10.5.4-5

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Question:

A small terrace at a football ground comprises of 15 steps each of which is 50 m long and built of solid concrete. Each step has a rise of 1/4 m and a tread of 1/2 m. Calculate the total volume of concrete required to build the terrace. [Hint: Volume of concrete required to build the first step=

$$volume = 1/4 \cdot 1/2 \cdot 50 \tag{1}$$

$S_n = \frac{15}{2} [12.5 + 87.5] \tag{12}$

$$volume = (7.5) \cdot 100 = 750m^3 \tag{13}$$

plot of x(n) and n

$$\mathbf{x}(\mathbf{n}) = (a + n \cdot d) \cdot u(n) \tag{14}$$

solution

parameter	description	value
1	length	50m
b	breadth	0.25m
h	height	0.5m
V	volume	$6.25m^3$

TABLE 0: input parameters

$$l_n = l_{n+1} \tag{3}$$

$$b_n = b_{n+1} \tag{4}$$

$$h_{n+1} - h_n = 0.25 (5)$$

$$V_{n+1} - V_n = 6.25 (6)$$

$$S_n = \frac{n+1}{2} [2a + (n)d] \tag{7}$$

$$n = 0, 1, 2, 3, \dots$$
 (8)

here

parameter	description	value
a	first term	6.25
d	common difference	6.25
n	no of terms -1	14

$$S_n = \frac{14+1}{2}[12.5 + (14)6.25] \tag{10}$$

$$S_n = \frac{15}{2} [12.5(14)6.25] \tag{11}$$

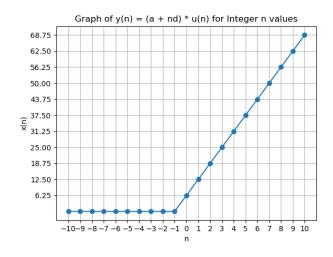


Fig. 1

$$x(n) \stackrel{Z}{\longleftrightarrow} X(Z)$$
 (16)

$$x(n) = (a + nd)u(n) \tag{17}$$

$$X(Z) = \sum_{-\infty}^{\infty} x(n)Z^{-n}$$
 (18)

$$= \frac{x(0)}{1 - z^{-1}} + \frac{dz^{-1}}{(1 - z^{-1})^2}, |z| > |r|$$

(19)

$$= \frac{6.25}{1 - z^{-1}} + \frac{6.25z^{-1}}{(1 - z^{-1})^2}, |z| > |r|$$

(20)