

Case Study : Normality of data? No ! Normality of the residuals of ANOVA.

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CASE STUDY PRESENTATION

The objective of this script is to exemplify the requirement of normality of the residuals of the ANOVA model – NOT of the raw data

PREPARATION OF THE WORKING INTERFACE IN R

```
### I. Set working directory
# On RStudio: tab 'Session' -> Set Working Directory -> Choose Directory.
# Choose the directory containing the datafile and the associated R script.

### II. Possibly, installation of new R packages needed for the analysis on RStudio:
# Click on the 'Packages' tab in the bottom-right window of R Studio interface -> 'Install Packages'
# Comment #1: R package installation requires a connection to internet
# Comment #2: Once packages have been installed, no need to re-install them
# again when you close-open again RStudio.

### III. Initialisation of the working space
# To erase all graphs
graphics.off()
# To erase objects from the working space - Clean up of the memory
rm(list = ls())
```

LOADING REQUIRED METHODS FOR ANALYSIS

```
library(ggplot2)    # a new graphic library - Will be presented in details in 'Regular' course
library(car)        # Levene's test for homogeneity of variances
library(agricolae)  # the Newman-Keuls test for multiple mean comparisons
```

LOADING/CREATING THE DATA and STARTING ANALYSIS

```
set.seed(145) # set random seed generator of computer.
              # All participants will get the 'same' random data set
```

we generate yield data for 100 plants of three hybrid maize varieties (G1, G2 and G3). The environmental variance σ_E^2 equals to 1.5. The phenotypic means of G1 equals 120kg/ha, of G2 equals 115kg/ha and of G3 equals 113kg/ha.

```
## generate data :
Yield <- data.frame( yield = c(rnorm(100, 120, 1.5),
                              rnorm(100, 115, 1.5),
```

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```

        rnorm(100, 113, 1.5)),
        genotype = rep(c("G1", "G2", "G3"), each = 100)
    )
( head(Yield, 12) ) ## print 12 first lines of Yield on screen

```

```

##      yield genotype
## 1  121.0304      G1
## 2  121.5995      G1
## 3  120.8051      G1
## 4  122.8590      G1
## 5  121.5947      G1
## 6  122.0555      G1
## 7  120.7917      G1
## 8  120.6046      G1
## 9  121.7516      G1
## 10 121.1890      G1
## 11 118.1797      G1
## 12 118.4916      G1

```

```

( tail(Yield, 12) ) ## print 12 last lines of Yield on screen

```

```

##      yield genotype
## 289 113.3233      G3
## 290 114.1899      G3
## 291 113.1149      G3
## 292 112.3984      G3
## 293 112.9925      G3
## 294 111.0509      G3
## 295 112.1010      G3
## 296 115.4383      G3
## 297 113.5930      G3
## 298 110.4583      G3
## 299 116.0888      G3
## 300 112.9643      G3

```

```

## histograms of yield

```

```

x11() ## open a graphic window

```

```

## syntax for ggplot will be explained later - do not spend time to understand/recall for now

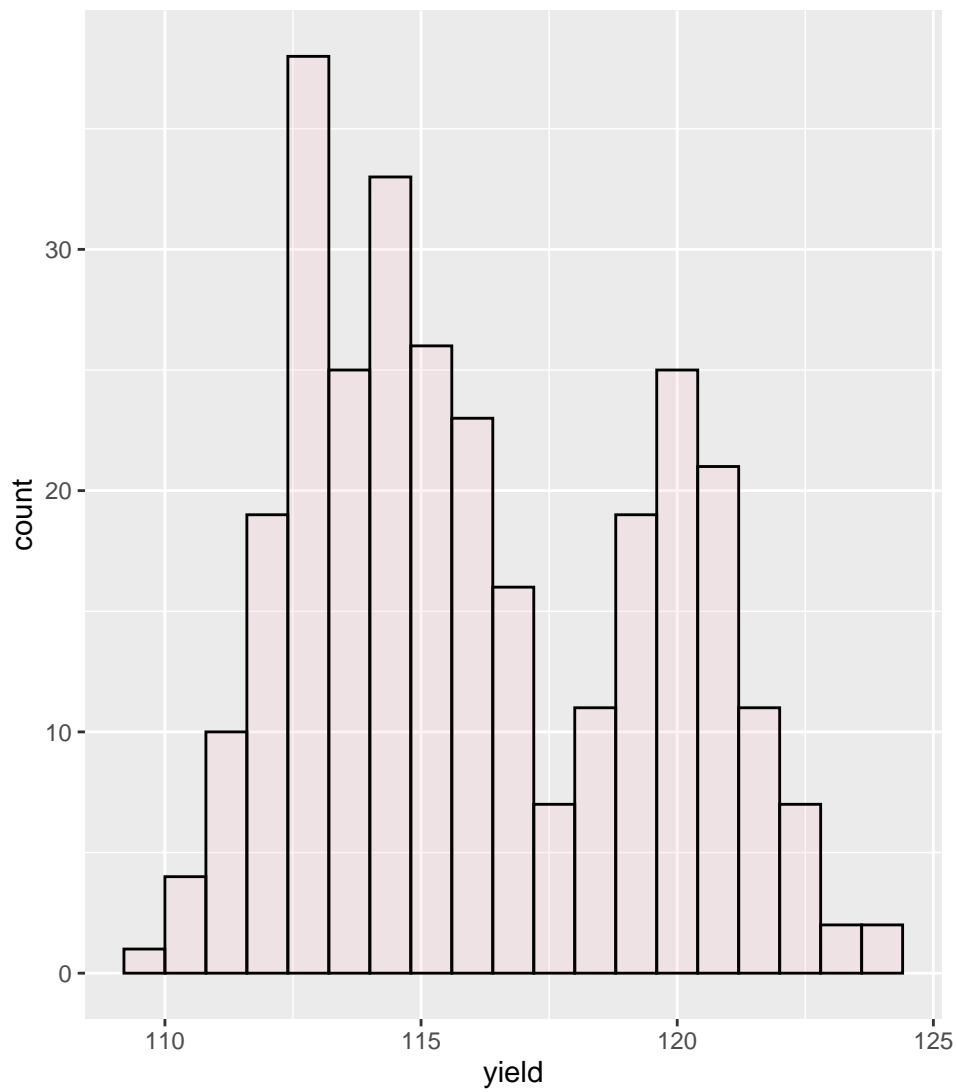
```

```

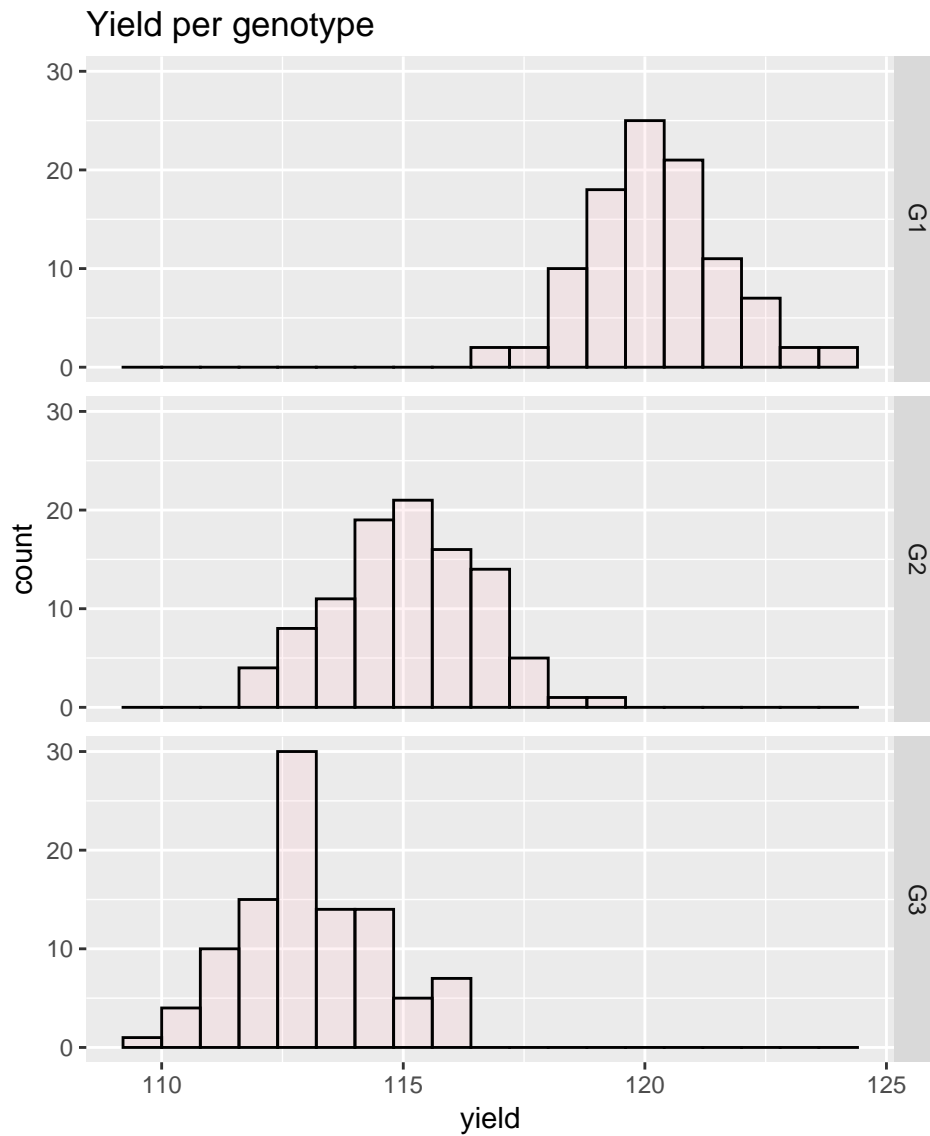
ggplot(Yield) + aes( yield) +
  geom_histogram(binwidth = 0.8, col = "black", fill = "pink", alpha = 0.2) +
  ggtitle("All yield data")

```

All yield data



```
## histograms per variety
x11()
ggplot( Yield) + aes( yield) +
  geom_histogram(binwidth = 0.8, col = "black", fill = "pink", alpha = 0.2) +
  facet_grid( genotype ~ .) +
  ggtitle("Yield per genotype")
```



Anova of yield data

```
model1 <- aov( yield ~ genotype, data = Yield)
```

```
summary(model1) ## your conclusions ?
```

```
##           Df Sum Sq Mean Sq F value Pr(>F)
## genotype    2 2735.8   1367.9    666.5 <2e-16 ***
## Residuals  297   609.6     2.1
```

```
## ---
```

```
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
x11()
```

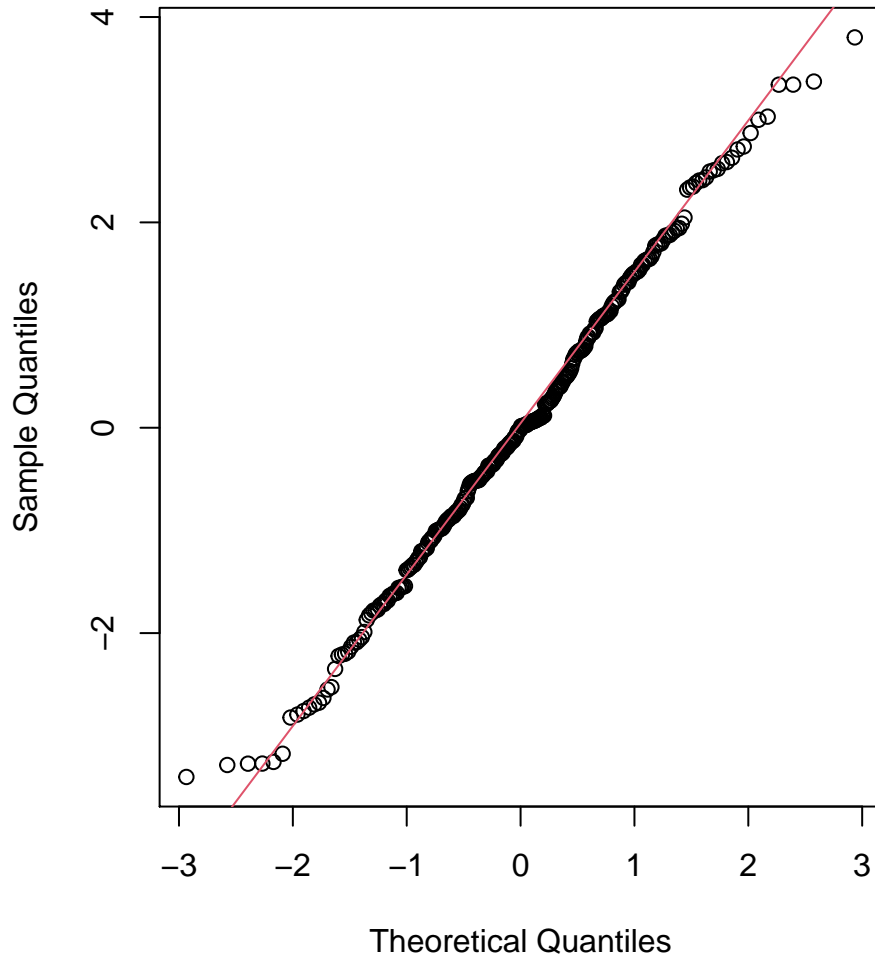
quantile - quantile plot are the standard tool to visualise

observed distribution vs expected distribution

*qqnorm(residuals(model1)) *## qqnorm() draws a quantile-quantile plot for normal (gaussian) distribution**

```
qqline(residuals(model1), col = 2)
```

Normal Q-Q Plot



```
# normality test for yield variable of the Yield dataframe  
shapiro.test(Yield$yield)
```

```
##  
## Shapiro-Wilk normality test  
##  
## data: Yield$yield  
## W = 0.94824, p-value = 8.772e-09
```

```
# normality test for the residuals of the model  
shapiro.test(residuals(model1))
```

```
##  
## Shapiro-Wilk normality test  
##  
## data: residuals(model1)  
## W = 0.99519, p-value = 0.477
```

```
# homogeneity of the variances of residuals in the different varieties  
## Q: is Sigma2E the same for all varieties ?
```

```
leveneTest( aov( yield ~ genotype, data = Yield) ) ## leveneTest automagically test the residuals
```

```
## Levene's Test for Homogeneity of Variance (center = median)  
##      Df F value Pr(>F)
```

```
## group    2  0.8289 0.4375
##          297
## your conclusions ?

## comparing the varieties using the Neuman-Keuls post-hoc test.
SNK.test(model1, "genotype", group = TRUE, console = TRUE)

##
## Study: model1 ~ "genotype"
##
## Student Newman Keuls Test
## for yield
##
## Mean Square Error:  2.052467
##
## genotype, means
##
##      yield      std   r      Min      Max
## G1 120.2716 1.379876 100 116.8708 123.6431
## G2 115.1472 1.520238 100 111.8629 118.9486
## G3 113.0897 1.393636 100 109.9146 116.1193
##
## Alpha: 0.05 ; DF Error: 297
##
## Critical Range
##           2           3
## 0.3987260 0.4772444
##
## Means with the same letter are not significantly different.
##
##      yield groups
## G1 120.2716      a
## G2 115.1472      b
## G3 113.0897      c
```