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10.5.4-5

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Question:

A small terrace at a football ground comprises of 15 steps each of which is 50 m long and built of solid concrete. Each step has a rise of 1/4 m and a tread of 1/2 m. Calculate the total volume of concrete required to build the terrace. [Hint: Volume of concrete required to build the first step=

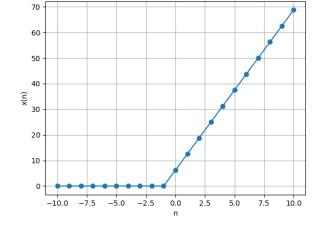
$$V = \frac{1}{4} \cdot \frac{1}{2} \cdot 50 \tag{1}$$

solution:

$$x(n+1) - x(n) = 6.25m^3$$
 (2)

$$y(n) = \frac{n+1}{2} [2x(0) + (n)d]$$
 (3)

$$n = 0 \quad 1 \quad 2 \quad 3 \quad \dots \tag{4}$$



x(n) vs n

Fig. 0: plot x(n) vs n

here

parameter	description	value
x (0)	first term	6.25
d	common difference	6.25
n	no of terms -1	14
x(n)	volume of $(n + 1)$ th step	x(0) + nd

TABLE 0: formula parameters

$$y(14) = \frac{14+1}{2} [12.5 + (14) 6.25]$$
 (5)

$$=\frac{15}{2}\left[12.5 + 87.5\right] \tag{6}$$

$$= (7.5) \cdot 100 \tag{7}$$

$$=750m^3$$
 (8)

convolution for y(n):

$$y(n) = x(n) * u(n)$$
(14)

$$Y(Z) = X(Z)U(Z)$$
(15)

$$X(Z) = \left(\frac{6.25}{1 - z^{-1}} + \frac{6.25z^{-1}}{(1 - z^{-1})^2}\right) \quad |z| > |1| \quad (16)$$

$$U(Z) = \frac{1}{1 - z^{-1}} \quad |z| > |1| \tag{17}$$

$$Y(Z) = \left(\frac{6.25}{1 - z^{-1}} + \frac{6.25z^{-1}}{\left(1 - z^{-1}\right)^2}\right) \left(\frac{1}{1 - z^{-1}}\right)$$
 (18)

$$x(n) \stackrel{Z}{\longleftrightarrow} X(Z)$$
 (9)

$$x(n) = (x(0) + nd) u(n)$$
 (10)

$$X(Z) = \sum_{-\infty}^{\infty} x(n) Z^{-n}$$
(11)

$$= \frac{x(0)}{1 - z^{-1}} + \frac{dz^{-1}}{\left(1 - z^{-1}\right)^2} \qquad |z| > |1| \qquad (12)$$

$$= \frac{6.25}{1 - z^{-1}} + \frac{6.25z^{-1}}{(1 - z^{-1})^2} \qquad |z| > |1| \qquad (13)$$