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10.5.4-5

EE23BTECH11033-killana jaswanth

Question:

A small terrace at a football ground comprises of 15 steps each of which is 50 m long and built of solid concrete. Each step has a rise of 1/4 m and a tread of 1/2 m. Calculate the total volume of concrete required to build the terrace. [Hint: Volume of concrete required to build the first step=

$$V = \frac{1}{4} \cdot \frac{1}{2} \cdot 50 \tag{1}$$

solution:

here

parameter	description	value
l	length	50m
b	breadth	0.25m
h	height	0.5m
y (n)	sum of volume	$6.25m^3$

TABLE 0: input parameters

$$x(n+1) - x(n) = 6.25m^3$$
 (2)

$$y(n) = \frac{n+1}{2} \left[2x(0) + (n) d \right]$$
 (3)

$$n = 0, 1, 2, 3, \dots$$
 (4)

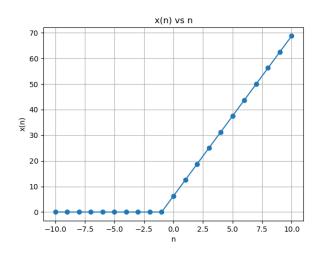


Fig. 0: plot x(n) vs n

$$= (7.5) \cdot 100$$
 (8)

$$=750m^3$$
 (9)

parameterdescriptionvalue
$$x(0)$$
first term6.25 d common difference6.25 n no of terms -114 $x(n)$ volume of $(n + 1)$ th step $x(0) + nd$

TABLE 0: formula parameters

$$y(14) = \frac{14+1}{2} [12.5 + (14) 6.25]$$
 (5)

$$=\frac{15}{2}\left[12.5\left(14\right)6.25\right] \tag{6}$$

$$=\frac{15}{2}\left[12.5 + 87.5\right] \tag{7}$$

$$x(n) \stackrel{Z}{\longleftrightarrow} X(Z)$$
 (10)

$$x(n) = (x(0) + nd) u(n)$$
 (11)

$$X(Z) = \sum_{-\infty}^{\infty} x(n) Z^{-n}$$
 (12)

$$= \frac{x(0)}{1 - z^{-1}} + \frac{dz^{-1}}{(1 - z^{-1})}^{2}, |z| > 1$$
(13)

$$= \frac{6.25}{1 - z^{-1}} + \frac{6.25z^{-1}}{(1 - z^{-1})^2}, |z| > 1$$
(14)

convolution for y(n):

$$y(n) = x(n) * u(n)$$
 (16)

$$x(n) \stackrel{Z}{\longleftrightarrow} X(Z)$$
 (17)

$$u(n) \stackrel{Z}{\longleftrightarrow} U(Z)$$
 (18)

$$y(n) \stackrel{Z}{\longleftrightarrow} Y(Z)$$
 (19)

$$Y(z) = X(z) U(z)$$
 (20)

$$X(z) = \left(\frac{6.25}{1 - z^{-1}} + \frac{6.25z^{-1}}{(1 - z^{-1})^2}\right), |z| > 1$$
(21)

$$U(z) = \frac{1}{1 - z^{-1}}, |z| > 1$$
 (22)

$$Y(z) = \left(\frac{6.25}{1 - z^{-1}} + \frac{6.25z^{-1}}{(1 - z^{-1})^2}\right) \left(\frac{1}{1 - z^{-1}}\right)$$
(23)

$$|z| > 1 \tag{24}$$