. One particular form of spillover are network effects. I show that mechanical bias due to mismeasurement also applies to network estimation in

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out mean method applies generally, whenever treatment varies across individuals and across a group of connected firms.

## Appendix A.

I turn to detecting and overcoming mechanical biases. To detect mechanical biases (due to both multiple spillovers and mismeasurement), I argue that researchers can test for heterogeneous effects. Economic theory often predicts which firms should be unaffected by a given type of spillover. For example, tradable firms do not respond to local demand spillovers (Moretti 2010; Mian and Sufi 2014; Giroud and Mueller 2017, 2019). If estimated regional demand spillovers are zero for tradable firms and only exist for non-tradable firms, as theory predicts, spillover estimates are unlikely to be mechanically biased. If instead estimated spillovers are of similar magnitude for all types of firms, then mechanical bias is likely an issue.

To overcome mechanical biases, I show that researchers can turn to instrumental variables (IV). An instrument needs to be correlated with individual treatment status, but uncorrelated with the treatment status of other firms in the group. Such an instrument solves bias due to both multiple spillovers and mismeasurement. An alternative approach to overcoming bias due to multiple spillovers is to include all relevant group-level leave-out means in the regressions. However, this may be difficult in practice. For one, it is usually not possible to measure all relevant types of connections between firms. For example, firms that use common inputs might generate spillovers onto each other, but detailed data on inputs are not typically available in standard datasets. In addition, the full set of relevant spillover channels is not known *ex ante* and regressions become underpowered with many regressors. Taken together, the findings show that researchers should interpret spillover estimates with caution and carefully address potential mechanical biases.

I illustrate the relevance of the biases and solutions using an application. I study an exogenous lending cut by a large German bank called Commerzbank (Huber 2018). Direct treatment status measures whether a firm had a banking relationship to Commerzbank. Directly treated firms reduced employment when their bank cut lending. Guided by a simple industrial organization model, I initially only test for spillovers among firms in the same product market. I find a significant product market spillover of similar magnitude to the direct effect. However, urban models suggest that local demand and agglomeration forces might also generate spillovers. When I additionally test for a regional spillover, the product market spillover shrinks and becomes insignificant, while the regional spillover is large and significant. This result illustrates that the presence of multiple spillovers can severely misguide conclusions about the nature of spillovers.

These findings leave open the possibility that other, omitted spillover types explain the regional spillover. I investigate this possibility by testing for heterogeneous effects. I identify a subset of sectors that, according to theory, are strongly affected by regional spillovers: non-tradable sectors (due to local demand) and high-R&D sectors (due to local agglomeration effects). I find that regional spillovers are only significant for firms in such sectors and insignificant for other sectors. Mechanical bias would affect all firms, so this heterogeneity suggests that regional spillovers are

not driven by mechanical bias.

Next, I investigate mismeasurement, by introducing measurement error into the direct treatment variable. The direct effect becomes insignificant and close to zero, while the regional spillover more than doubles in size. This falsely suggests that the entire regional effect is driven by spillovers, with directly treated firms not growing any differently to untreated firms. However, the heterogeneity test is particularly useful here. I find that spillovers are large and significant for all types of firms. This reveals that the spillover estimates based on mismeasured data are partially driven by mechanical bias and not by the theoretical forces posited in urban models.

I conclude by discussing the usefulness of direct spillover estimation. The results suggest that one job lost at a directly treated firm led to another 1.6 jobs lost at untreated firms in the same region. This finding implies that realistic general equilibrium models need to include strong regional amplification forces. It also offers lessons for policy. Consider a public lending program targeted at a median treated firm. A naive calculation based only on the direct effect suggests that this program would raise regional employment by 1.2 employees for 100,000 USD of lent funds. In contrast, direct spillover estimation implies much larger gains of 2.8 employees. The latter calculation requires knowledge of both direct and spillover effects and would not be possible based only on regional estimates.

## II Related Literature

This paper relates to the methodological discussion in finance and macroeconomics on how to convert estimates derived from micro data to higher or lower levels of aggregation. Most of this literature relies on structural, model-based approaches (Browning et al. 1999; Acemoglu 2010; Nakamura and Steinsson 2018b).<sup>3</sup> The method of direct spillover estimation using (quasi-)experimental variation has traditionally not played a large role. For instance, no paper published in the leading economics and finance journals in 2017 estimates both direct and spillover effects and compares their magnitudes using the method of direct estimation.<sup>4</sup>

In recent years, however, a few papers in all areas of finance and macroeconomics have started using direct spillover estimation, mostly analyzing regional or sectoral spillover (Dupor and McCrory 2018; Huber 2018; Bernstein et al. 2019; Auerbach et al. 2020; Gathmann et al. 2020; Helm

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<sup>3</sup>Recent examples include: Li et al. (2016); Auclert et al. (2018, 2019); Sarto (2018); Beraja et al. (2019); Chodorow-Reich (2019); Chodorow-Reich et al. (2021); Guren et al. (2020); Wolf (2020); Herreño (2021).

<sup>4</sup>See also Berg et al. (2021) for more discussion on publications using differences-in-differences and spillover estimation. The journals published 610 papers in 2017 and are: *American Economic Review*, *Econometrica*, *Journal of Political Economy*, *Quarterly Journal of Economics*, *Review of Economic Studies*, *Journal of Finance*, *Journal of Financial Economics*, *Review of Financial Studies*. Seven papers in these journals explicitly analyze some form of spillover in a quasi-experimental research design. Three of these seven papers are in the subfield of corporate finance and none in the other parts of finance and macroeconomics.

2020; Verner and Gyöngyösi 2020; Conley et al. 2021). In line with this applied work, recent methodological contributions emphasize that spillovers are large in many standard macroeconomic and financial models and that researchers should estimate them (Mian et al. 2019; Berg et al. 2021). But despite this growing interest, there exists little econometric guidance on how researchers can implement spillover estimation. As a result, the applied literature in finance and macroeconomics pays little attention to mechanical biases like multiple spillovers and nonlinearities. While existing papers are well versed in the standard (quasi-)experimental toolkit (e.g., inspecting the IV exclusion restrictions through balancing tests), these tools do not overcome the mechanical biases.

The contribution of this paper is to offer econometric advice tailored to estimating spillovers in finance and macroeconomics. I describe sources of mechanical bias and offer practical solutions. The inherent nature of large-scale financial and macroeconomic shocks makes biases due to multiple spillovers and nonlinearity particularly relevant. First, spillovers operate across multiple overlapping groups and it is not theoretically clear which spillover types are relevant. This makes interpreting spillover results challenging, as I outline in the discussion of multiple spillovers. Second, nonlinear effects are common in financial settings (e.g., due to liquidity constraints or capital thresholds) and many treatment variables are hard to measure (e.g., banking relationships), which can mechanically bias estimates.

The classic econometrics literature emphasizes that spillovers violate the stable unit treatment value assumption (Rubin 1980, 1990) and that spillovers are difficult to estimate in the absence of exogenous variation (Manski 1993; Moffitt et al. 2001; Glaeser et al. 2003; Bramoullé et al. 2009). Subsequent work develops techniques to optimally estimate spillovers with randomized controlled trials (RCTs in Duflo and Saez 2003; Hirano and Hahn 2010; Avitabile 2012; Baird et al. 2018; Vazquez-Bare forthcoming) and without data on group memberships (Manresa 2016; Breza et al. 2020). Relative to this methodological work, the aim of this paper is to give practical guidance on econometric problems that arise frequently in applied finance and macroeconomics, but are rarely discussed.

Outside of finance and macroeconomics, several applied papers estimate spillovers directly, mainly in education (Ammermueller and Pischke 2009; Epple and Romano 2011; Sacerdote 2011; Angrist 2014; List et al. 2019), development (RCTs in Miguel and Kremer 2004; Angelucci and De Giorgi 2009; Janssens 2011; Muralidharan et al. 2017; Cunha et al. 2019; Filmer et al. 2021; Egger et al. forthcoming), and public economics (Blundell et al. 2004; Rincke and Traxler 2011; Crépon et al. 2013; Ferracci et al. 2014; Lalive et al. 2015; Gautier et al. 2018; Boning et al. 2020). The types of spillovers analyzed in these papers differ from common settings in finance and macroeconomics. First, multiple spillovers are typically not a challenge in these papers because all relevant spillover types are ex-ante defined and observed by the authors.<sup>5</sup> Second, sharp non-

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<sup>5</sup>In education economics, the typical object of interest are peer effects operating within a classroom or school.

linear effects are theoretically and empirically relevant especially for financial shocks, because of liquidity, borrowing, and capital constraints, so mechanical bias due to nonlinearity is more common in financial contexts. These two differences may explain why issues of multiple spillovers and nonlinearity have not played a large role in applied spillover papers outside of finance and macroeconomics.

### III Empirical Framework

#### III.A Basic Model of Direct and Spillover Effects

Consider an economic shock that affects firms or households with varying intensity, as indicated by their “treatment status.” For example, if the shock is a credit supply disruption, treatment status is a firm’s dependence on failing banks. If the shock is fiscal stimulus, treatment status measures whether firms or households receive a stimulus check.

Economic theory suggests that the treatment status of a given firm or household can affect the outcomes of other firms and households. For instance, if two firms are located in the same region, they hire on the same local labor market. When one firm is treated, it may change its labor demand, thereby affecting local wages. If two firms sell substitute products, they are competitors. When a competitor is treated, product prices may change, affecting all firms in the sector. In general, whenever firms are in some way connected, the treatment status of one firm can generate spillovers onto other firms. Similarly, whenever households are connected, there can be cross-household spillovers. I henceforth use “firms” to describe the object of study, but the analysis applies equally when households or other entities are directly treated.

While in reality there are many channels that connect firms, to simplify exposition, I assume that there are just two: firms are connected either if they operate in the same region or in the same product market sector. The treatment status of an individual firm  $i$  in region  $r(i)$  and sector  $s(i)$  is given by  $x_i$ . An outcome, such as firm investment or employment growth, is given by  $y_i$ . Assuming linearity, the relationship between outcome and treatment status of various firms is:

$$y_i = \beta x_i + \sum_{j \neq i, r(j)=r(i)} \gamma^j x_j + \sum_{k \neq i, s(j)=s(i)} \lambda^k x_k + \alpha + \varepsilon_i. \quad (1)$$

The first coefficient  $\beta$  is the direct effect of individual treatment ( $x_i$ ) on the outcome. The direct effect represents by how much the outcome would change if firm  $i$  alone was treated. In addition,

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In development economics, units are usually self-contained villages (i.e., “largely closed local economies,” as put by Egger et al. (forthcoming)). In public economics, researchers typically focus on policy that locally affects well-defined labor markets or social groups. In all these setting, spillovers operate chiefly through the pre-defined group of interest rather than through other groups, unlike in macroeconomics and finance where cross-regional sectors, financial markets, input-output chains, etc. play a role.



there are spillover effects  $\gamma^j$  and  $\lambda^k$ . Each spillover effect represents by how much outcome  $y_i$  of firm  $i$  would change if another firm in the same region (firm  $j$  with treatment status  $x_j$ ) or in the same sector (firm  $k$  with treatment status  $x_k$ ) was treated.

Throughout the paper, I assume that treatment of all firms is exogenous to the error, such that  $E(x_i \varepsilon_i) = 0 \forall i$ . This implies that bias does not arise due to standard “endogeneity” issues of treatment being correlated with other determinants of the outcome (as in Manski’s (1993) reflection problem). Instead, bias will arise mechanically due to the issues involved in constructing and estimating spillover coefficients.

The superscripts on the coefficients  $\gamma^j$  and  $\lambda^k$  indicate that spillover effects are firm-specific, since spillovers arising from two different firms are not necessarily identical. It is, however, difficult to estimate one spillover coefficient per firm in the data. Instead, researchers commonly assume that spillovers are identical for firms in the same sector or region, which facilitates estimation:

$$\gamma^j = \frac{\gamma}{N_{r(j)} - 1} \forall j, \quad (2)$$

$$\lambda^k = \frac{\lambda}{N_{s(j)} - 1} \forall k. \quad (3)$$

The number of firms in a region and sector is  $N_{r(j)}$  and  $N_{s(j)}$ , respectively. Intuitively, the assumptions imply that the greater the number of firms in a region or sector, the less important the region- or sector-level spillovers generated by an individual firm.

Under these assumptions, the outcome depends on only three coefficients: individual treatment status and two “leave-out means”:

$$y_i = \beta x_i + \gamma \overline{x_{r(i)}} + \lambda \overline{x_{s(i)}} + \alpha + \varepsilon_i. \quad (4)$$

The leave-out mean  $\overline{x_{r(i)}}$  is the average treatment status of all other firms in region  $r(i)$  apart from firm  $i$ :

$$\overline{x_{r(i)}} = \frac{\sum_{j \neq i, r(j)=r(i)} x_j}{N_{r(i)} - 1} \quad (5)$$

and  $\overline{x_{s(i)}}$  is defined analogously.

The coefficients  $\gamma$  and  $\lambda$  are the region- and sector-level spillovers. They measure the change in the outcome of firm  $i$  if the average exposure of other firms in its region or sector increases. The direct effect (i.e., the change if firm  $i$  alone is treated) is given by  $\beta$ . A useful way to report magnitudes are the ratios of spillover to direct effects,  $\frac{\gamma}{\beta}$  and  $\frac{\lambda}{\beta}$ .<sup>6</sup>

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<sup>6</sup>Alternatively, researchers may prefer to report the share of the total effect due to general equilibrium spillovers. For instance, if spillover leave out-means are uncorrelated ( $\text{Corr}(\overline{x_{r(i)}}, \overline{x_{s(i)}}) = 0$ ), the share of the regional total effect

Spillover coefficients on their are often hard to interpret because they do not capture absolute changes, but relative treatment effects in relation to a control firm for whom direct treatment and leave-out means are all zero.<sup>7</sup>

The assumptions in equations 2 and 3 imply that spillovers are identical across firms in a group. Alternatively, researchers may prefer assuming that spillovers are activity-weighted (e.g., that firms with more workers generate larger spillovers). The framework above can easily be adapted to incorporate this assumption. Treatment can be defined at the level of individual workers, so that  $x_{pi}$  measures the treatment status of worker  $p$  employed at firm  $i$ . The direct treatment status of a firm is given by the average of the treatment status of all workers at firm  $i$ :

$$\tilde{x}_i = \frac{\sum_{p \in i} x_{pi}}{\tilde{N}_i},$$

where the number of workers at firm  $i$  is  $\tilde{N}_i$ . (If treatment is determined at the firm level,  $x_{pi}$  is identical for all workers at firm  $i$ , so that  $\tilde{x}_i = x_i$ , where  $x_i$  is simply the treatment status of the firm from equation 4.) If we then assume that spillovers are identical for workers in the same sector or region, the model becomes:

$$y_i = \tilde{\beta} \tilde{x}_i + \tilde{\gamma} \widetilde{x_{r(i)}} + \tilde{\lambda} \widetilde{x_{s(i)}} + \tilde{\alpha} + \tilde{\epsilon}_i.$$

The regional leave-out mean is the average treatment of all workers employed by other firms in a region:

$$\widetilde{x_{r(i)}} = \frac{\sum_{j \neq i, r(j)=r(i)} x_{pj}}{\widetilde{N_{r(i)}} - \tilde{N}_i}, \quad (6)$$

where the total number of workers in the region is  $\widetilde{N_{r(i)}}$  and  $\widetilde{x_{s(i)}}$  can be defined analogously.

### III.B Variation in Treatment Is Exogenous

I assume that individual treatment status as well as treatment status of firms in the same region and sector is exogenous to all other determinants of firm outcomes:

$$E(x_i \epsilon_i) = 0 \quad \forall i.$$

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driven by spillovers is  $\frac{\gamma}{\beta + \gamma}$ . This fact can be seen by taking expectations of equation 4 over regions.

<sup>7</sup>In the example using regions and sectors,  $\gamma$  and  $\lambda$  measure direct and spillover effects relative to a firm that was not directly exposed to the shock ( $x_i = 0$ ) and in whose region and sector no other firm was directly exposed to the shock ( $\widetilde{x_{r(i)}} = \widetilde{x_{s(i)}} = 0$ ). This means, the coefficients do not capture the total difference in firm outcomes relative to a world where the shock did not happen. Instead, they capture the effect of treatment relative to firms that were treated neither directly nor through spillovers. See Chodorow-Reich (2020) for a formal analysis of relative versus absolute effects, which is not the focus of this paper.

In practice, exogenous variation means that researchers have either experimentally randomized treatment status or identified quasi-random variation. As a result of this assumption, all estimation issues described below are not driven by the usual endogeneity concerns about correlations between treatment and unobserved errors (Manski 1993; Moffitt et al. 2001). As shown below, the issues I discuss are more subtle and depend on the distribution of treatment across regions and sectors.

Exogenous variation is a high bar in practice. In many studies, variation in direct treatment may be exogenous within region and sector, but variation in treatment of firms in the same region and sector is not. For instance, exposure to failing banks may be exogenous when comparing firms within regions, but the distribution of failing banks across regions may be correlated with other shocks to firm growth. In such cases, the group definition fails the exogeneity criterion and cannot be used to estimate region-level spillover effects.

### III.C Treatment May Vary Systematically Across Regions and Sectors

I assume that direct treatment status depends on several random variables:

$$x_i = u_{r(i)} + u_{s(i)} + z_i + v_i, \quad (7)$$

where  $u_{r(i)}$  is a common factor for all firms in region  $r(i)$  and  $u_{s(i)}$  is a common factor for all firms in sector  $s(i)$ . The other components vary at the individual level:  $z_i$  is an observed variable, which is uncorrelated within regions and sectors and can serve as instrument for  $x_i$ , and  $v_i$  is an unobserved random error. The variables  $u_{r(i)}$ ,  $u_{s(i)}$ ,  $z_i$ , and  $v_i$  are uncorrelated with each other and with the error  $\varepsilon_i$  in equation 4.

If  $u_{r(i)}$  is identical across regions and  $u_{s(i)}$  is identical across sectors, treatment status does not vary systematically across regions and sectors. However, variation across regions and sectors is systematic in most research designs. Variation is always systematic in experiments where researchers intentionally treat some groups more than others. In most naturally occurring settings, variation is also systematic. For instance, exposure to the 2008/09 credit crisis varied systematically across regions and sectors because banks tend to specialize in certain regions and sectors, rather than picking borrowers at random (Chodorow-Reich 2014; Bentolila et al. 2018; Huber 2018). As a result, certain areas and sectors were systematically more exposed to failing banks. Similarly, fiscal stimulus tends to be concentrated in specific regions (Chodorow-Reich 2019).

On the positive side, systematic variation guarantees that there is a large degree of variation across regions and sectors when the number of firms per region and sector is large, making it easier to estimate spillovers. In contrast, when variation across regions and sectors is not systematic, there will be hardly any variation in large samples, making it hard to precisely estimate spillovers.

The challenge is that naturally occurring systematic variation is often not exogenous. The factors generating systematic variation may also drive differences in firm outcomes across groups. For example, failing banks might be more likely to operate in regions with low growth potential. This would generate a correlation between the leave-out mean and other shocks to firm growth (correlation between  $u_{r(i)}$  and the error term in equation 4). For the purpose of this paper, I leave aside concerns of exogeneity and focus on other estimation issues.

### III.D Setup for the Simulations

I investigate the properties of spillover estimates by running simulations. In each simulation, I randomly sort 5,000 observations (indexed by  $i$ ) into 500 equally-sized regions and 500 equally-sized sectors. In the baseline simulations, I assume that the region and sector terms  $u_{r(i)}$  and  $u_{s(i)}$  are both independently and log-normally distributed with mean 0 and standard deviation 1. This implies that variation is systematic across regions and sectors in the baseline simulations. In additional simulations, I assume that variation is not systematic, in which case  $u_{r(i)}$  and  $u_{s(i)}$  are zero.  $\varepsilon_i$ ,  $z_i$ , and  $v_i$  are normally distributed with mean 0 and standard deviation 1. Throughout the paper, I report coefficients and standard errors averaged over 100 simulations.

## IV Bias Due to Multiple Potential Spillovers

Having laid out the empirical framework, I highlight the difficulties that arise when estimating spillovers. In this section, I show that spillover estimates can be biased if there are multiple potential spillover types and make practical suggestions on how to investigate bias.

### IV.A Testing the Wrong Type of Spillover

I assume that there is no true spillover within sectors, but a spillover within regions with a coefficient of one. The true data-generating process is thus:

$$y_i = x_i + \overline{x_{r(i)}} + \varepsilon_i. \quad (8)$$

Treatment varies systematically across regions and sectors (i.e.,  $u_{r(i)}$  and  $u_{s(i)}$  in equation 7 are not identical across regions and sectors).

Researchers may not include all relevant spillovers in their specification. Theoretical models often focus on one type of spillover mechanism. For instance, industrial economists focus on competition, so their research question might only consider spillovers within product markets. Financial economists study credit reallocation, so they might only be interested in spillovers among

borrowers of the same bank. Based on theory, researchers may be drawn to empirically investigating only one type of spillover, even if that spillover does not appear in the true model.

Measurement difficulties are another reason why researchers may overlook relevant spillover types. Some economic connections between firms are not recorded in standard datasets. For example, the default of one firm might generate capital constraints for a lender, but lender identities are often not observed in the data. In practice, the range of possible spillover channels is large. As a result, researchers may not be able to include all relevant spillover forces in their specifications.

#### IV.B Bias Due to Testing the Wrong Type of Spillover

Testing for a spillover with zero coefficient while omitting a true spillover biases estimates. The bias arises even if the included and omitted leave-out means are not correlated. The lack of correlation makes this form of biased spillover estimates less salient and detectable relative to standard forms of omitted variable bias. In equation 8, the regional and sectoral leave-out means are uncorrelated by construction, so it is not obvious that the coefficient on the regional leave-out mean should be biased.

To illustrate the effects of ignoring relevant spillovers, I use the simulated data based on equation 8 and run regressions that only contain direct treatment status  $x_i$  and the sectoral leave-out mean  $\bar{x}_{s(i)}$ . The true ratio of regional spillover to direct effect is a positive 100 percent. In contrast, the estimated sectoral spillover coefficient on  $\bar{x}_{s(i)}$  is negative and significant (Table I, column 1). The ratio of estimated spillover to direct effect is large at -33 percent. The focus on the wrong spillover therefore changes the sign of estimated spillovers and leads to a severe misinterpretation of economic forces.

The reason for the bias is the presence of systematic variation across regions and sectors. When  $x_i$  and  $\bar{x}_{s(i)}$  are the only regressors, the omitted  $\bar{x}_{r(i)}$  enters the error term. Both  $x_i$  and the omitted  $\bar{x}_{r(i)}$  are functions of the regional factor  $u_{r(i)}$  (equation 7). As a result,  $x_i$  and the error term are positively correlated, which biases the estimated coefficient on  $x_i$ . The spillover estimate is then also biased because  $x_i$  and  $\bar{x}_{r(i)}$  are positively correlated (due to the common factor  $u_{r(i)}$ ).

#### IV.C Investigating Bias Due to Multiple Spillover Types

Instrumental variables can solve the bias. Ideally, researchers identify an instrument at the individual level, such as  $z_i$  (as described in equation 7). The instrument needs to be correlated with individual treatment status  $x_i$ , but uncorrelated with the treatment status of other firms in the group (i.e., uncorrelated with  $u_{r(i)}$ ). The sectoral leave-out mean  $\bar{x}_{s(i)}$  can then serve as instrument for  $\bar{x}_{s(i)}$ . Coefficients based on instrumenting for  $x_i$  and  $\bar{x}_{s(i)}$  using  $z_i$  and  $\bar{x}_{s(i)}$  are consistent (Table I, column 2). In the absence of an instrument at the individual level, researchers can still estimate

the spillover coefficient consistently by using an instrument for only the leave-out mean  $\overline{z_{s(i)}}$  and controlling for  $x_i$ .

An obvious alternative solution to the bias is to control for other potential spillover types. This is feasible in the simulation exercise because the regional leave-out mean is observable (column 3). However, in many cases, not all potential spillover types are observable, as discussed earlier.

Identifying instrumental variables and controlling for other spillover types are ideal solutions, but may be practically infeasible. But researchers can still make progress in such cases. The bias due to testing the wrong type of spillover appears mechanically in all subgroups of firms and households because of the way leave-out means are constructed. But in many settings, economic theory predicts that spillovers should not exist among a certain subgroup. For instance, firms selling non-tradable goods are affected by regional demand shocks, but firms selling tradables are not (Mian and Sufi 2014). The spillover coefficient for tradable producers should be zero if regional demand drives spillovers. If the estimated spillover on tradable producers is indeed zero, researchers can conclude that the non-zero spillover estimate on other firms is not a mechanical bias due to including the wrong type of spillover. If instead significant spillovers show up for all firm types, the spillover estimates are likely biased.

Finally, note that multiple spillover types do not lead to bias if there is no systematic group-level variation (column 4). This requires that both  $u_r$  and  $u_s$  are identical across regions and sectors, respectively (equation 7). However, this condition is often not met in large-scale shocks, as outlined in Section III.C.

#### IV.D Bias Due to Multiple Non-Zero Spillovers

The bias is not limited to the case where a spillover with zero coefficient is included in the model. In an additional simulation, I assume that spillovers operate within regions and sectors with a coefficient of one. The true data-generating process is thus:

$$y_i = x_i + \overline{x_{r(i)}} + \overline{x_{s(i)}} + \varepsilon_i. \quad (9)$$

However, as above, researchers only include the sectoral leave-out mean, possibly because they follow a model focused on product market competition or because they are unable to observe firm region. The direct effect is biased upward and sectoral spillover downward (Table II, column 1). While the true ratio is 100 percent, the estimated ratio is 29 percent. IV (column 2) and controlling for all relevant spillover types (column 3) overcome the bias. In the absence of these solutions, tests for heterogeneous effects based on theory are also an attractive approach.

## V Bias Due to Mismeasurement

In this section, I outline how mismeasurement of treatment status biases spillover estimates. I describe two cases: classical measurement error and mismeasurement due to nonlinear effects.

### V.A Definition of Measurement Error

To illustrate the role of classical error, I assume that there is only a regional spillover, given by  $\gamma$ , so that the true data-generating process is:

$$y_i = \beta x_i + \gamma \overline{x_{r(i)}} + \varepsilon_i. \quad (10)$$

Imagine that direct treatment status  $x_i$  is measured with error. Observed treatment status is:

$$x_i^* = x_i + \eta_i.$$

Measurement error  $\eta_i$  is normally distributed with mean 0 and standard deviation  $\sigma$ . It is uncorrelated with  $\varepsilon_i$ ,  $u_{r(i)}$ ,  $u_{s(i)}$ ,  $z_i$ , and  $v_i$ . The leave-out mean is constructed from individual-level data, so measurement error affects the observed leave-out mean too:

$$\overline{x_{r(i)}}^* = \overline{x_{r(i)}} + \overline{\eta_{r(i)}}.$$

The distortion caused by measurement error can be measured using the signal-to-total variance ratio, which is:

$$STV = \frac{V[x_i]}{V[x_i^*]}.$$

The greater the standard deviation of the measurement error, the lower the information content of the observed variable.

### V.B Bias Due to Measurement Error

Using simulated data, I illustrate how estimates of spillovers depend on classical error. I generate data based on equation 10, assuming that there is no spillover effect ( $\gamma = 0$ ). In the absence of measurement error ( $STV = 1$ ), the regression results are consistent. The estimated direct effect (coefficient on  $x_i^*$ ) is close to one and significant, while the estimated spillover (coefficient on  $\overline{x_{r(i)}}^*$ ) is small and insignificant (Table III, panel A, column 1).

With low measurement error ( $STV = 0.95$ ), the spillover becomes statistically significant. The ratio of spillover to direct effect rises to 5 percent (column 2). The greater the measurement error, the greater the spillover estimate. Bound and Krueger (1991) document that measurement error

in earnings growth in the Current Population Survey leads to  $STV = 0.7$ . The ratio of spillover to direct effect is 223 percent with  $STV = 0.7$  (column 4). Hence, with an empirically plausible degree of measurement error, the estimated spillover is more than twice as large as the estimated direct effect, even though the true spillover is 0.

The intuitive reason for the overestimated spillover is the presence of systematic group-level variation (i.e., the variation in  $u_{r(i)}$ ). The individual measurement error partially gets averaged out when calculating  $\overline{x_{r(i)}}^*$ . As a result,  $\overline{x_{r(i)}}^*$  contains relatively less measurement error than  $x_i^*$  and relatively more information about the group-level component  $u_{r(i)}$ . That means some of the true direct effect (the part that is caused by high  $u_{r(i)}$ ) shows up in the spillover estimate.

### V.C The Direction of Bias Due to Measurement Error

The examples so far showed that measurement error can inflate a spillover estimate when the true spillover is zero. In general, measurement error can cause bias in either direction. Algebraically, the spillover estimate from specification 10 converges to:

$$plim \hat{\gamma} = \beta C_1 + \gamma C_2,$$

where  $0 \leq C_1$ ;  $0 \leq C_2 \leq 1$ ; and  $C_1 = 0$  if  $u_{r(i)}$  is identical across regions.<sup>8</sup>

This equation shows that the spillover estimate is always attenuated if variation is not systematic (i.e.,  $u_{r(i)}$  is identical across regions). If there is systematic variation (i.e.,  $u_{r(i)}$  varies across regions), the relative magnitude of direct and spillover effects determines the bias. If the true direct effect is non-zero and the true spillover is zero ( $\beta \neq 0$  and  $\gamma = 0$ ), the direction of bias of the spillover estimate has the sign of the direct effect. If the true direct effect is zero and the true spillover is non-zero ( $\beta = 0$  and  $\gamma \neq 0$ ), the spillover estimate is attenuated.

To illustrate this result, I generate data where the true direct and spillover effects are both one ( $\beta = \gamma = 1$ ). Under systematic variation, the spillover is overestimated (Table III, panel B, column 1). Under random group-level variation ( $u_{r(i)} = 0$ ), the spillover is attenuated (column 2).

### V.D Bias Due to Nonlinear Direct Effects

Nonlinear responses to shocks are common in financial settings. For instance, liquidity-constrained households extract housing equity when house prices go up, but do not inject equity when house prices fall (Cloyne et al. 2019). Similarly, large losses in bank capital have disproportionate effects on lending and real outcomes, relative to small losses (Brunnermeier and Sannikov 2014).

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<sup>8</sup>The full derivation and definitions of  $C_1$  and  $C_2$  are in Appendix B.



Researchers may not be aware of the underlying data generating process, however, and mis-measure direct treatment status. Standard practice is to use linear regressors. This introduces a similar bias as classical measurement error. I illustrate this bias by specifying the true data generating equation as:

$$y_i = w_i + \varepsilon_i,$$

where  $w_i$  is a nonlinear variable based on an observable  $x_i$ :

$$w_i = \begin{cases} x_i & \text{if } x_i > 0, \\ 0 & \text{otherwise.} \end{cases}$$

The true spillover effects in the model are zero.

If researchers correctly account for the nonlinear relationship between  $y_i$  and  $x_i$ , the regression produces consistent estimates. The estimated direct coefficient on  $w_i$  is close to one and significant, while the regional spillover coefficient on  $\overline{w_{r(i)}}$  is small and insignificant (Table IV, column 1).

If researchers incorrectly use a linear regressor, the estimated spillover on the linear leave-out mean is positive and significant (column 2). The ratio of estimated spillover to direct effect is 20 percent. This result falsely suggests that spillover effects played an important role in amplifying the effects of the shock. The ratio of estimated spillover to direct effect rises with the degree of nonlinearity. For instance, I redefine:

$$w_i = \begin{cases} x_i^2 & \text{if } x_i > 0, \\ 0 & \text{otherwise.} \end{cases}$$

The correctly specified regressors are still consistently estimated (column 3). However, using the linear regressors leads to an estimated ratio of 166 percent (column 4). This estimated ratio incorrectly implies that the spillover is quantitatively more important than the direct effect.

The reason for the overestimated spillover is that the specification with linear regressors fits the same coefficient for observations with  $x_i > 0$  and for observations with  $x_i \leq 0$ . As a result, the direct estimate is too low for observations with  $x_i > 0$  (relative to the true effect). With systematic variation (i.e.,  $u_{r(i)}$  differs across groups), some of the true direct effect for observations with  $x_i > 0$  (the part that is caused by high  $u_{r(i)}$ ) loads on the coefficient on the leave-out mean and generates bias. The bias gets worse with the degree of nonlinearity, as the wedge between true and estimate direct effect rises. With random variation (i.e.,  $u_{r(i)}$  identical across groups), using linear regressors does not produce a biased spillover estimate because there is no common component in direct exposure that could load onto the leave-out mean (columns 5 and 6).

## **V.E Investigating Bias Due to Mismeasurement**

As with multiple spillovers, IV overcomes the bias from mismeasurement. Using  $z_i$  as individual-level instrument (equation 7), the IV estimates are consistent if there is measurement error (Table III, column 5) or if direct effects are nonlinear (Table IV, column 7). A natural solution to nonlinearity is to relax the linearity assumption. For instance, plotting direct effects by bins of  $x_i$  should reveal which parts of the distribution of  $x_i$  are treated.

Testing for heterogeneous spillovers, based on theory, is a useful tool. If spillovers are only significant for a subset of firms, for which theory predicts they should be, generic bias due to mismeasurement across all firm types cannot explain the spillover results.

## **VI Application: Estimating Spillovers Following a Banking Shock**

In this section, I illustrate that mechanical biases due to multiple spillover types and mismeasurement can be large in practice. I study a real-world application by estimating spillovers following a bank lending cut. I then inform a policy calculation using the estimated spillovers.

### **VI.A Empirical Setting and Data**

I analyze a lending cut by Commerzbank, the second-largest German bank in 2008. Commerzbank primarily lent to German firms and households. It suffered severe losses on its international financial investments during the financial crisis 2008/09, having held positions in US mortgage markets and failing Icelandic banks. Importantly, the losses were not caused by Commerzbank's lending to the German economy. German firms borrowing from Commerzbank were of comparable credit quality and on similar growth paths compared to firms borrowing from other banks.

Nonetheless, Commerzbank's crisis affected its German borrowers. As Commerzbank became financially constrained in 2008/09, it cut lending to German firms. Finding another lender is difficult for firms, especially in a time of crisis, as documented by a large literature on relationship banking (Sharpe 1990; Boot 2000). As a result, German firms borrowing from Commerzbank faced a reduction in their loan supply and grew more slowly after the lending cut. In contrast, aggregate lending by other German banks actually increased slightly during the crisis.

Recent papers analyze the effect of Commerzbank's lending cut on firms (Huber 2018; Berg et al. 2021; Biermann and Huber 2021). To summarize, the evidence suggests that Commerzbank's lending cut was exogenous to the German economy, so that firms, product markets, and regions with greater dependence on Commerzbank would have grown at the same rates as other firms, had the lending cut not happened. Firms with a Commerzbank relationship became financially constrained and grew employment more slowly after the lending cut, compared to firms borrowing

from other banks. In addition, firms grew more slowly when a large share of other firms in the region had a Commerzbank relationship.

I construct a firm-level dataset following Huber (2018). Direct treatment status  $x_i$  is a binary indicator for whether a firm had a relationship to Commerzbank in 2006, measured using a confidential record of German firms' relationship banks by the credit rating agency Creditreform.<sup>9</sup> The outcome is the symmetric growth rate of firm employment between 2008 and 2012, calculated using the database Dafne by Bureau van Dijk.

I calculate leave-out means to test for spillovers at the level of two groups: product markets and regions. The share of other firms with a Commerzbank relationship (leave-out mean) in the product market is  $\overline{x_{s(i)}}$  and the share in the region is  $\overline{x_{r(i)}}$ . Regions are defined as administrative counties (*Kreise*) where firms are located. Product markets are defined as industry cells (at the level of two-digit industries in the German WZ classification) for tradable firms and industry-region cells for non-tradable firms (since they sell locally).<sup>10</sup>

For the purpose of this paper, I take as starting point that firms with a relationship to Commerzbank experienced an exogenous shock after Commerzbank's lending cut. I therefore take as given the identification assumption, which is that direct treatment status as well as product market and region leave-out means are uncorrelated with other shocks hitting firms. Detailed arguments in favor of this assumption are presented in the above-cited papers.

## VI.B Bias Due to Multiple Potential Spillovers

I begin with an analysis that an economist interested in product markets might conduct. Theory suggests that firms may benefit from increased market share when firms in the same product market are treated, but may also suffer from lower technological spillovers (Greenstone et al. 2010; Bloom et al. 2013; Giroud et al. 2021). To test the net effect of these opposing channels, I regress firm employment growth between 2008 and 2012 on direct treatment status and the product market leave-out mean. The coefficients on both direct treatment and market leave-out mean are statistically significant, negative, and of equal magnitude (Table V, column 1). This suggests that the spillover is as large as the direct effect in a market where all firms are treated. Taken at face value, the finding supports theoretical models where reduced technological spillovers play an important role in amplifying crises.

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<sup>9</sup>Bank relationships are available for 112,344 firms. German firms and banks usually form long-lasting relationships, as only 1.7 percent of firms add a new bank per year (Dwenger et al. 2015). This system of relationship banking facilitates credit provision during good times, but makes it more difficult to access credit when the bank cuts lending.

<sup>10</sup>Following Mian and Sufi (2014), I classify an industry as tradable if it exports at least 10,000 USD per worker, 500 USD million in total, or if the industry's regional Herfindahl index is in the top quartile (using U.S. industry data). The Herfindahl criterion uses the fact that tradable industries are geographically concentrated because they do not need to produce where they sell.

Economic theory suggests that there may be other spillovers, however. At the regional level, the sign of the spillover is also theoretically ambiguous. Firms may suffer from reductions in local demand and agglomeration forces when firms in the same region are treated, but may benefit from lower local wages (Ellison et al. 2010; Moretti 2010; Mian and Sufi 2014; Giroud and Mueller 2017, 2019). Including the regional leave-out mean in the specification strongly changes the conclusions. The estimated market spillover shrinks toward zero and becomes statistically insignificant (column 2). The estimated regional spillover is large and significant, consistent with models that include strong local demand and agglomeration effects, but inconsistent with large spillovers through product markets.

These findings highlight that a specification testing only for the market spillover leads researchers to misinterpret spillover forces. Consistent with the earlier conceptual discussion, spillover estimates are misleading if a relevant spillover is not included in the specification. Unlike in the case of standard omitted variable bias, such bias can arise even if the different leave-out means are uncorrelated. This implies that researchers should include all potential spillover forces in their specification, even when they are orthogonal to the leave-out mean of interest.

However, this poses practical difficulties. Many group connections are not reported. For instance, the data used here do not include information on whether firms use common inputs. Directly treated firms may generate spillovers onto other firms that use common inputs. The regional spillover estimate may be biased because the specification does not consider spillovers among common input users.

To get around this difficulty, researchers can test for heterogeneous spillover effects based on theory. Regional models predict that non-tradable producers and innovative firms with high R&D are strongly affected by local shocks, while other firms are not (Jaffe et al. 1993; Henderson 2003). If regional spillovers are present in equal measure among all types of firms, it is likely that the estimates are mechanically biased. However, if regional spillovers are zero for firms in tradable and low-R&D sectors, as theory predicts, spillover estimates are not driven by a generic mechanical bias. Splitting the sample, I find that the regional spillover is significant and large for non-tradable and high R&D sectors (column 3), but it is small and insignificant for tradable and low-R&D sectors (column 4). This suggests that the regional spillover is not an artifact of mechanical bias. In general, identifying a placebo category of firms, where spillovers should be zero, is a useful way for researchers to ensure that spillovers are not mechanically biased.

## **VI.C Bias Due to Measurement Error**

I next explore the impact of measurement error. Both spillover and direct effect are significant in a specification without measurement error. The ratio of spillover to direct effect is 4.6 (Table VI, column 1). Direct treatment status is a binary variable in this application, so I add measurement

error by misclassifying a random subset of the sample: 5 percent of observations are misclassified with low measurement error; 10 percent with medium; and 30 percent with high. I calculate the regional leave-out mean based on the mismeasured direct treatment status, as researchers in practice would.

The estimated ratio of spillover to direct effect rises with the magnitude of measurement error, from 6.7 with low error to 28.4 percent with high error (columns 2-4). These findings show that the intuition derived from the simulations has practical relevance. Measurement error attenuates the direct effect, so part of the direct effect falsely loads onto the spillover coefficient. In fact, with high error, the direct coefficient becomes insignificant and close to zero (column 4). Researchers using mismeasured data would erroneously conclude that local general equilibrium forces account for essentially all of the impact of a shock on a region.

Researchers can explore heterogeneous effects based on theory to test whether mechanical bias drives the spillover estimate. As above, I split the sample by the degree to which firms should be affected by local spillovers. With high measurement error, I find that spillovers are large and significant for both types of firms (columns 5 and 6). This finding should raise concern among researchers testing for regional spillovers. It suggests that mechanical bias plagues the estimates and that results are not driven by the theoretical forces described in urban models. Finding an appropriate instrument is one potential avenue to solving the issue. In the case of classical measurement error, any other variable that measures the same treatment would be an option, even if this instrument is also measured with error. In the absence of an instrument and heterogeneity tests, researchers should interpret spillover estimates with caution.

## **VI.D Magnitude of Regional Spillovers**

The results suggest that an untreated firm in a median region (with 24 percent of other firms treated) grew by 2.7 percentage points less solely because of regional spillovers (Table V, column 2). The spillover effect in the median region is of equal magnitude to the direct effect, which is also estimated at 2.7 percentage points. Spillovers thus played a first-order role in the regional impact of the lending cut.

The spillover estimate can be represented as a job-for-job effect: the employment change of untreated firms relative to the employment change of directly treated firms. Untreated firms in the median region experienced just the spillover effect, an employment decline of 2.7 percentage points. Treated firms experienced both spillover and direct effects, an employment decline of 5.4 percentage points. The elasticity of untreated employment with respect to treated employment is thus 0.5. Multiplying the elasticity by the ratio of untreated to treated employment in the median region (which is 3.2) yields a job-for-job spillover of 1.6. For each job lost at directly treated firms, 1.6 jobs are lost at untreated firms.

## **VI.E Policy Calculation Based on Spillovers**

Spillover estimates can be useful in the analysis of government policy. Consider a stabilization policy that allows Commerzbank to continue lending to a median borrower.<sup>11</sup> The direct effects of Commerzbank's lending cut approximately lowered the median borrower's number of employees by one and bank debt by 90,243 USD.<sup>12</sup> By providing 90,243 USD for Commerzbank to lend to a median firm, the government could undo the direct effect and increase employment of the treated firm by one. Regional employment would then increase by an additional 1.6 employees, using the earlier estimate of the job-for-job spillover. This implies that, by providing 100,000 USD, the government would increase regional employment by 2.8 employees.

The estimate of 2.8 employees is close to recent estimates of the effect of fiscal stimulus. For instance, the impact of the 2009 American Recovery and Reinvestment Act, averaged across studies, was 2.1 jobs per 100,000 USD of stimulus (Chodorow-Reich 2019). However, in contrast to fiscal stimulus, the government would recoup most funds lent to Commerzbank's borrowers in subsequent years, because firm delinquencies remain below 10 percent even in recessions. This makes the lending policy relatively effective from a net present value perspective.

Note that estimates of direct and spillover effects are key for this type of policy analysis. We need an estimate of the direct effect to measure the funds required to offset the initial shock to treated firms. And then we need to know the spillover effect to estimate the impact on other firms. If we only knew the total impact of the lending cut on the region, we could not evaluate a policy targeted at directly treated firms. If we only knew the direct effect, we would significantly understate the benefit of the policy by ignoring the large spillovers.

## **VII Conclusion**

Large-scale macroeconomic and financial shocks affect firms and households through many complex spillover channels. By using direct spillover estimation, researchers can test which general equilibrium connections need to feature in models and how empirical estimates from one level of aggregation can inform other levels of aggregation.

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<sup>11</sup>The German government in fact conducted a policy in this spirit. It aimed to stabilize loan supply to German firms by injecting capital and purchasing a 25 percent stake in Commerzbank through its government fund Soffin. Despite these measures, Commerzbank still reduced lending. Commerzbank was the only large nationwide lender in Germany to be subsidized by Soffin. Only three other, specialized banks received capital from Soffin (two real estate banks, Aareal Bank and Hypo Real Estate Group, and the Landesbank West LB/Portigon), which shows that Commerzbank was relatively strongly affected by the crisis.

<sup>12</sup>The median firm in the sample had 36 employees and held 880,424 USD in bank debt (598,928 Euro using the 2008 average exchange rate) in 2008. The direct effect on employment was roughly 2.7 percent (Table V, column 2) and on bank debt was 10.25 percent (Table 4, column 3 of Huber 2018). Multiplying the percentage impact by the initial value yields the absolute changes of 1 employee and 90,243 USD in bank debt.

However, direct spillover estimation requires careful implementation. Spillover estimates suffer from distinct sources of mechanical bias that are not sufficiently discussed in applied research. For example, spillover estimates can be of the wrong sign, large, and statistically significant if additional spillover types operate through channels outside of the empirical model. Mismeasurement, such as classical measurement error or nonlinear direct effects, can lead to large and significant spillover estimates even if the true model contains zero spillovers.

Mechanical biases are particularly relevant for researchers studying large-scale financial and macroeconomic shocks because these settings feature many types of spillover channels, nonlinear effects are common, and measurement is difficult. An application to a real-world credit cut highlights that mechanical bias can be large in a real-world setting. Researchers may form completely erroneous judgments about which spillover channels are important, for example, by concluding that there are large sectoral spillovers when, in fact, true sectoral spillovers are zero and regional spillovers are large. Fortunately, several practical tools allow researchers to detect and overcome mechanical bias. Testing for heterogeneous effects, instrumental variables, and flexible functional forms directly address the problems.

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## Tables

Table I: Testing for the wrong spillover biases estimates

	(1)	(2)	(3)	(4)
Coefficient on $x_i$ (true coefficient = 1)	1.626*** (0.059)	0.995*** (0.037)	0.999*** (0.008)	0.998*** (0.012)
Coefficient on $\overline{x_{s(i)}}$ (true coefficient = 0)	-0.530*** (0.051)	-0.012 (0.127)	0.001 (0.009)	0.004 (0.033)
Coefficient on $\overline{x_{r(i)}}$ (true coefficient = 1)			1.000*** (0.009)	
Group-level variation Estimator	OLS	Systematic IV	OLS	Random OLS

Notes: The variable  $x_i$  is the direct treatment status of firm  $i$ , which is in sector  $s(i)$  and region  $r(i)$ ; and  $\overline{x_{s(i)}}$  and  $\overline{x_{r(i)}}$  are the average treatment status of all other firms in  $s(i)$  and  $r(i)$ , respectively, apart from firm  $i$  (leave-out means). The IV specification in column 2 instrument for  $x_i$  and  $\overline{x_{s(i)}}$  using  $z_i$  and  $\overline{z_{s(i)}}$ . Systematic variation means that  $u_{s(i)}$  and  $u_{r(i)}$  (from equation 7) are log-normally distributed with mean 0 and standard deviation 1. Random variation indicates that  $u_{s(i)}$  and  $u_{r(i)}$  are 0 for every firm. The reported coefficients and standard errors are averaged over 100 simulations.

Table II: Testing for just one type of spillover biases estimates

	(1)	(2)	(3)	(4)
Coefficient on $x_i$ (true coefficient = 1)	1.626*** (0.059)	0.995*** (0.037)	0.999*** (0.008)	0.998*** (0.012)
Coefficient on $\overline{x_{s(i)}}$ (true coefficient = 1)	0.470*** (0.051)	0.988*** (0.127)	1.001*** (0.009)	1.004*** (0.033)
Coefficient on $\overline{x_{r(i)}}$ (true coefficient = 1)			1.000*** (0.009)	0.999*** (0.009)
Group-level variation Estimator	OLS	Systematic IV	OLS	Random OLS

Notes: The variable  $x_i$  is the direct treatment status of firm  $i$ , which is in sector  $s(i)$  and region  $r(i)$ ; and  $\overline{x_{s(i)}}$  and  $\overline{x_{r(i)}}$  are the average treatment status of all other firms in  $s(i)$  and  $r(i)$ , respectively, apart from firm  $i$  (leave-out means). The IV specification in column 2 instrument for  $x_i$  and  $\overline{x_{s(i)}}$  using  $z_i$  and  $\overline{z_{s(i)}}$ . Systematic variation means that  $u_{s(i)}$  and  $u_{r(i)}$  (from equation 7) are log-normally distributed with mean 0 and standard deviation 1. Random variation indicates that  $u_{s(i)}$  and  $u_{r(i)}$  are 0 for every firm. The reported coefficients and standard errors are averaged over 100 simulations.

Table III: Mismeasurement due to classical error biases spillover estimates

Panel A: Specifications with zero true spillover effect					
	(1)	(2)	(3)	(4)	(5)
Coefficient on $x_i^*$ (true coefficient = 1)	0.999*** (0.009)	0.863*** (0.010)	0.754*** (0.010)	0.469*** (0.009)	1.000*** (0.029)
Coefficient on $\overline{x_{r(i)}}^*$ (true coefficient = 0)	-0.000 (0.011)	0.129*** (0.012)	0.229*** (0.013)	0.474*** (0.019)	0.001 (0.103)
Measurement error Estimator	None OLS	Low OLS	Medium OLS	High OLS	High IV

Panel B: Specifications with true spillover effect

	(1)	(2)
Coefficient on $x_i^*$ (true coefficient = 1)	0.521 (0.009)	0.700 (0.011)
Coefficient on $\overline{x_{r(i)}}^*$ (true coefficient = 1)	1.365 (0.032)	0.693 (0.045)
Measurement error Estimator	High OLS	High OLS
Group-level variation	Systematic	Random

Notes: The variable  $x_i$  is the direct treatment status of firm  $i$ , which is in sector  $s(i)$  and region  $r(i)$ ; and  $\overline{x_{r(i)}}$  is the average treatment status of all other firms in  $r(i)$ , apart from firm  $i$  (leave-out means). An asterisk indicates that the variable is observed and may contain measurement error. The signal-to-total-variance ratio of  $x_i$  is 95 percent for low measurement error, 90 percent for medium measurement error, and 70 percent for high measurement error. The IV specification in panel A, column 5 instruments for  $x_i^*$  and  $\overline{x_{r(i)}}^*$  using  $z_i$  and  $\overline{z_{r(i)}}$ . Systematic variation means that  $u_{s(i)}$  and  $u_{r(i)}$  (from equation 7) are log-normally distributed with mean 0 and standard deviation 1. Random variation indicates that  $u_{s(i)}$  and  $u_{r(i)}$  are 0 for every firm. The reported coefficients and standard errors are averaged over 100 simulations.

Table IV: Mismeasurement due to nonlinearity biases spillover estimates

	(1)	(2)	(3)	(4)	(5)	(6)	(7)
Coefficient on $w_i$ (true coefficient = 1)	1.002*** (0.012)		1.000*** (0.002)		1.002*** (0.017)		
Coefficient on $\overline{w_{r(i)}}$ (true coefficient = 0)	-0.002 (0.013)		-0.000 (0.002)		-0.004 (0.051)		
Coefficient on $x_i$ (true coefficient > 0)		0.793*** (0.013)		4.594*** (0.363)		0.503*** (0.012)	0.773*** (0.021)
Coefficient on $\overline{x_{r(i)}}$ (true coefficient = 0)		0.148*** (0.016)		7.648*** (2.025)		-0.003 (0.032)	-0.019 (0.102)
Regressor correctly specified	Yes	No	Yes	No	Yes	No	No
Definition of $w_i$	$w_i = x_i \text{ if } x_i > 0$	$w_i = x_i \text{ if } x_i > 0$	$w_i = x_i^2 \text{ if } x_i > 0$	$w_i = x_i^2 \text{ if } x_i > 0$	$w_i = x_i \text{ if } x_i > 0$	$w_i = x_i \text{ if } x_i > 0$	$w_i = x_i \text{ if } x_i > 0$
Group-level variation	OLS	OLS	OLS	OLS	OLS	OLS	IV
Group-level variation	Systematic	Systematic	Systematic	Systematic	Random	Random	Systematic

Notes: In columns 1, 2, 5, and 6,  $w_i = x_i \text{ if } x_i > 0$  and  $w_i = 0 \text{ if } x_i \leq 0$ . In columns 3 and 4,  $w_i = x_i^2 \text{ if } x_i > 0$  and  $w_i = 0 \text{ if } x_i \leq 0$ . The variable  $x_i$  is the direct treatment status of firm  $i$  in region  $r(i)$  and sector  $s(i)$ ; and  $\overline{x_{r(i)}}$  is the average treatment status over all other firms in region  $r(i)$ , apart from firm  $i$  (leave-out mean). The variable  $\overline{w_{r(i)}}$  is the leave-out mean of  $w_i$  in region  $r(i)$ , where  $w_i$  is defined as described in the column. The IV specification in column 7 instruments for  $x_i$  and  $\overline{x_{r(i)}}$  using  $z_i$  and  $\overline{z_{r(i)}}$ . Systematic variation means that  $u_{r(i)}$  (from equation 7) is log-normally distributed with mean 0 and standard deviation 1. Random variation indicates that  $u_{r(i)}$  is 0 for every firm. The reported coefficients and standard errors are averaged over 100 simulations.

Table V: Application: Testing for the wrong spillover

	(1)	(2)	(3)	(4)
Coefficient on $x_i$	-0.030*** (0.007)	-0.027*** (0.007)	-0.031** (0.013)	-0.026*** (0.009)
Coefficient on $\overline{x_{s(i)}}$	-0.030* (0.018)	-0.015 (0.018)	-0.045 (0.031)	-0.007 (0.024)
Coefficient on $\overline{x_{r(i)}}$		-0.114** (0.051)	-0.213*** (0.077)	-0.067 (0.055)
Sectors in sample	All sectors		Non-tradable and high R&D	Tradable and low R&D
Observations	45,252	45,252	14,810	30,442

Notes: The variable  $x_i$  is the direct treatment status of firm  $i$ , which is in sector  $s(i)$  and region  $r(i)$ ; and  $\overline{x_{s(i)}}$  and  $\overline{x_{r(i)}}$  are the average treatment status of all other firms in  $s(i)$  and  $r(i)$ , respectively, apart from firm  $i$  (leave-out means). All specifications control for firm log age, export share (fraction of exports out of total revenue), import share (fraction of imports out of total costs) and fixed effects for four firm size bins (1–49, 50–249, 250–999, and over 1,000 employees), industry fixed effects at the level of the one-digit WZ classification; and a fixed effect for firms in the former GDR. Standard errors are clustered by region.

Table VI: Application: Measurement error

	(1)	(2)	(3)	(4)	(5)	(6)
Coefficient on $x_i^*$	-0.027*** (0.007)	-0.023*** (0.006)	-0.024*** (0.006)	-0.009 (0.006)	-0.021** (0.010)	-0.004 (0.007)
Coefficient on $\overline{x_{r(i)}}^*$	-0.123** (0.050)	-0.155*** (0.054)	-0.160*** (0.058)	-0.256*** (0.086)	-0.346*** (0.128)	-0.214** (0.094)
Measurement error	None	Low	Medium	High	High	High
Sectors in sample		All sectors			Non-tradable and high R&D	Tradable and low R&D
Observations	45,252	45,252	45,252	45,252	14,810	30,442

Notes: The variable  $x_i^*$  is the observed direct treatment status of firm  $i$  in region  $r(i)$ ; and  $\overline{x_{r(i)}}^*$  is the average observed treatment status of all other firms in  $r(i)$ , apart from firm  $i$  (leave-out means). The binary variable is misclassified for a random 5 percent of observations in the case of low, 10 percent in the case of medium, and 30 percent in the case of high measurement error. All specifications control for firm log age, export share (fraction of exports out of total revenue), import share (fraction of imports out of total costs) and fixed effects for four firm size bins (1–49, 50–249, 250–999, and over 1,000 employees), industry fixed effects at the level of the one-digit WZ classification; and a fixed effect for firms in the former GDR. Standard errors are clustered at the regional level.

# Online Appendix

## Appendix A Estimating Spillover Effects Through Networks

The estimation issues studied in the paper are relevant for researchers using variation at the individual and group level to estimate spillovers. In this section, I show that similar issues apply to the estimation of spillover effects through networks. Network analysis requires slightly different notation, but the intuition is similar. I then explicitly show how measurement error and nonlinear direct effects can bias the estimates of network spillovers.

### Appendix A.A Setup of a Network

Researchers often study how networks amplify shocks. For instance, an active literature focuses on the transmission of firm-level shocks to other firms, through production or financial linkages (Barrot and Sauvagnat 2016; Boehm et al. 2019; Carvalho and Tahbaz-Salehi 2019; Carvalho et al. 2020; Tintelnot et al. 2020). For the sake of concreteness, I describe the following analysis using the language of supply linkages in production networks, but the insights are more general.

A typical specification to analyze production networks is:

$$y_i = \theta x_i + \delta \overline{x_{(i)}} + \varepsilon_i, \quad (\text{A1})$$

where  $y_i$  is a firm-level outcome and  $x_i$  is the direct treatment status of firm  $i$ . The average treatment status of firms that are direct suppliers to firm  $i$  is:

$$\overline{x_{(i)}} = \frac{\sum_{j \neq i} (x_j \cdot \mathbb{1}\{j \text{ supplies to } i\})}{N_i}, \quad (\text{A2})$$

where  $\mathbb{1}\{j \text{ supplies to } i\}$  indicates whether firm  $j$  is a supplier to firm  $i$ . The number of suppliers to firm  $i$  is  $N_i$ . In the general network case and in all simulations below, links are directed, so that a link from  $j$  to  $i$  ( $j$  supplies  $i$ ) does not imply that there is also a link from  $i$  to  $j$ .<sup>A1</sup>

The key assumption is how direct treatment status is determined. I specify that:

$$x_i = r_i + \sum_{j \neq i} (r_j \cdot \mathbb{1}\{j \text{ supplies to } i\}) + u_i. \quad (\text{A3})$$

The first term  $r_i$  is a random factor associated with firm  $i$ . The second term is the sum of all factors associated with the suppliers to firm  $i$ . The third term  $u_i$  is a random error. The variables  $r_i$ ,  $\varepsilon_i$ , and  $u_i$  are uncorrelated, and each component is independently distributed across firms.

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<sup>A1</sup>The model in equation A1 can be generalized to include not just the treatment status of direct links, but also the treatment status of second order links (i.e., the treatment status of a supplier's supplier) and further higher order links (as in Carvalho et al. 2020). The intuition below also applies to such higher order analyses.



The second term implies that the treatment status of each firm is correlated with the treatment status of its suppliers. Such correlated treatment status occurs naturally if the creation of supply links is correlated with the process determining treatment status. For instance, if firms linked to the same supplier happen to be located in the same region (as in the case of sectoral clustering) and if treatment status is regionally concentrated (as in the case of natural disasters), then treatment status can be approximated by equation A3. Note that treatment status is still exogenous (i.e., uncorrelated with the error term  $\varepsilon_i$  in equation A1). Correlated treatment status simply means that the process determining treatment status is not exogenous to supply links. In experimental settings, treatment status is less likely to be correlated with suppliers' treatment status because researchers can randomize treatment status independently of regional concentration or other types of clustering.

### Appendix A.B Effects of Measurement Error on Network Spillover Estimates

To highlight the consequences of measurement error in network analysis, I run 100 simulations. In each simulation, I generate a random network among 500 firms with density 0.002. This implies that firms have on average one supplier, with a standard deviation of one. I assume that  $r_i$  is log-normally distributed with mean 0 and standard deviation 1. The error terms  $\varepsilon_i$  and  $u_i$  are drawn from a normal distribution with mean 0 and standard deviation 0.1.

I generate data where the true direct effect is one ( $\theta = 1$ ) but the network spillover effect is zero ( $\delta = 0$ ). If treatment status is measured without error, a regression of the firm outcome on  $x_i$  and  $\bar{x}_{(i)}$  produces consistent estimates (Table A.I, column 1). However, with measurement error, the network spillover effect is positive and significant (column 2).<sup>A2</sup> The ratio of network spillover to direct effect is 24 percent.

The intuitive reason for the bias in the network analysis is similar to above. There is a common factor in direct treatment status and supplier's treatment status. The common factor is relatively stronger, and measurement error is relatively weaker, in the measure of suppliers' treatment status. As a result, some of the true direct effect loads onto the spillover estimate.

### Appendix A.C Effects of Nonlinear Direct Effects on Network Spillover Estimates

The network spillover estimate can also be biased if the true direct effect is nonlinear. To analyze the impact of nonlinearity, I define:

$$w_i = \begin{cases} x_i^2 & \text{if } x_i > 0, \\ 0 & \text{otherwise.} \end{cases}$$

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<sup>A2</sup>The specification of measurement error is the same as in Section V.A above. Direct treatment status  $x_i$  can only be measured with error, such that  $x_i^* = x_i + \eta_i$ . Measurement error  $\eta_i$  is drawn from a normal distribution with mean 0 and standard deviation  $\sigma$ . It is uncorrelated with  $\varepsilon_i$ ,  $r_i$ , and  $u_i$ . I set  $\sigma$  so that the signal-to-total variance ratio equals 0.7.

Table A.I: Estimates of network spillovers are biased under measurement error and nonlinear direct effects

	(1)	(2)	(3)	(4)
Coefficient on $x_i^*$ (true coefficient = 1)	1.000 (0.001)	0.656 (0.042)		0.411 (0.050)
Coefficient on $\bar{x}_{(i)}^*$ (true coefficient = 0)	0.000 (0.002)	0.158 (0.036)		0.077 (0.021)
Coefficient on $w_i$ (true coefficient = 1)			1.000 (0.003)	
Coefficient on $\bar{w}_{(i)}$ (true coefficient = 0)			0.000 (0.004)	
Measurement error	No	Yes	No	No
True direct effects are nonlinear	No	No	Yes: $w_i = x_i^2$ if $x_i > 0$	

Notes: In columns 1 and 2, the true data generating equation is  $y_i = x_i + \varepsilon_i$ . The variable  $x_i^*$  is the observed direct treatment status of firm  $i$  and  $\bar{x}_{(i)}^*$  is the observed average treatment status over all suppliers of firm  $i$ . The variables are measured correctly in columns 1, 3, and 4. The variables are measured with error in column 2, so that the signal-to-total-variance ratio of  $x_i$  is 0.7. In columns 3 and 4, the true data generating equation is  $y_i = w_i + \varepsilon_i$ , where  $w_i = x_i^2$  if  $x_i > 0$  and  $w_i = 0$  if  $x_i \leq 0$ . The reported coefficients and standard errors are averaged over 100 simulations.

Direct treatment status  $x_i$  is determined as in equation A3 above.<sup>A3</sup> I assume that the true direct effect of  $w_i$  is one ( $\theta = 1$ ) and the network spillover effect is zero ( $\delta = 0$ ), so that the true data generating process is given by:

$$y_i = w_i + \varepsilon_i. \quad (\text{A4})$$

If researchers specify the nonlinear relationship between  $x_i$  and  $y_i$  correctly, the regression produces consistent estimates (Table A.I, column 3). But if researchers use linear regressors, as is standard practice, the estimates are biased and the ratio of network spillover to direct effect is 19 percent (column 4).

The reason for the bias is, once again, the factor  $r_i$  that is common to the direct treatment status of firm  $i$  and suppliers' treatment status. The coefficient on  $x_i$  estimates a linear direct effect. Conditional on this linear effect, there remains a nonlinear correlation between suppliers' treatment status and the outcome  $y_i$ , induced by the factor  $r_i$  in suppliers' treatment status. This leads to a significant, large, and inconsistent estimate of the network spillover.

<sup>A3</sup>The random network and other random terms also follow the calibration above. The only difference is that the mean of the random error  $u_i$  is negative for the purpose of this section (equal to the negative of the 90th percentile of the distribution of  $r_i + \sum_{j \neq i} (r_j \cdot \mathbb{1}\{j \text{ supplies to } i\})$ ). If this mean was not negative, almost all observations would have positive  $x_i$  and there would not be a nonlinear direct effect of  $x_i$  and  $y_i$ .

## Appendix B Derivation of the Bias Due to Measurement Error

The true model is:

$$y_i = \beta x_i + \gamma \overline{x_{r(i)}} + \varepsilon_i. \quad (\text{A5})$$

Direct treatment status  $x_i$  is measured with error. The observed variables are:

$$\begin{aligned} x_i^* &= x_i + \eta_i = u_{r(i)} + z_i + v_i + \eta_i, \\ \overline{x_{r(i)}^*} &= \overline{x_{r(i)}} + \overline{\eta_{r(i)}} = \overline{u_{r(i)}} + \overline{z_{r(i)}} + \overline{v_{r(i)}} + \overline{\eta_{r(i)}}. \end{aligned}$$

I assume that the variables  $\varepsilon_i$ ,  $u_{r(i)}$ ,  $z_i$ , and  $v_i$  are uncorrelated with each other.

The OLS estimator of  $\gamma$  is:

$$\begin{aligned} \hat{\gamma} &= \frac{\sum_i \left( \overline{x_{r(i)}^*} - \overline{\overline{x_{r(i)}^*}} \right) (y_i - \overline{y_i}) \sum_i (x_i^* - \overline{x_i^*})^2 - \sum_i (x_i^* - \overline{x_i^*}) (y_i - \overline{y_i}) \sum_i \left( \overline{x_{r(i)}^*} - \overline{\overline{x_{r(i)}^*}} \right) (x_i^* - \overline{x_i^*})}{\sum_i \left( \overline{x_{r(i)}^*} - \overline{\overline{x_{r(i)}^*}} \right)^2 (x_i^* - \overline{x_i^*})^2 - \left( \sum_i \left( \overline{x_{r(i)}^*} - \overline{\overline{x_{r(i)}^*}} \right) (x_i^* - \overline{x_i^*}) \right)^2} \\ &= \frac{\sum_i \left( \overline{x_{r(i)}^*} - \overline{\overline{x_{r(i)}^*}} \right) (\beta (x_i - \overline{x_i}) + \gamma (\overline{x_{r(i)}} - \overline{\overline{x_{r(i)}}}) + (\varepsilon_i - \overline{\varepsilon_i})) \sum_i (x_i^* - \overline{x_i^*})^2}{\sum_i \left( \overline{x_{r(i)}^*} - \overline{\overline{x_{r(i)}^*}} \right)^2 (x_i^* - \overline{x_i^*})^2 - \left( \sum_i \left( \overline{x_{r(i)}^*} - \overline{\overline{x_{r(i)}^*}} \right) (x_i^* - \overline{x_i^*}) \right)^2} \\ &= \frac{\sum_i (x_i^* - \overline{x_i^*}) (\beta (x_i - \overline{x_i}) + \gamma (\overline{x_{r(i)}} - \overline{\overline{x_{r(i)}}}) + (\varepsilon_i - \overline{\varepsilon_i})) \sum_i \left( \overline{x_{r(i)}^*} - \overline{\overline{x_{r(i)}^*}} \right) (x_i^* - \overline{x_i^*})}{\sum_i \left( \overline{x_{r(i)}^*} - \overline{\overline{x_{r(i)}^*}} \right)^2 (x_i^* - \overline{x_i^*})^2 - \left( \sum_i \left( \overline{x_{r(i)}^*} - \overline{\overline{x_{r(i)}^*}} \right) (x_i^* - \overline{x_i^*}) \right)^2} \\ &= \frac{\sum_i \left( \beta (x_i - \overline{x_i}) \left( \overline{x_{r(i)}^*} - \overline{\overline{x_{r(i)}^*}} \right) + \gamma (\overline{x_{r(i)}} - \overline{\overline{x_{r(i)}}}) \left( \overline{x_{r(i)}^*} - \overline{\overline{x_{r(i)}^*}} \right) + (\varepsilon_i - \overline{\varepsilon_i}) \left( \overline{x_{r(i)}^*} - \overline{\overline{x_{r(i)}^*}} \right) \right) \sum_i (x_i^* - \overline{x_i^*})^2}{\sum_i \left( \overline{x_{r(i)}^*} - \overline{\overline{x_{r(i)}^*}} \right)^2 (x_i^* - \overline{x_i^*})^2 - \left( \sum_i \left( \overline{x_{r(i)}^*} - \overline{\overline{x_{r(i)}^*}} \right) (x_i^* - \overline{x_i^*}) \right)^2} \\ &= \frac{\sum_i (\beta (x_i - \overline{x_i}) (x_i^* - \overline{x_i^*}) + \gamma (\overline{x_{r(i)}} - \overline{\overline{x_{r(i)}}}) (x_i^* - \overline{x_i^*}) + (\varepsilon_i - \overline{\varepsilon_i}) (x_i^* - \overline{x_i^*})) \sum_i \left( \overline{x_{r(i)}^*} - \overline{\overline{x_{r(i)}^*}} \right) (x_i^* - \overline{x_i^*})}{\sum_i \left( \overline{x_{r(i)}^*} - \overline{\overline{x_{r(i)}^*}} \right)^2 (x_i^* - \overline{x_i^*})^2 - \left( \sum_i \left( \overline{x_{r(i)}^*} - \overline{\overline{x_{r(i)}^*}} \right) (x_i^* - \overline{x_i^*}) \right)^2}, \end{aligned} \quad (\text{A6})$$

where the first equality is the definition of the OLS estimator with two regressors. The second equality comes from substituting the true equation A5 for  $y_i$ . The third equality comes from rearranging terms.

The probability limit of the OLS estimator is:

$$\begin{aligned}
plim \hat{\gamma} &= \frac{\left( \beta Cov \left( x_i, \overline{x_{r(i)}} \right) + \gamma Cov \left( \overline{x_{r(i)}}, \overline{x_{(i)}} \right) + Cov \left( \varepsilon_i, \overline{x_{r(i)}} \right) \right) V \left( x_i^* \right)}{V \left( \overline{x_{r(i)}} \right) V \left( x_i^* \right) - Cov \left( \overline{x_{r(i)}}, x_i^* \right)^2} \\
&\quad - \frac{\left( \beta Cov \left( x_i, x_i^* \right) + \gamma Cov \left( \overline{x_{r(i)}}, x_i^* \right) + Cov \left( \varepsilon_i, x_i^* \right) \right) Cov \left( \overline{x_{r(i)}}, x_i^* \right)}{V \left( \overline{x_{r(i)}} \right) V \left( x_i^* \right) - Cov \left( \overline{x_{r(i)}}, x_i^* \right)^2} \\
&= \frac{\left( \beta V \left( u_{r(i)} \right) + \gamma \left( V \left( u_{r(i)} \right) + \frac{V(z_i) + V(u_i)}{\bar{N} - 1} \right) \right) \left( V \left( u_{r(i)} \right) + V \left( z_i \right) + V \left( u_i \right) + V \left( \eta_i \right) \right)}{\left( V \left( u_{r(i)} \right) + V \left( z_i \right) + V \left( u_i \right) + V \left( \eta_i \right) \right) \left( V \left( u_{r(i)} \right) + \frac{V(z_i) + V(u_i) + V(\eta_i)}{\bar{N} - 1} \right) - V \left( u_{r(i)} \right)^2} \\
&\quad - \frac{\left( \gamma \left( V \left( u_{r(i)} \right) + V \left( z_i \right) + V \left( u_i \right) \right) + \gamma \left( V \left( u_{r(i)} \right) \right) \right) V \left( u_{r(i)} \right)}{\left( V \left( u_{r(i)} \right) + V \left( z_i \right) + V \left( u_i \right) + V \left( \eta_i \right) \right) \left( V \left( u_{r(i)} \right) + \frac{V(z_i) + V(u_i) + V(\eta_i)}{\bar{N} - 1} \right) - V \left( u_{r(i)} \right)^2}
\end{aligned}$$

where the first equality comes from substituting covariances and variances for the probability limits of the individual terms in equation A6. The second equality comes from solving for the covariances and variances.  $\bar{N}$  is the average number of firms per group. Finally, rearranging gives:

$$\begin{aligned}
plim \hat{\gamma} &= \beta \frac{(\bar{N} - 1) V \left( u_{r(i)} \right) V \left( \eta_i \right)}{\left( V \left( z_i \right) + V \left( u_i \right) + V \left( \eta_i \right) \right)^2 + \bar{N} V \left( u_{r(i)} \right) \left( V \left( z_i \right) + V \left( u_i \right) + V \left( \eta_i \right) \right)} \\
&\quad + \gamma \frac{(\bar{N} - 1) V \left( u_{r(i)} \right) \left( V \left( z_i \right) + V \left( u_i \right) + V \left( \eta_i \right) \right)}{\left( V \left( z_i \right) + V \left( u_i \right) + V \left( \eta_i \right) \right)^2 + \bar{N} V \left( u_{r(i)} \right) \left( V \left( z_i \right) + V \left( u_i \right) + V \left( \eta_i \right) \right)} \\
&\quad + \gamma \frac{\left( V \left( z_i \right) + V \left( u_i \right) \right) \left( V \left( u_{r(i)} \right) + V \left( z_i \right) + V \left( u_i \right) + V \left( \eta_i \right) \right)}{\left( V \left( z_i \right) + V \left( u_i \right) + V \left( \eta_i \right) \right)^2 + \bar{N} V \left( u_{r(i)} \right) \left( V \left( z_i \right) + V \left( u_i \right) + V \left( \eta_i \right) \right)}.
\end{aligned}$$