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UNIVERSITÄT BERN

Statistical Inference for Data Science

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31. August 2021

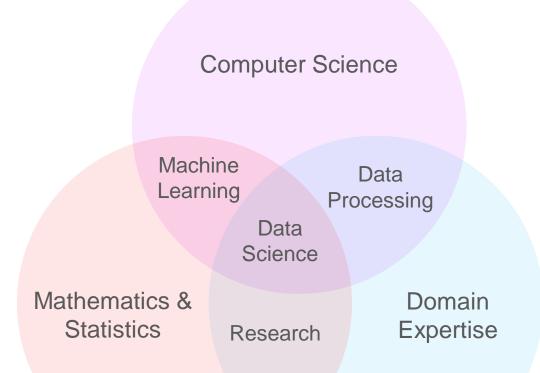


Welcome to Data Science!

Data Science uses

- Mathematics and Statistics
- Computer Science
- Domain expertise

on data to build information and extract knowledge.



Module 2

Day 1 Descriptive Statistics and Probability Parameter estimation

Day 2

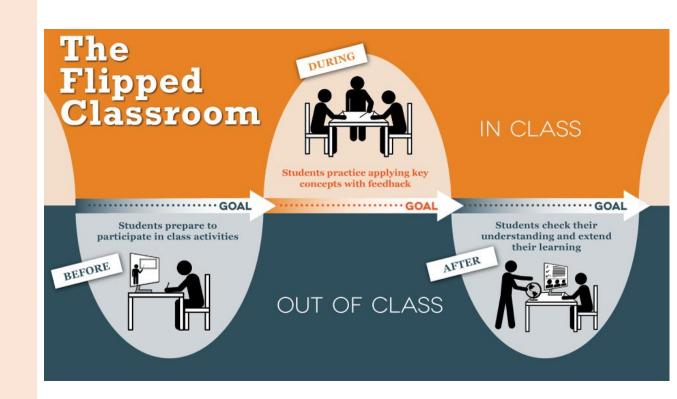
Hypothesis testing Day 3

Putting it all together Day 4

Project Presentation session (date to be fixed!)

Inverted classroom

- Introduction lectures
- In-depth study of the content with notebooks
- Discussion sessions based on your questions and comments
- Project: poster with poster presentation
- 1-2 questions per day



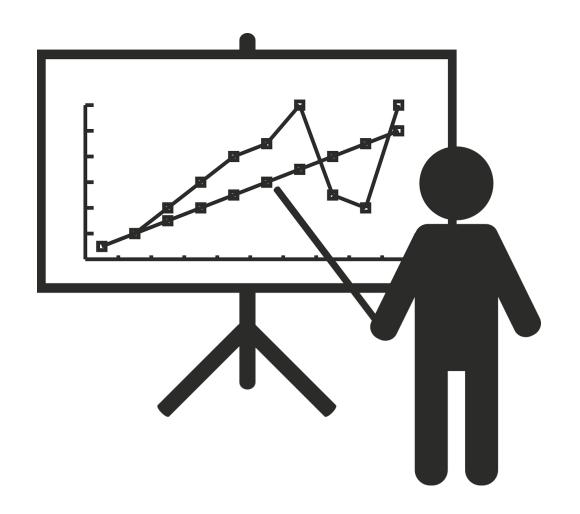
Project

Formal

- Group of 2 people
- 15min presentation, 15min discussion
- Half-day presence on two dates (to be fixed)

Content

- Choose your own data set
- answer research questions using statistics



Iris data set

3 classes: versicolor, setosa, virginica

4 characteristics

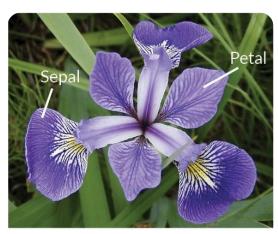
- petal: length, width
- sepal: length, width



Iris Setosa



Iris Virginica



Iris Versicolor

Foretaste (Project, 4th day)

Some new company recently sequenced the genes of the Iris species Setosa and patented it, apparently in order to preserve this species because it is so beautiful. Due this patent it is not allowed to change the plant.

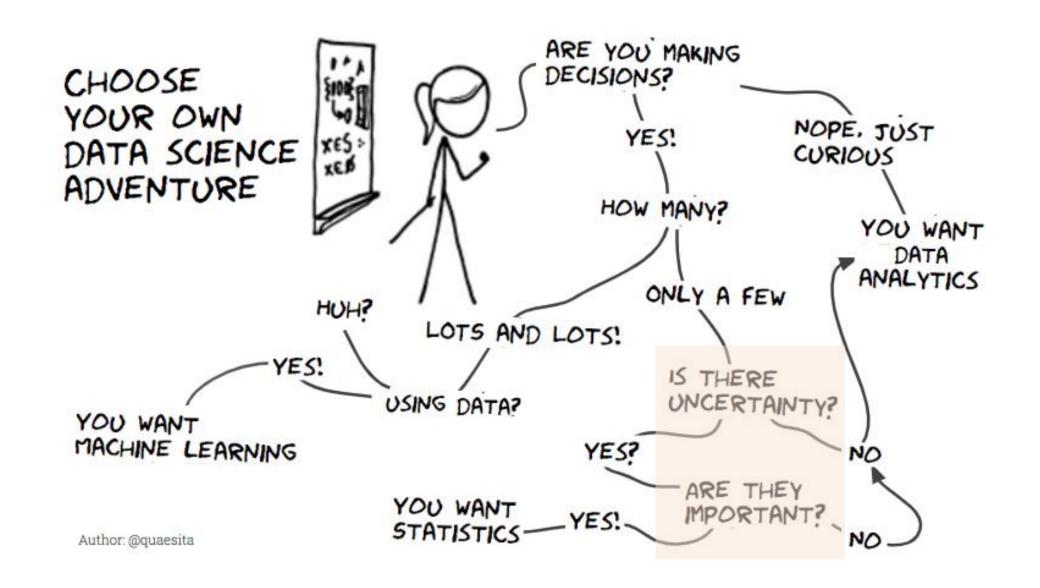
A big farmer and hater of Iris and with a field where Iris is a disturbing weed, has been using a new product from Sonte Manto for a couple of years. The product is supposed to effectively kill Iris plants.

A big Iris lover collected a sample of Iris plants from the farmer's field and thinks the Iris Setosa setal leaves are bigger than normal. She sent the sample to the company, which in turn came to the conclusion that Setosa must have mutated due to the product from Sonte Manto.

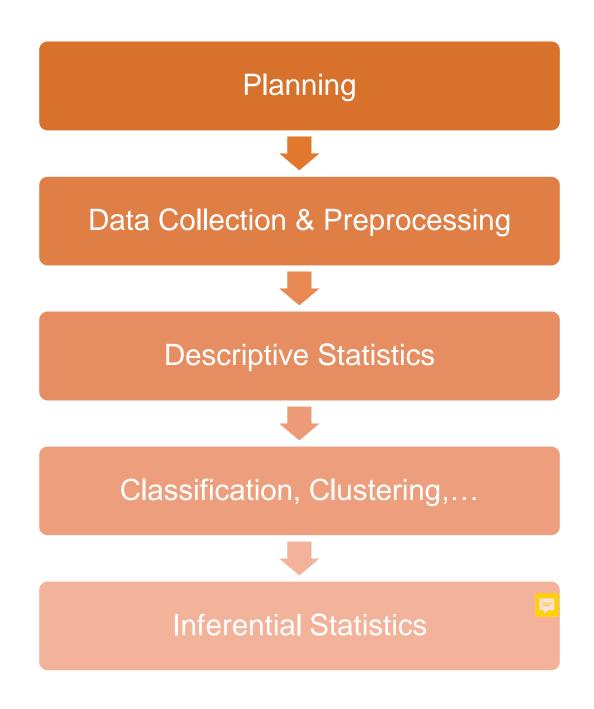
So the company sued Sonte Manto with the claim that they have changed the plant with their product. Sonte Manto may risk to pay a billion dollars.



The court is asking you to give a neutral and scientific advice.



General Procedure



Describing Data

Why?

- Get an overview
- Patterns
- Outliers
- Quality
- Learn about distibutions

How?

- Tables
- Plots
- Words
- Statistics



Good description is the basis for good inference

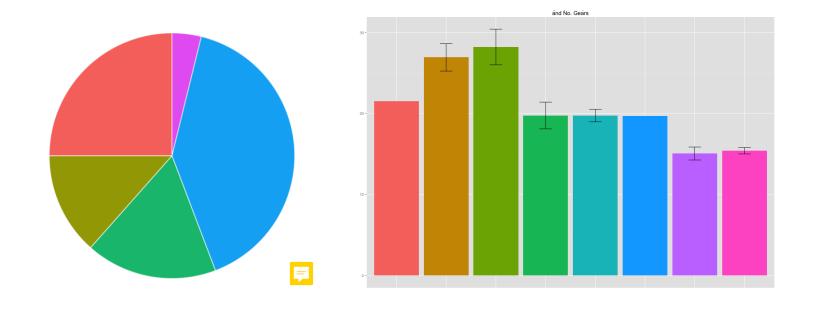
Descriptive Statistics

The two main tasks of descriptive statistics are

- the quantitative description and summary, and
- the graphical representation of data

What tools are suitable depends on the type of the variable we want to describe.

Categorical Variables



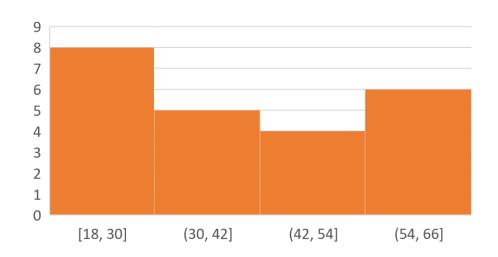
- Absolute frequency (eg. Number of female participants)
- Relative frequency (eq. Number of female participants divided by the sample size)

Numerical Variables

Summary Tables

Age	Nr. of People	
18-30	8	
30-42	5	
42-54	4	
54-66	6	

Histograms



What are typical values for the variable X?

Sample Mean:

$$\bar{x} = \frac{1}{n} \sum_{i=1}^{n} x_i = \frac{x_1 + x_2 + \dots + x_n}{n}$$

Sample Median: «center of the observations»

even $q_{0.5}$

median ist more robust than the mean

Location

(Numerical Variables)

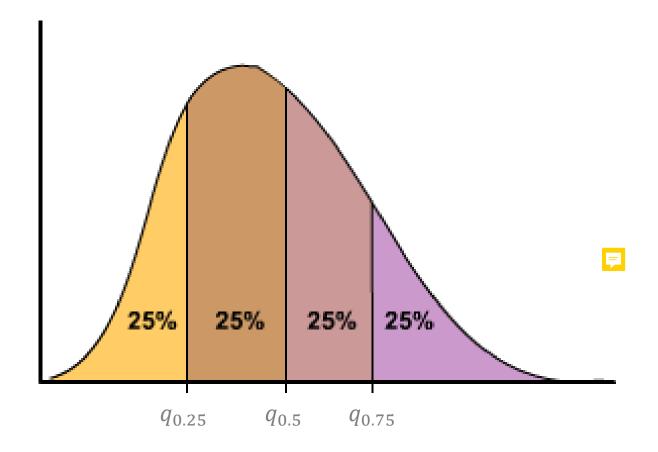
Generalizing the idea of the median to other fractions.

Typical for descripitve analyses: $q_{0.25}$, $q_{0.5}$, $q_{0.75}$

Typical for hypothesis testing: $q_{0.01}$, $q_{0.05}$, $q_{0.95}$, $q_{0.99}$



(Numerical Variables)



Spread

(Numerical Variables)

How strong is the deviation from the center?

Sample standard deviation:

$$s = \sqrt{\frac{1}{n-1} \sum_{i=1}^{n} (x_i - \bar{x})^2}$$

• IQR (inter quartile range):

$$IQR = q_{0.75} - q_{0.25}$$

$$S = 4.05, IQR = 5.93$$

$$S = 1.16, IQR = 1.34$$

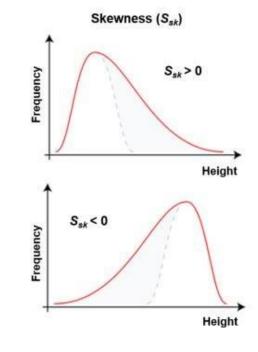
Shape

(Numerical Variables)

Is the distribution symmetric?

• Skewness:

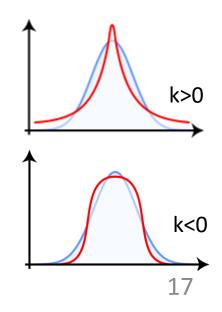
$$skewness = \frac{1}{n} \sum_{i=1}^{n} \frac{(x_i - \bar{x})^3}{s^3}$$



Does the distribution look like a bell curve?

Kurtosis:

$$kurtosis = \frac{1}{n} \sum_{i=1}^{n} \frac{(x_i - \bar{x})^4}{s^4} - 3$$



Simultaneous description I

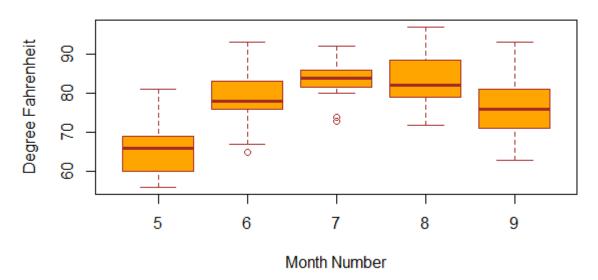
(of two features)

Contigency table (2 categorical features)

	Male	Female	Total
Blonde	4	8	12
Brunette	7	9	16
Total	11	17	28

Boxplots (1 categorical and 1 numerical feature)

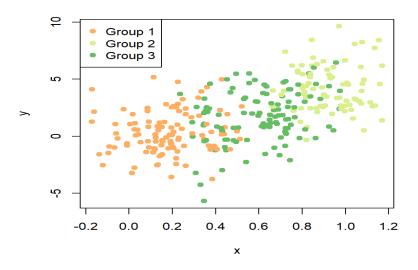
Different boxplots for each month



Simultaneous description II

(of two features)

Scatterplot (2 numerical features)



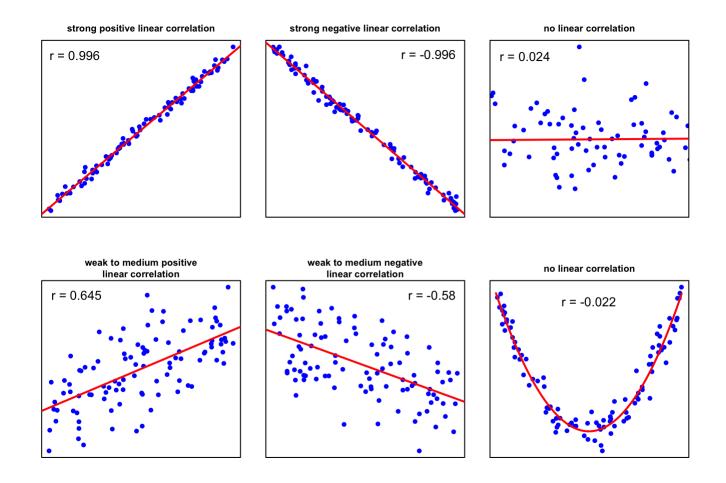
Pearson Correlation (2 numerical features)

$$r = rac{\sum_{i=1}^{n}(x_i - ar{x})(y_i - ar{y})}{\sqrt{\sum_{i=1}^{n}(x_i - ar{x})^2}\sqrt{\sum_{i=1}^{n}(y_i - ar{y})^2}}$$

Pearson Correlation (2 numerical features)

Simultaneous description III

(of two features)



Probability I

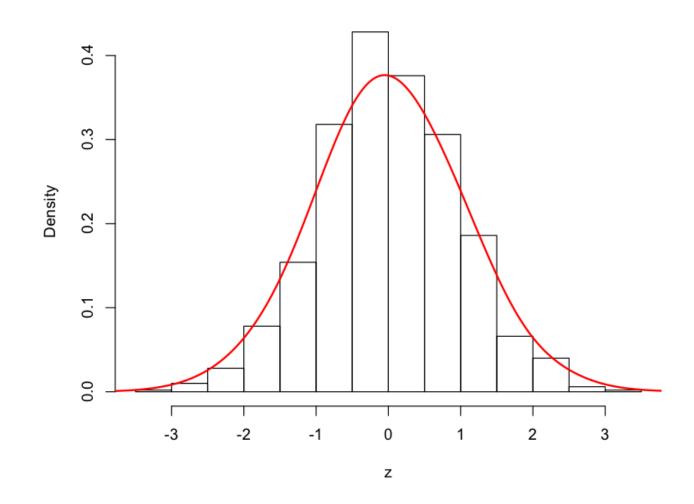
Empirical data is usually regarded as random. Why?

- 1. Objects under consideration (e.g. persons) as a random sample from a larger population
 - ---- conclusions about the population
- 2. physical or chemical measurements have random measurement errors
 - must be taken into account to evaluate data reliably
- view observations of features as random draw from population
- feature has a pdf
- use knowledge on this pdf to quantify the uncertainty of our conclusions

Probability density function (pdf)

Histogram With Fitted Density Curve, bw=.5

Probability II



Iris data set

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4 characteristics

- petal: *length, width*
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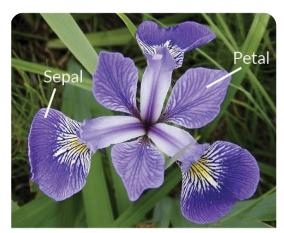
Let's analyse this data set descriptively



Iris Setosa



Iris Virginica



Iris Versicolor