

Closest Pair (2D)

pts = $[(1,2), (2,5), (4,3), (7,3)]$

function Closest_pair (pts) .

if len(pts) <= 3:

return smallest dis

else:

left = pts [:len(pts)]

right = pts [len(pts):]

// recursive

disleft = Closestpair (left)

disright = Closestpair (right)

d = min (disleft, disright)

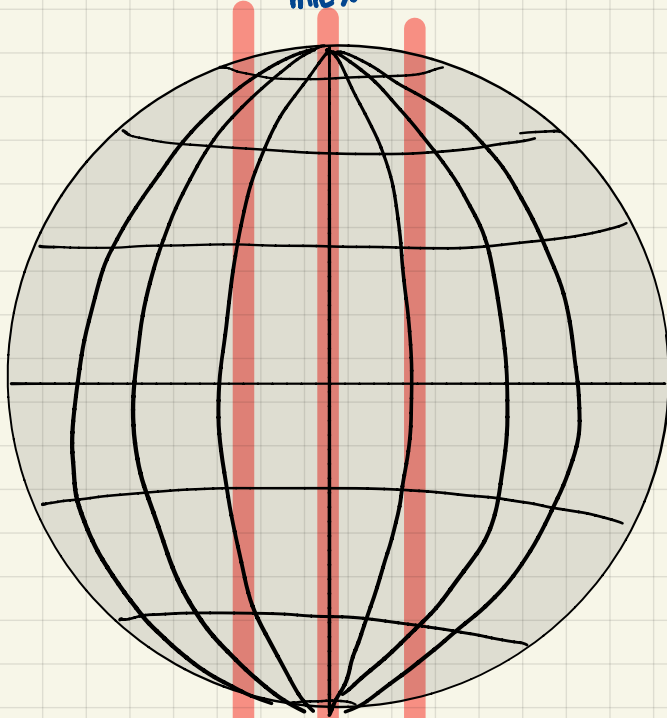
// handle mid area.

construct area of $+d$ & $-d$ base on mid x

compute their distance

⋮

(long=0)
mid x

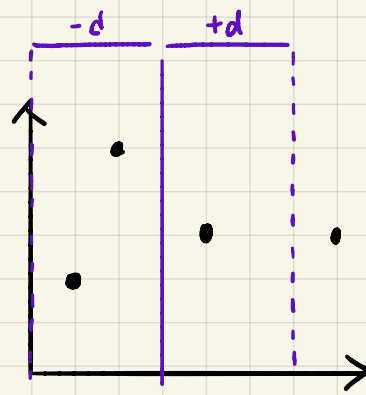


$-d$ $+d$ how to calculate the long lat on the line?



Ex: At \otimes , $d = 6000$ km

how to construct the mid area $(+d, -d)$ to compare?



(divide)

// cut input in half and handle seperately.

$(-90 \sim 90)$
y-axis
 $(-180 \sim 180)$
x-axis

For (lat, long)

we get distance using

Haversine $a = \sin^2(\Delta\phi/2) + \cos \phi_1 \cdot \cos \phi_2 \cdot \sin^2(\Delta\lambda/2)$

formula: $c = 2 \cdot \text{atan2}(\sqrt{a}, \sqrt{1-a})$

$d = R \cdot c$

where ϕ is latitude, λ is longitude, R is earth's radius (mean radius = 6,371km); note that angles need to be in radians to pass to trig functions!

```
JavaScript: const R = 6371e3; // metres
const  $\phi_1$  = lat1 * Math.PI/180; //  $\phi$ ,  $\lambda$  in radians
const  $\phi_2$  = lat2 * Math.PI/180;
const  $\Delta\phi$  = (lat2-lat1) * Math.PI/180;
const  $\Delta\lambda$  = (lon2-lon1) * Math.PI/180;

const a = Math.sin( $\Delta\phi/2$ ) * Math.sin( $\Delta\phi/2$ ) +
  Math.cos( $\phi_1$ ) * Math.cos( $\phi_2$ ) *
  Math.sin( $\Delta\lambda/2$ ) * Math.sin( $\Delta\lambda/2$ );
const c = 2 * Math.atan2(Math.sqrt(a), Math.sqrt(1-a));
const d = R * c; // in metres
```