

EXAM 1

Computer Architecture and Organization

WINTER 2023

Exam 1 , February 22, 2024

- Please make sure your handwriting is clear and legible. This will help us in grading, so you don't lose any points for illegible writing.
- No use of cell phones or any electronic devices
- Two (2) double sided pages of handwritten notes is allowed
- The following pledge is required:

"Honor code: I have neither given nor received unauthorized aid in completing this work."

Name:

Question_1

Compute:

(a) $5_{10} - 3_{10}$ and (b) $3_{10} - 5_{10}$ using 4-bit **two's complement numbers**.

**Honor code: I have neither given nor received unauthorized aid in completing this work. –
May Wandyez**

5(10)	0	1	0	1
3(10)	0	0	1	1
Two's Complement 3(10)	1	1	0	1
Result	0	0	1	0

3(10)	0	0	1	1
5(10)	0	1	0	1
Two's Complement 5(10)	1	0	1	1
Result (add the complement and the 3(10) discard leftmost carry forward)	1	1	1	0

Question_2: Complete the following truth table (few values are provided as hints)

W X Y Z	W'XY	WZ	W'XY+WZ	W'+Z	W+XY	(W'+Z)(W+XY)
0 0 0 0	0	0	0	1	0	0
			0		0	
0 0 1 0	0	0		1		
		0				0
0 1 0 0	0	0	0			0
0 1 0 1	0	0	0	1	0	0
	1			1	1	1
0 1 1 1	1	0	1	1	1	1
				0		
1 0 0 1	0	1				1
1 0 1 0		0		0		0
	0	1			1	1
1 1 0 0				0	1	0
1 1 1 0						
	0		1			1

W	X	Y	Z	W'XY	WZ	W'+Z	W+XY	(W'+Z)(W+XY)
0	0	0	0	0	0	1	0	0
0	0	0	1	0	0	1	0	0
0	0	1	0	0	0	1	0	0
0	0	1	1	0	0	1	0	0
0	1	0	0	0	0	1	0	0
0	1	0	1	0	0	1	0	0
0	1	1	0	1	0	1	1	1
0	1	1	1	1	0	1	1	1
1	0	0	0	0	0	0	1	0
1	0	0	1	0	1	1	1	1
1	0	1	0	0	0	0	1	0
1	0	1	1	0	1	1	1	1
1	1	0	0	0	0	0	1	0
1	1	0	1	0	1	1	1	1
1	1	1	0	0	0	0	1	0
1	1	1	1	0	1	1	1	1

Question_3

Simplify the following two Boolean expressions: Hint (use Demorgan's theorem)

$$F = [(A' + B)'B]'C + B$$

$$F = ((A'+B)' B)' C + B$$

Demorgan's theorem

$$F = (AB'B)' C + B$$

B and not B is always equals to 0

This is then inverted to always equals 1, but C is still required for the AND

$$F = C + B$$

DON'T FORGET TO DO THESE

$$G = [(AB)'(B + C)]'C$$

$$G = ((AB)'(B+C))' C$$

Demorgan's Theorem

$$((AB)'' + (B+C)')C$$

$$(AB + (B+C)')C$$

$$(AB + B'C')C$$

$$ABC + BCC'$$

$$G = ABC$$

Question_4

Find a minimum sum-of-products expression for:

$$F(a, b, c) = \sum m(0, 1, 2, 5, 6, 7)$$

Simplify using **Karnaugh map** **AND** **Boolean Algebra**

000,001,010,101,110,111

Sum of Product Expression:

$$Y = A'B'C' + A'B'C + A'BC' + AB'C + ABC' + ABC$$

$$Y = A'B'(C+C') + A'BC' + AB'C + AB(C+C')$$

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$$Y = A'B' + AB + A'BC' + AB'C$$

$$Y = AB + A'(B' + BC') + AB'C$$

$$AB + A'(B' + C) + AB'C$$

$$A'(B + C) + A(B + B'C)$$

$$Y = A'(B + C) + A(B + C)$$

Hrm I don't think I did that algebra right.

		Σ	2
A	B		
0	0	1	0
0	1	1	0
1	0	0	1
1	1	1	1

		Σ	2
A	B		
0	0	1	0
0	1	1	0
1	0	0	1
1	1	1	1

		Σ	2
A	B		
0	0	1	0
0	1	1	0
1	0	0	1
1	1	1	1

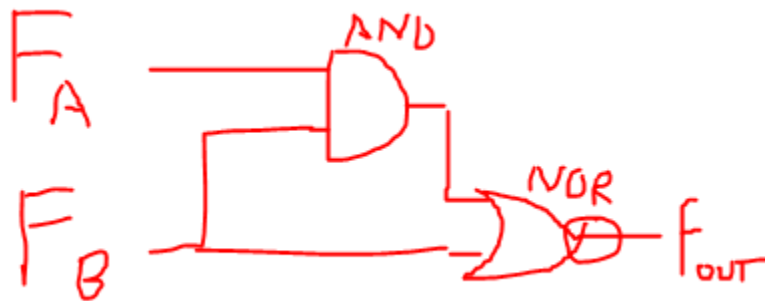
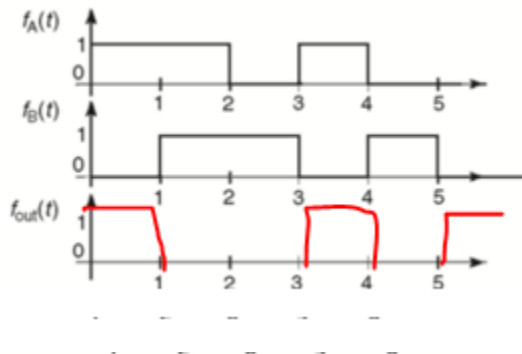
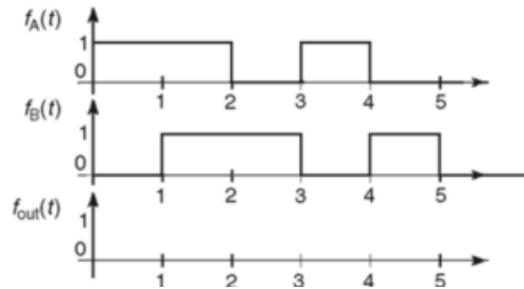
$$Y = (A \text{ XNOR } B) + A'BC' + AB'C$$

$$Y = (A \text{ XNOR } B) + (A \text{ XNOR } C)$$

Question_5

Two signals F_A and F_B are fed into an AND gate, the output of which is fed into a NOR gate, at the same time, the signal F_B is fed into the same NOR gate. Assuming the signals are positive high and neglect any delay time.

Construct the digital logic circuit diagram, truth table, and complete the following sequence diagram:



EQUATION IS TYPED AS: $(AB) \text{ NOR } (B)$

When B is zero, output is one. Effectively the gate is NOT B.

Truth Table:

FA	FB	AB	FOUT
0	0	0	1
0	1	0	0
1	0	0	1
1	1	1	0

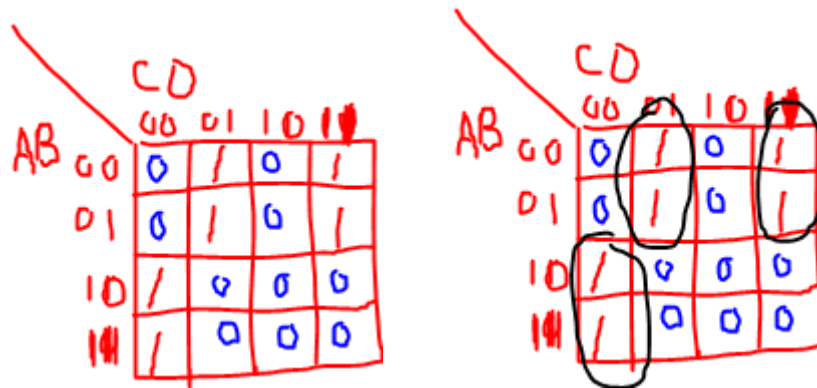
Question_6

Design a circuit that will tell whether a given month has 31 days in it. The month is specified by a 4-bit input A3:0. For example, if the inputs are 0001, the month is January, and if the inputs are 1100, the month is December.

The circuit output Y should be HIGH only when the month specified by the inputs has 31 days in it.

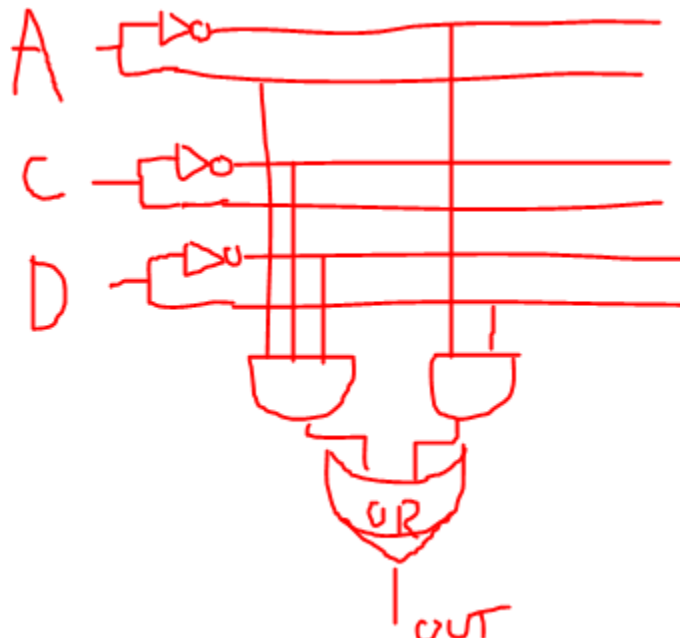
Write the simplified equation and draw the circuit diagram using a minimum number of gates.
 (Hint: Remember to take advantage of don't cares.)

There are 7 months having 31 days, January 1 0001, March 3 0011, May 5 0101, July 7 0111, August 8 1000, October 10 1010, December 12 1100,



Used a Karnaugh map to figure out how to actually write the equation

$$\text{Equation} = AC'D' + A'D$$



3 Gates is fairly few (well 4 if you break down the AND gate into the number of gates the transistor actually needs).

Question_7

Consider a three-input, one output system where A,B,C are inputs that represent the digits of binary number N and f is the output such that $f=1$ if $N \geq 011_2$ and $f=0$ if $N < 011_2$.

Construct the system Truth Table, and find the solution using 1) minterms, 2) simplification using Boolean Algebra, and 3) Karnaugh Map, construct the simplified digital circuit.

$$N \geq 3 \rightarrow 1, N < 3 \rightarrow 0$$

Truth Table:

A	B	C	F
0	0	0	0
0	0	1	0
0	1	0	0
0	1	1	1
1	0	0	1
1	0	1	1
1	1	0	1
1	1	1	1

Minterms:

$$F = A'BC + AB'C' + AB'C + ABC' + ABC$$

$$F = BC(A' + A) + AB'C + AB'C + ABC'$$

$$BC + AB'(C' + C) + ABC'$$

$$BC + AB' + ABC'$$

$$B(C + AC') + AB'$$

$$AB' + B(A + C)$$

$$AB' + AB + BC$$

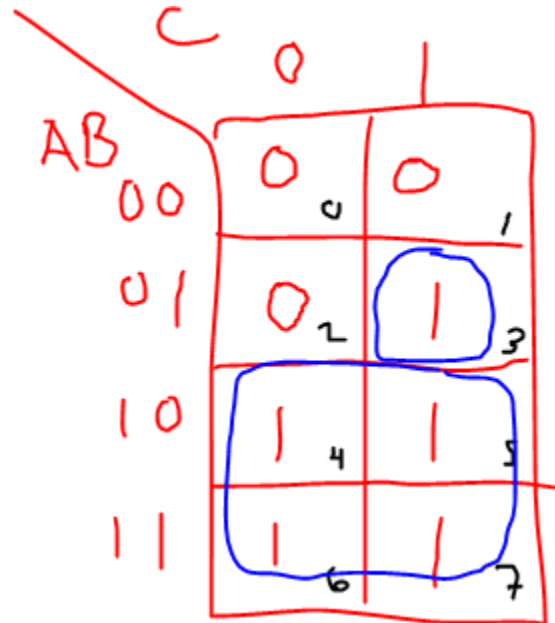
$$A(B + B') + BC$$

$$F = A + BC$$

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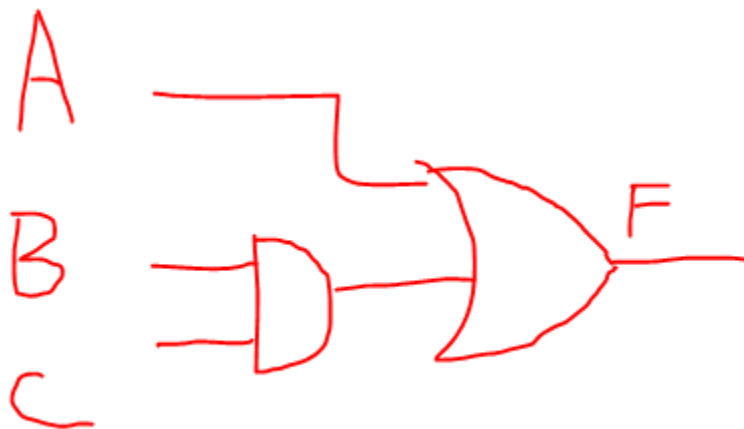
$$F = A + BC$$

Karnaugh Map:

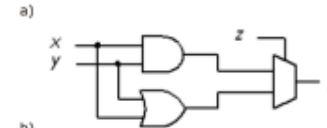
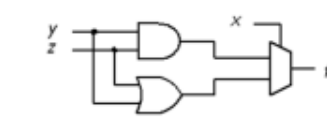
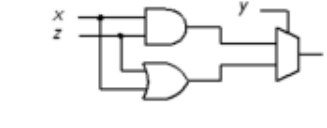


$$F = A + BC$$

Circuit Diagram:

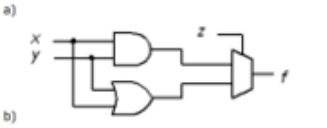
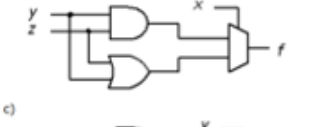
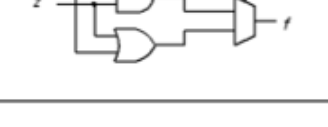


Question_8.1- Which circuit below implements the function $f(x,y,z)=xy+xz+yz$?

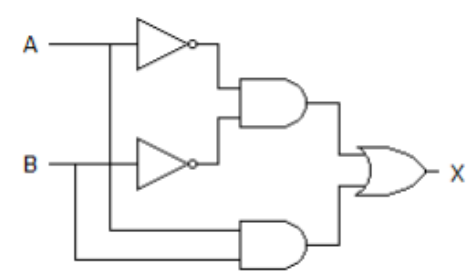
<p>a) Figure a b) Figure b c) Figure c d) All of the mentioned</p>	<p>a) </p> <p>b) </p> <p>c) </p>
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ZZZZZZZZ

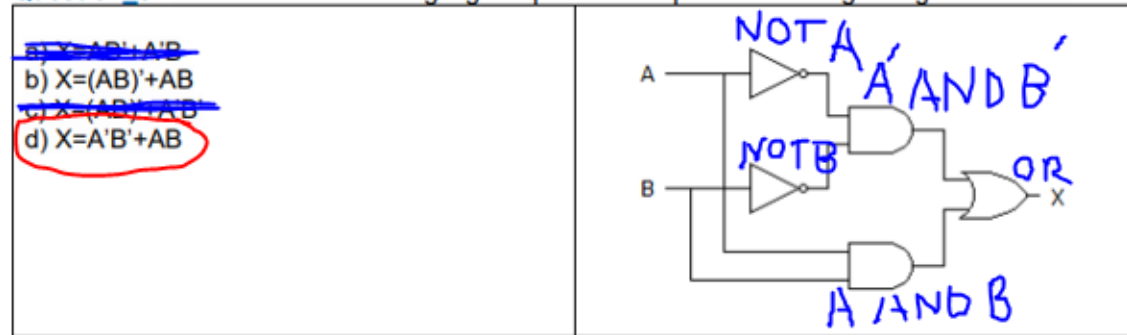
Question_8.1- Which circuit below implements the function $f(x,y,z)=xy+xz+yz$?

<p>a) Figure a b) Figure b c) Figure c d) All of the mentioned</p>	<p>a) </p> <p>b) </p> <p>c) </p>
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Question_8.2- Which of the following logic expressions represents the logic diagram shown?

<p>a) $X=AB'+A'B$ b) $X=(AB)'+AB$ c) $X=(AB)'+A'B'$ d) $X=A'B'+AB$</p>	
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Question 8.2- Which of the following logic expressions represents the logic diagram shown?



Question 8.3- Which of the following is the correct truth table for the circuit shown below:

x	y	z	f
0	0	0	0
0	0	1	0
0	1	0	1
0	1	1	1
1	0	0	1
1	0	1	0
1	1	0	0
1	1	1	1

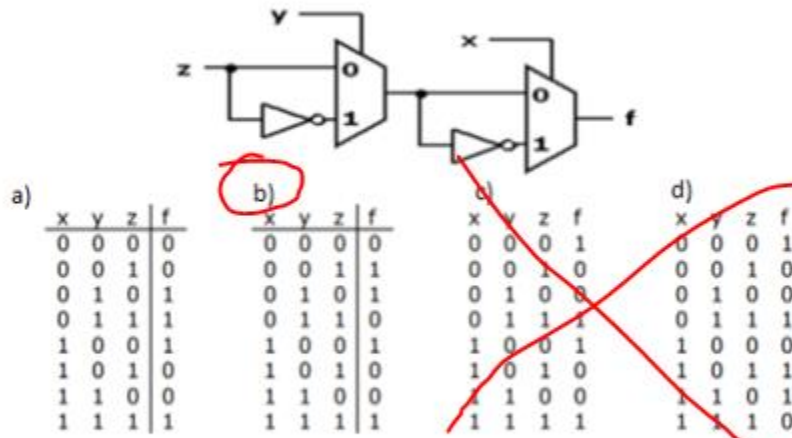
x	y	z	f
0	0	0	0
0	0	1	1
0	1	0	1
0	1	1	0
1	0	0	1
1	0	1	0
1	1	0	0
1	1	1	1

x	y	z	f
0	0	0	1
0	0	1	0
0	1	0	0
0	1	1	1
1	0	0	1
1	0	1	0
1	1	0	0
1	1	1	1

x	y	z	f
0	0	0	1
0	0	1	0
0	1	0	0
0	1	1	1
1	0	0	0
1	0	1	1
1	1	0	1
1	1	1	0

- a) Table a.
 b) Table b.
 c) Table c.
 d) Table d

Question_8.3- Which of the following is the correct truth table for the circuit shown below:



- a) Table a.
 b) Table b.
 c) Table c.
 d) Table d

Table B seems to match.

I'm confused, easier to make a truth table to check:

Z	Z'	Y	Multiplexer 1 output	NOT multiplexer one output	X	Multiplexer 2 output
0	1	0	0	1	0	0
0	1	0	0	1	1	1
0	1	1	1	0	0	1
0	1	1	1	0	1	0
1	0	0	1	0	0	1
1	0	0	1	0	1	0
1	0	1	0	1	0	0
1	0	1	0	1	1	1

Remember for multiplexers, if S is 0, then the upper output is selected, otherwise the lower one is.