10.5.4-5

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Question:
A small terrace at a football ground comprises of 15 steps each of which is 50 m long and built of solid concrete.Each step has a rise of 1/4 m and a tread of 1/2 m. Calculate the total volume of concrete required to build the terrace. [Hint: Volume of concrete required to build the first step=

$$V = \frac{1}{4} \cdot \frac{1}{2} \cdot 50 \tag{1}$$

solution:

$$x(n+1) - x(n) = 6.25m^3 \tag{2}$$

$$y(n) = \frac{n+1}{2}\left[2x(0) + (n)\,d\right] \tag{3}$$

$$n = 0 \quad 1 \quad 2 \quad 3 \quad \ldots \tag{4}$$

here

parameter	description	value
$x(0)$	first term	6.25
d	common difference	6.25
n	no of terms -1	14
$x(n)$	volume of $(n+1)$th step	$x(0)+nd$

TABLE 0: formula parameters

$$y(14) = \frac{14+1}{2}\left[12.5 + (14)\,6.25\right] \tag{5}$$

$$= 750m^3 \tag{6}$$

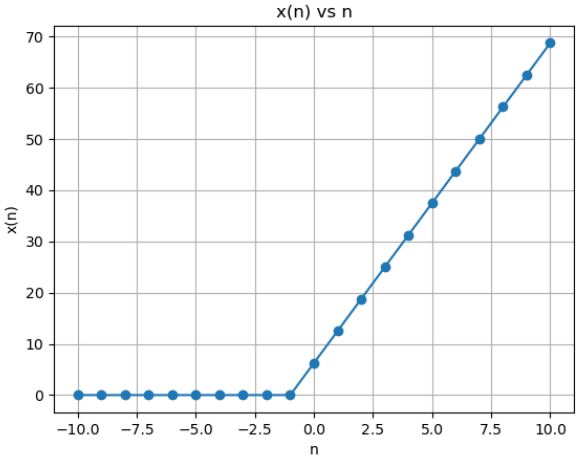

Fig. 0: plot x(n) vs n

$$x(Z) = \frac{x(0)}{1 - z^{-1}} + \frac{dz^{-1}}{(1 - z^{-1})^2} \qquad |z| > |1| \tag{7}$$

$$x(Z) = \frac{6.25}{1 - z^{-1}} + \frac{6.25z^{-1}}{(1 - z^{-1})^2} \qquad |z| > |1| \tag{8}$$

convolution for y(n):

$$Y(Z) = X(Z)\,U(Z) \tag{9}$$

$$U(Z) = \frac{1}{1 - z^{-1}} \qquad |z| > |1| \tag{10}$$

$$Y(Z) = \left(\frac{6.25}{1 - z^{-1}} + \frac{6.25z^{-1}}{(1 - z^{-1})^2}\right)\left(\frac{1}{1 - z^{-1}}\right) \tag{11}$$