## Calculus III Honors Spring 2012 Exam 1 - Practice Problems, Set 1

- 1. Write down 2 different parametric equations that both describe a circle of radius 1 centered at (0,1). Also write down a polar equation for the same circle.
- 2. Write down a polar equation for the line y = 1.
- 3. Graph the curve given by  $x(t) = t^3$ ,  $y(t) = \sin(t)$ . Find the tangent line at  $t = \frac{\pi}{4}$ . Find the vertical and horizontal tangents.
- 4. Using a parametric equation, find the arc length of an arc of angle  $\alpha$  on a circle of radius r. Do the same using polar coordinates.
- 5. Graph the polar curve  $r = 1 + \cos(\theta)$ . Find the enclosed area.
- 6. Graph the curve given by  $x = t + t^2$  and  $y = 1 t^2$  for  $t \ge 0$ . Find the area between this curve and the x- and y- axes.