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```
clear all; format compact; close all; syms f(x) x y
```

Problem 1 (finished)

Rearrange the following equations to form a strictly diagonally dominant system. Apply two steps of Jacobi and Gauss-Seidel methods starting with the zero vector.

The rearranged diagonally dominant system is

```
syms u v
[1 3; 5 4] * [u;v] == [-1 ; 6]
```

```
ans =
    u + 3*v == -1
    5*u + 4*v == 6
```

solving for u and v $u = (6-4v)/5$, $v = (-1-u)/3$

Using Jacobi method: $[u_0 ; v_0] = [0 ; 0]$ So $[u_1 ; v_1] = [6/5 ; -1/3]$

$[u_2 ; v_2] = [22/15 ; -11/15]$

Gauss-Seidel Method: $[u_0 ; v_0] = [0 ; 0]$ So $[u_1 ; v_1] = [6/5 ; (-1-6/5)/3] = [6/5 ; -11/15]$

$[u_2 ; v_2] = [(6-(-44/15))/5 ; (-1-(134/75))/3] = [134/75 ; -209/225]$

Problem 2 (Yup)

$Ax = b$ using Jacobi method, $(D+R)x = b$ So , $Dx = b-Rx$, and $x = D^{-1}(b-RX)$ Therefore $x_{n+1} = D^{-1}(b-RX_n)$

The Jacobi method for $x_{n+1} = D^{-1}(b-Rx_n)$

$$x_1^{(k+1)} = (b_1 - a_{12}x_2^k - a_{13}x_3^k)/a_{11}$$

$$x_2^{(k+1)} = (b_2 - a_{21}x_1^k - a_{23}x_3^k)/a_{22}$$

$$x_3^{(k+1)} = (b_3 - a_{31}x_1^k - a_{32}x_2^k)/a_{33}$$

$$x_n^{(k+1)} = (b_n - a_{n1}x_1^k - a_{n2}x_2^k - a_{n3}x_3^k)/a_{nn}$$

Therefore the Jacobi method is given for matrix A

