

Contents

- AMSC 460 - HW16
- Problem 1

AMSC 460 - HW16

```
clear all; format compact; close all; syms f(x) x y z
```

Problem 1

(a) Using MATLAB's backslash command, find the solution to the normal equations $A^T A x = A^T b$.

```
A = [1+10^(-8) -1;-1 1;1 -1]
b = [2;1;-1]
```

```
A =
    1.0000    -1.0000
   -1.0000     1.0000
    1.0000   -1.0000
b =
     2
     1
    -1
```

```
AT = A.';
B = AT*A;
C = AT*b;
x1 = B\C
```

```
Warning: Matrix is close to singular or badly scaled. Results may be
inaccurate. RCOND = 2.896879e-17.
```

```
x1 =
    1.0e+07 *
     5.7533
     5.7533
```

(b) Using MATLAB's `\texttt{qr}` command and backslash, find the solution to the triangular system $\hat{R}x = (Q^T b)_{1:n}$. Compare this to the solution to the normal equations. How far apart are the answers? Compute the distance in a norm of your choice.

```
[Q,R] = qr(A)
```

```

Q =
    -0.5774    -0.8165    -0.0000
     0.5774    -0.4082     0.7071
    -0.5774     0.4082     0.7071
R =
    -1.7321     1.7321
         0    -0.0000
         0         0

```

```

Qt = Q.'
D = Qt*b
x2 = R\D
distance = abs(x1-x2)
norm(x1-x2)

```

```

Qt =
    -0.5774     0.5774    -0.5774
    -0.8165    -0.4082     0.4082
    -0.0000     0.7071     0.7071
D =
    -0.0000
    -2.4495
    -0.0000
x2 =
    1.0e+08 *
         3.0000
         3.0000
distance =
    1.0e+08 *
         2.4247
         2.4247
ans =
    3.4290e+08

```

(c) Using MATLAB's `\texttt{cond}` command, what are the condition numbers of A , $A^T A$, and \hat{R} ? Which condition number should we worry about in double precision floating point arithmetic? Which computed answer is more accurate?

```
cond(A)
```

```

ans =
    4.2426e+08

```

Condition number of A , $\kappa(A^T)$

```
cond(B)
cond(R)
% Since all of the items are much larger than 1 so both methods are bad
% Therefore the QR decomposition is more accurate
```

```
ans =
    1.7998e+16
ans =
    4.2426e+08
```