



SIGIR '17, August 07-11, 2017, Shinjuku, Tokyo, Japan

IRGAN: A MINIMAX GAME FOR UNIFYING GENERATIVE AND DISCRIMINATIVE INFORMATION RETRIEVAL MODELS

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INTRODUCTION

FORMULATION

- A minimax Retrieval Framework
- Extension to Pairwise Case
- Discussion
- Links to Existing work

APPLICATION

- Web Search
- Item Recommendation
- Question Answering

EXPERIMENTS

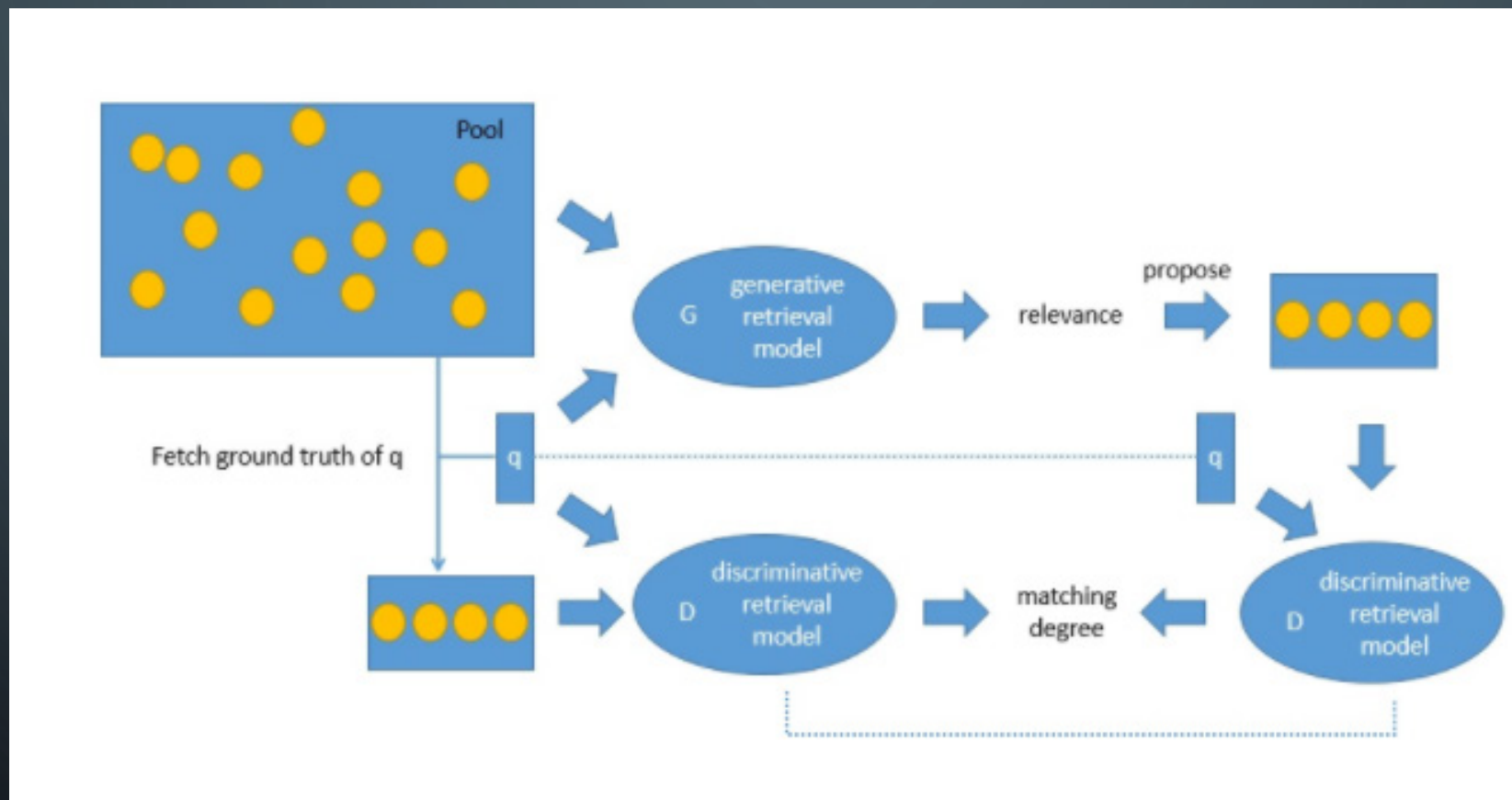
- Web Search
- Item Recommendation
- Question Answering

INTRODUCTION

- Generator solution (relevant) document is generated from a given information need: $q \rightarrow d \rightarrow P(d | q)$
- Statistical language models of text retrieval consider a reverse generative process from a document to a query: $d \rightarrow q \rightarrow P(q | d)$
- Discriminative (classification) solution learned from labelled relevant judgements or their proxies such as clicks or ratings : $q + d \rightarrow r \rightarrow P(d, q)$

- Discriminative model $p_{\phi}(r | q, d)$ aims to maximise the objective function by learning from labelled data
- Generative retrieval model $p_{\vartheta}(d | q, r)$ acts as a challenger who constantly pushes the discriminator to its limit
- Existing approaches generally try to model the interaction between user and system, whereas our approach aims to unify generative and discriminative IR models.

FRAMEWORK



FRAMEWORK

- For a given query q_n , a set of relevant documents labelled, the size of which is much smaller than the total number of documents M .
- true relevance distribution as conditional probability $p_{\text{true}}(d \mid q, r)$, which depicts the (user's) relevance preference distribution over the candidate documents with respect to her submitted query.
- Given a set of samples from $p_{\text{true}}(d \mid q, r)$ observed as the training data

Minimax Retrieval Framework

- **Generative retrieval model** $p_{\theta}(d|q, r)$ which tries to select relevant documents, from the candidate pool for the given query q
- Its goal is to approximate the true relevance distribution $p_{\text{true}}(d|q, r)$ as much as possible.
- **Discriminative retrieval model** $f_{\phi}(q, d)$, discriminate well-matched query-document tuples (q, d) from ill-matched ones, where the goodness of matching given by $f_{\phi}(q, d)$, depends on the relevance of d to q
- Its goal is to distinguish between relevant documents and nonrelevant documents for the query q



• $J^{G^*, D^*} = \min_{\theta} \max_{\phi} \sum_{n=1}^N \left(\mathbb{E}_{d \sim p_{true}(d|q_n, r)} [\log D(d|q_n)] + \mathbb{E}_{d \sim p_{\theta}(d|q_n, r)} [\log(1 - D(d|q_n))] \right)$

Optimising Discriminative Retrieval

- *maximise* the log-likelihood of correctly distinguishing the true and generated relevant documents.
- With the observed relevant documents, and the ones sampled from the current optimal generative model $p_{\theta^*}(d | q, r)$
- $\phi^* = \arg \max_{\phi} \sum_{n=1}^N \left(\mathbb{E}_{d \sim p_{true}(d|q_n, r)} \left[\log \sigma \left(f_{\phi}(d, q) \right) \right] + \mathbb{E}_{d \sim p_{\theta}(d|q_n, r)} \left[\log \left(1 - \sigma \left(f_{\phi}(d, q) \right) \right) \right] \right)$
- where if the function f_{ϕ} is differentiable with respect to ϕ , the above is solved typically by stochastic gradient descent

Optimising Generative Retrieval.

- *minimise* the objective; it fits the underlying relevance distribution over documents $p_{\text{true}}(d | q, r)$, randomly samples documents from the whole document set in order to *fool* the discriminative retrieval model.

Scenario of Reinforcement Learning



Optimising Generative Retrieval.

- $\theta^* = \arg \min_{\theta} \sum_{n=1}^N \left(\mathbb{E}_{d \sim p_{true}(d|q_n, r)} \left[\log \sigma \left(f_{\phi}(d, q) \right) \right] + \mathbb{E}_{d \sim p_{\theta}(d|q_n, r)} \left[\log \left(1 - \sigma \left(f_{\phi}(d, q) \right) \right) \right] \right)$
$$= \arg \max_{\theta} \sum_{n=1}^N \left(\mathbb{E}_{d \sim p_{\theta}(d|q_n, r)} \left[\log \left(1 + \exp \left(f_{\phi}(d, q) \right) \right) \right] \right)$$
- As the sampling of d is discrete, it cannot be directly optimised by gradient descent as in the original GAN formulation.
- A common approach is to use policy gradient based reinforcement learning
- $\mathbb{E}_{d \sim p_{\theta}(d|q_n, r)} \left[\log \left(1 + \exp \left(f_{\phi}(d, q) \right) \right) \right] = J^G(q_n)$

Optimising Generative Retrieval.

policy gradient based reinforcement learning

$$\begin{aligned} & \bullet \nabla_{\theta} J^G(q_n) \\ &= \nabla_{\theta} \mathbb{E}_{d \sim p_{\theta}(d|q_n, r)} \left[\log \left(1 + \exp \left(f_{\phi}(d, q_n) \right) \right) \right] \\ &= \sum_{i=1}^M \nabla_{\theta} p_{\theta}(d_i|q_n, r) \log \left(1 + \exp \left(f_{\phi}(d_i, q_n) \right) \right) \\ &= \sum_{i=1}^M p_{\theta}(d_i|q_n, r) \nabla_{\theta} \log p_{\theta}(d_i|q_n, r) \log \left(1 + \exp \left(f_{\phi}(d_i, q_n) \right) \right) \\ &= \mathbb{E}_{d \sim p_{\theta}(d|q_n, r)} \left[\nabla_{\theta} \log p_{\theta}(d|q_n, r) \log \left(1 + \exp \left(f_{\phi}(d, q_n) \right) \right) \right] \\ &\cong \frac{1}{K} \sum_{k=1}^K \nabla_{\theta} \log p_{\theta}(d_k|q_n, r) \log \left(1 + \exp \left(f_{\phi}(d_k, q_n) \right) \right) \end{aligned}$$

Algorithm 1 Minimax Game for IR (a.k.a IRGAN)

Input: generator $p_{\theta}(d|q, r)$; discriminator $f_{\phi}(\mathbf{x}_i^q)$;
training dataset $\mathcal{S} = \{\mathbf{x}\}$

- 1: Initialise $p_{\theta}(d|q, r), f_{\phi}(q, d)$ with random weights θ, ϕ .
- 2: Pre-train $p_{\theta}(d|q, r), f_{\phi}(q, d)$ using \mathcal{S}
- 3: **repeat**
- 4: **for** g-steps **do**
- 5: $p_{\theta}(d|q, r)$ generates K documents for each query q
- 6: Update generator parameters via policy gradient Eq. (5)
- 7: **end for**
- 8: **for** d-steps **do**
- 9: Use current $p_{\theta}(d|q, r)$ to generate negative examples and combine with given positive examples \mathcal{S}
- 10: Train discriminator $f_{\phi}(q, d)$ by Eq. (3)
- 11: **end for**
- 12: **until** IRGAN converges

- the generator and discriminator can be initialised by their conventional models.

- Eq(5) : $\frac{1}{K} \sum_{k=1}^K \nabla_{\theta} \log p_{\theta}(d_k|q_n, r) \log \left(1 + \exp \left(f_{\phi}(d_k, q_n) \right) \right)$

- Eq(3) : $arg \max_{\phi} \sum_{n=1}^N \left(\mathbb{E}_{d \sim p_{true}(d|q_n, r)} \left[\log \sigma \left(f_{\phi}(d, q) \right) \right] + \mathbb{E}_{d \sim p_{\theta}(d|q_n, r)} \left[\log \left(1 - \sigma \left(f_{\phi}(d, q) \right) \right) \right] \right)$
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Links to Existing Work

- G provides different negative samples to the D training (like negative sampling)
- D's reward signal provides strategic guidance for G training
- G pick documents are regards as negative sample , but pseudo relevance feedback are regards as positive samples
- G will have many iterations , but pseudo relevance feedback usually no further iterations

Web Search

- $x_{q,d} \in R^k$, each dimension represented some value(BM25 、TFIDF 、PageRank)
- $s(q, d) = w_2^T \tanh(W_1 x_{q,d} + b_1) + w_0$

Item recommendation

- Matrix factorisation
- $s(u, i) = b_i + v_u^T v_i$
- b_i = basic item , v_u 、 v_i =latent vector of user and item

Question Answering

- Question and Answer is represented as a sequence of words
- Using CNN or LSTM to learn sequence of words(l-words), each word is embedded as a vector(k-dim), now we have matrix in $R^{l \times k}$
- After CNN get v_q and $v_a \in R^z$, z = number of convolutional kernels.
- $s(q, a) = \cos(v_q, v_a)$

