664project3

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Data Cleaning

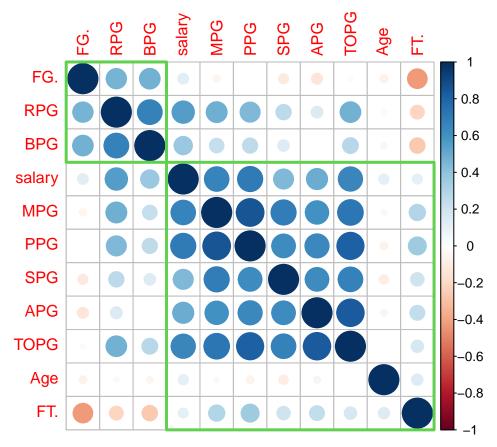
```
data <- read.csv(file = 'final_dataset2.csv')
data = data[data[,"G"] >= 40,]  #screen out less statistically significant data points
data = data[data[,"Age"] >= 24,]  #salary cap
data_reduced = data[,c('Player', 'Pos', 'salary','Age','FG.','FT.','MPG','PPG','APG','RPG','TOPG','BPG'
```

Correlation

```
library(corrplot)
```

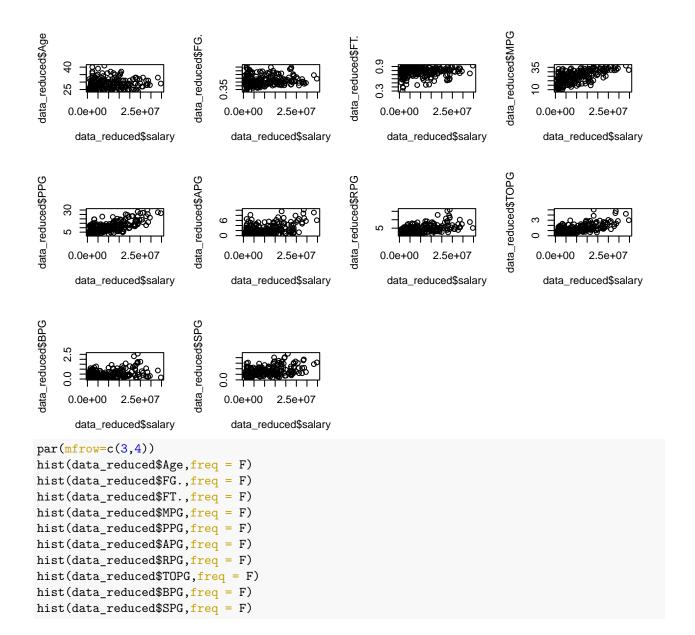
corrplot 0.92 loaded

```
corrplot(cor(data_reduced[,c(3:13)]),
    method = "circle",
    order = "hclust",  # Ordering method of the matrix
    hclust.method = "ward.D", # If order = "hclust", is the cluster method to be used
    addrect = 2,  # If order = "hclust", number of cluster rectangles
    rect.col = 3,  # Color of the rectangles
    rect.lwd = 3)
```

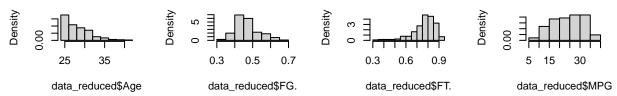


EDA

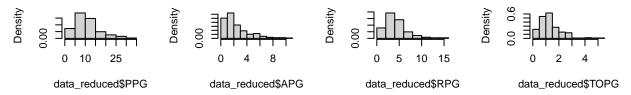
```
par(mfrow=c(3,4))
plot(data_reduced$salary, data_reduced$Age)
plot(data_reduced$salary, data_reduced$FG.)
plot(data_reduced$salary, data_reduced$FT.)
plot(data_reduced$salary, data_reduced$MPG)
plot(data_reduced$salary, data_reduced$PPG)
plot(data_reduced$salary, data_reduced$APG)
plot(data_reduced$salary, data_reduced$RPG)
plot(data_reduced$salary, data_reduced$TOPG)
plot(data_reduced$salary, data_reduced$PPG)
plot(data_reduced$salary, data_reduced$PPG)
plot(data_reduced$salary, data_reduced$PPG)
plot(data_reduced$salary, data_reduced$PPG)
```



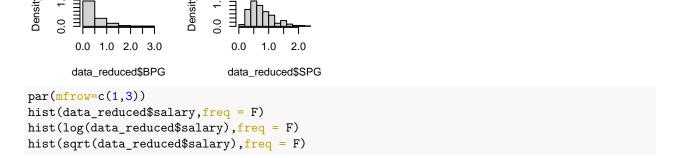
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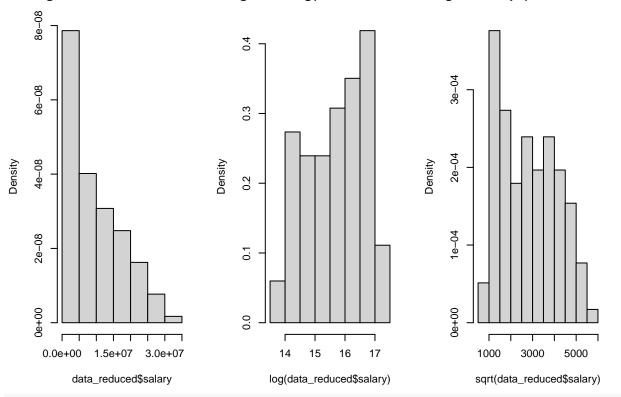
stogram of data_reducecstogram of data_reducecstogram of data_reducectogram of data_reduced



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Histogram of data_reduced\$sallistogram of log(data_reduced\$saistogram of sqrt(data_reduced\$s



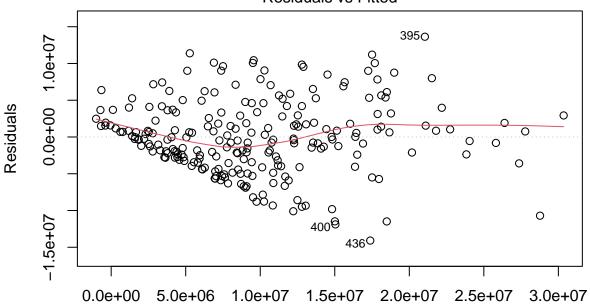
model1 = lm(salary~Age+FG.+FT.+MPG+PPG+APG+RPG+TOPG+BPG+SPG, data = data_reduced)
summary(model1)

```
##
## Call:
  lm(formula = salary ~ Age + FG. + FT. + MPG + PPG + APG + RPG +
       TOPG + BPG + SPG, data = data_reduced)
##
##
## Residuals:
##
         Min
                    1Q
                           Median
                                         3Q
                                                   Max
  -14089723 -2994727
                          -253863
                                    3077857
                                             13638501
##
##
##
  Coefficients:
##
                Estimate Std. Error t value Pr(>|t|)
##
  (Intercept) -10742788
                             5588191
                                     -1.922 0.055828 .
## Age
                  374641
                                       3.703 0.000268 ***
                              101166
## FG.
                                      -0.205 0.837583
                -1376158
                             6705565
## FT.
                -5556879
                             4163071
                                      -1.335 0.183302
## MPG
                  178543
                              104891
                                       1.702 0.090117 .
## PPG
                  595949
                                       4.072 6.48e-05 ***
                              146358
## APG
                  464214
                              380792
                                       1.219 0.224103
                                       2.831 0.005059 **
## RPG
                  688235
                              243074
## TOPG
                  180454
                             1206349
                                       0.150 0.881226
## BPG
                 1512513
                             1184947
                                       1.276 0.203128
## SPG
                -1172602
                             1282839
                                     -0.914 0.361669
## ---
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
##
```

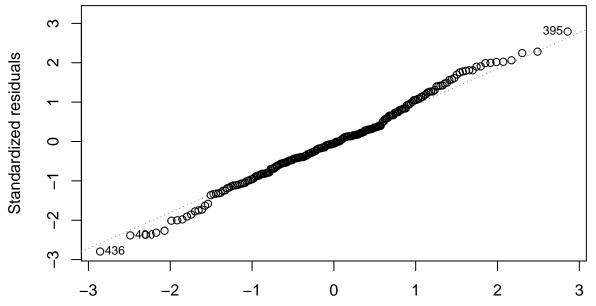
Residual standard error: 5106000 on 223 degrees of freedom ## Multiple R-squared: 0.6099, Adjusted R-squared: 0.5924 ## F-statistic: 34.87 on 10 and 223 DF, p-value: < 2.2e-16

plot(model1)

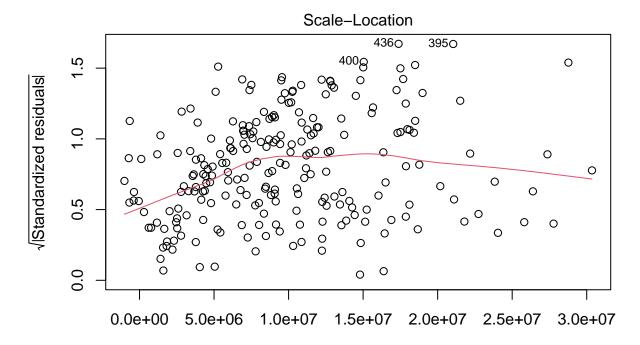
Residuals vs Fitted



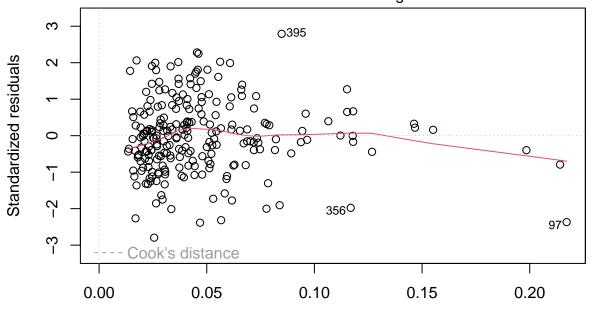
Fitted values Im(salary ~ Age + FG. + FT. + MPG + PPG + APG + RPG + TOPG + BPG + SPG) Normal Q-Q



Theoretical Quantiles Im(salary ~ Age + FG. + FT. + MPG + PPG + APG + RPG + TOPG + BPG + SPG)



Fitted values
Im(salary ~ Age + FG. + FT. + MPG + PPG + APG + RPG + TOPG + BPG + SPG)
Residuals vs Leverage



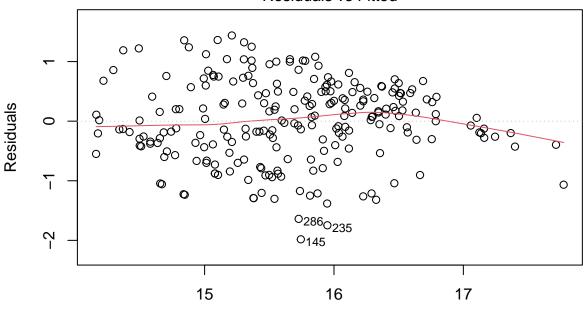
Leverage Im(salary ~ Age + FG. + FT. + MPG + PPG + APG + RPG + TOPG + BPG + SPG)

 $\label{eq:model2} model2 = lm(log(salary) \sim Age+FG.+FT.+MPG+PPG+APG+RPG+TOPG+BPG+SPG, \ \, \mbox{data} = data_reduced) \\ summary(model2)$

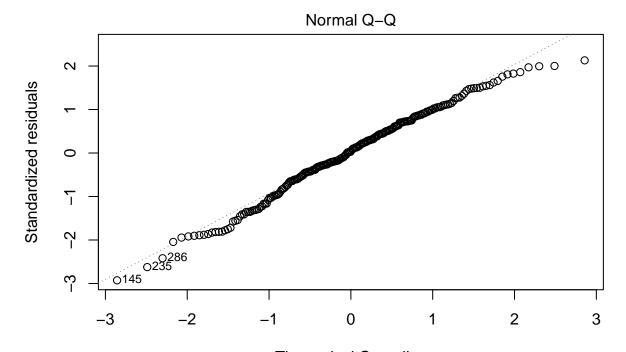
```
##
## Call:
## lm(formula = log(salary) ~ Age + FG. + FT. + MPG + PPG + APG +
## RPG + TOPG + BPG + SPG, data = data_reduced)
```

```
##
## Residuals:
##
                  1Q
                       Median
                      0.02802 0.49012
  -1.98249 -0.40067
                                         1.43804
##
##
  Coefficients:
               Estimate Std. Error t value Pr(>|t|)
##
                                     15.331 < 2e-16 ***
## (Intercept) 11.53557
                            0.75246
## Age
                0.06899
                            0.01362
                                      5.065 8.57e-07 ***
## FG.
                            0.90291
                0.52017
                                      0.576
                                              0.5651
## FT.
               -0.17224
                            0.56056
                                     -0.307
                                              0.7589
## MPG
                0.05889
                            0.01412
                                      4.170 4.36e-05 ***
                            0.01971
## PPG
                0.02460
                                      1.248
                                              0.2132
                                     -0.845
                                              0.3990
## APG
               -0.04333
                            0.05127
## RPG
                0.05911
                            0.03273
                                      1.806
                                              0.0723 .
## TOPG
                0.18835
                            0.16244
                                      1.160
                                              0.2475
## BPG
                0.08460
                            0.15955
                                      0.530
                                              0.5965
## SPG
               -0.06184
                            0.17274
                                     -0.358
                                              0.7207
##
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
##
## Residual standard error: 0.6876 on 223 degrees of freedom
## Multiple R-squared: 0.5475, Adjusted R-squared: 0.5272
## F-statistic: 26.98 on 10 and 223 DF, p-value: < 2.2e-16
plot(model2)
```

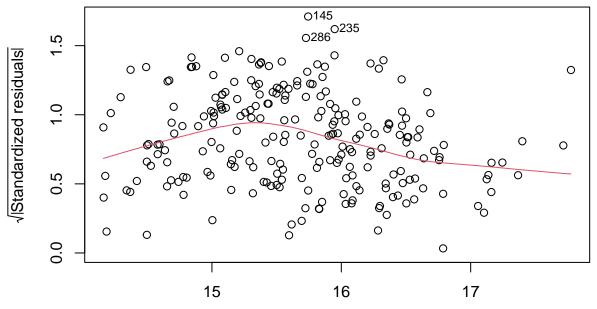
Residuals vs Fitted



Fitted values Im(log(salary) ~ Age + FG. + FT. + MPG + PPG + APG + RPG + TOPG + BPG + SPG

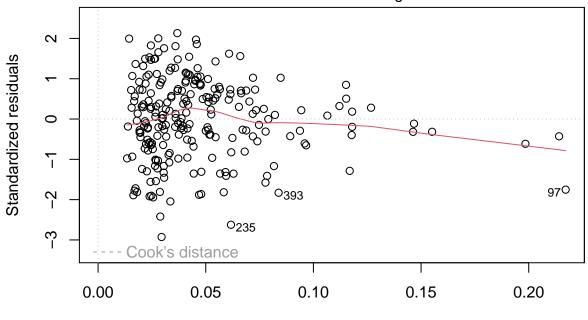


Theoretical Quantiles
Im(log(salary) ~ Age + FG. + FT. + MPG + PPG + APG + RPG + TOPG + BPG + SPG
Scale-Location



Fitted values Im(log(salary) ~ Age + FG. + FT. + MPG + PPG + APG + RPG + TOPG + BPG + SPG

Residuals vs Leverage

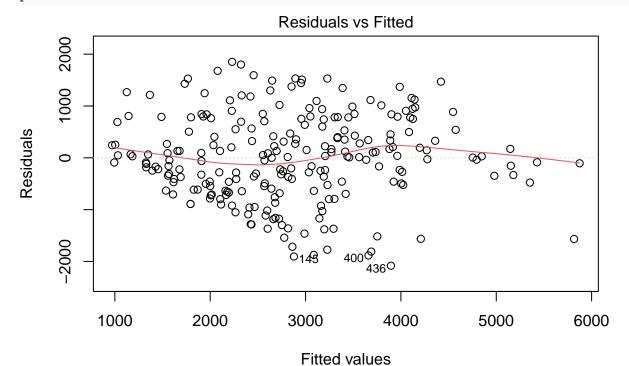


Im(log(salary) ~ Age + FG. + FT. + MPG + PPG + APG + RPG + TOPG + BPG + SPG

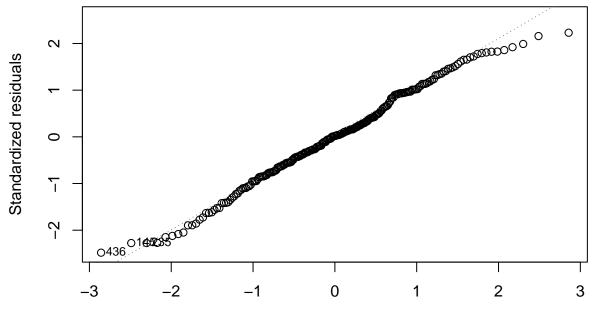
Leverage

model3 = lm(sqrt(salary)~Age+FG.+FT.+MPG+PPG+APG+RPG+TOPG+BPG+SPG, data = data_reduced)
summary(model3)

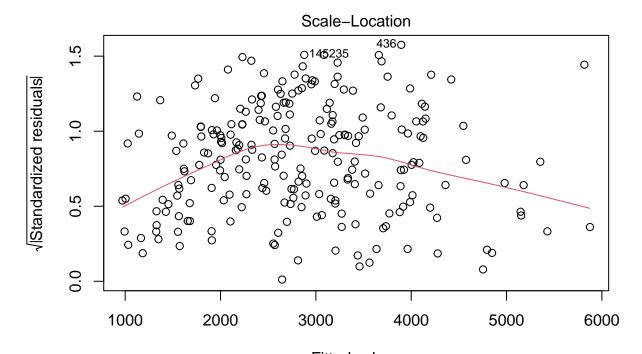
```
##
## Call:
## lm(formula = sqrt(salary) ~ Age + FG. + FT. + MPG + PPG + APG +
       RPG + TOPG + BPG + SPG, data = data reduced)
##
##
## Residuals:
##
        Min
                   1Q
                        Median
                                     3Q
                                              Max
##
   -2081.39
            -524.60
                         14.38
                                 628.16
                                         1851.96
##
## Coefficients:
                Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) -1495.535
                             929.840
                                      -1.608 0.10917
## Age
                  74.377
                              16.833
                                       4.418 1.55e-05 ***
## FG.
                 224.765
                            1115.764
                                       0.201
                                              0.84053
## FT.
                -624.707
                             692.709
                                      -0.902
                                              0.36812
                  55.008
## MPG
                              17.453
                                       3.152
                                              0.00185
## PPG
                  64.437
                              24.353
                                       2.646
                                              0.00873
##
  APG
                   5.909
                              63.361
                                       0.093
                                              0.92578
## RPG
                  93.739
                              40.446
                                       2.318
                                              0.02138 *
## TOPG
                 147.406
                             200.729
                                       0.734
                                              0.46351
## BPG
                 193.064
                             197.168
                                       0.979
                                              0.32855
## SPG
                -143.745
                             213.456
                                      -0.673 0.50138
                     '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
## Residual standard error: 849.7 on 223 degrees of freedom
## Multiple R-squared: 0.5892, Adjusted R-squared: 0.5708
```



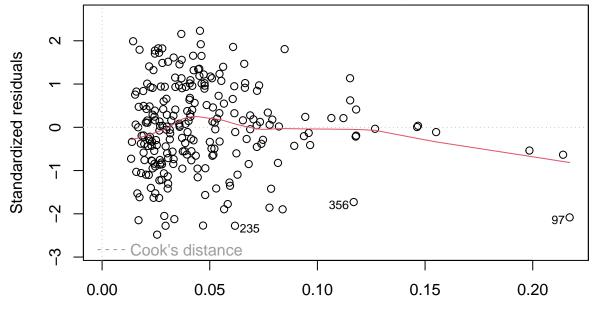
Im(sqrt(salary) ~ Age + FG. + FT. + MPG + PPG + APG + RPG + TOPG + BPG + SP Normal Q-Q



Theoretical Quantiles Im(sqrt(salary) ~ Age + FG. + FT. + MPG + PPG + APG + RPG + TOPG + BPG + SP



Fitted values
Im(sqrt(salary) ~ Age + FG. + FT. + MPG + PPG + APG + RPG + TOPG + BPG + SP
Residuals vs Leverage

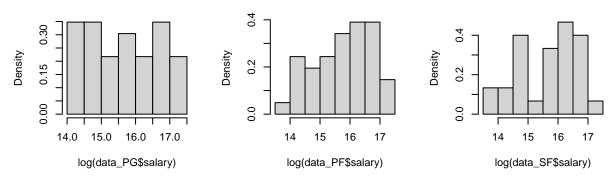


Leverage Im(sqrt(salary) ~ Age + FG. + FT. + MPG + PPG + APG + RPG + TOPG + BPG + SP

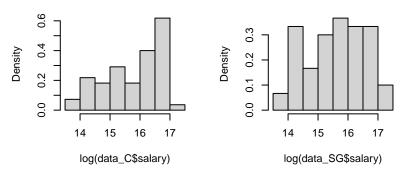
```
data_PG = data_reduced[data_reduced[,2] == "PG", ]
data_PF = data_reduced[data_reduced[,2] == "PF", ]
data_SF = data_reduced[data_reduced[,2] == "SF", ]
data_C = data_reduced[data_reduced[,2] == "C", ]
data_SG = data_reduced[data_reduced[,2] == "SG", ]
```

```
par(mfrow=c(2,3))
hist(log(data_PG$salary),freq = F)
hist(log(data_PF$salary),freq = F)
hist(log(data_SF$salary),freq = F)
hist(log(data_C$salary),freq = F)
hist(log(data_SG$salary),freq = F)
```

Histogram of log(data_PG\$sala | Histogram of log(data_PF\$sala | Histogram of log(data_SF\$sala |

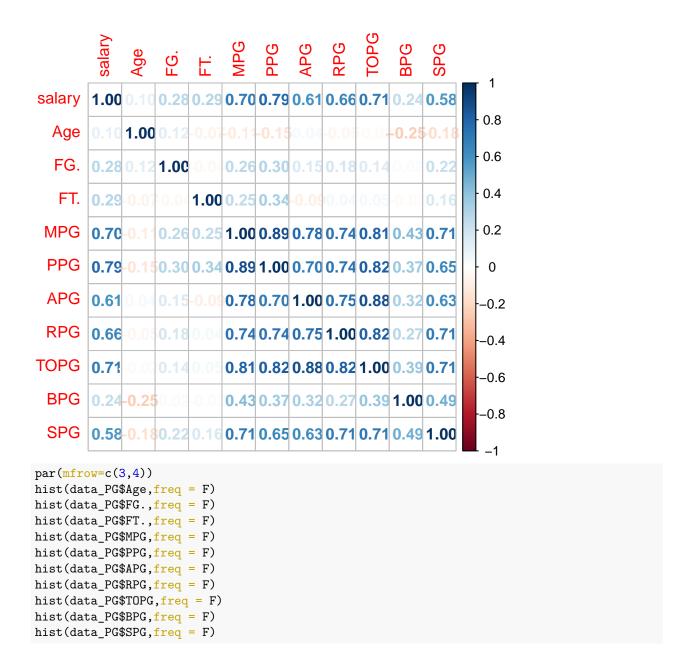


Histogram of log(data_C\$salar Histogram of log(data_SG\$salar

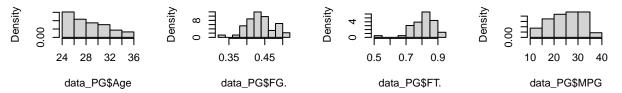


For the PG players,

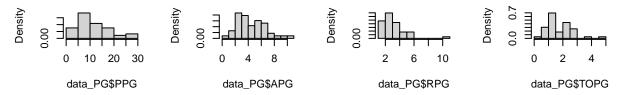
corrplot(cor(data_PG[,-c(1,2)]), method = 'number')



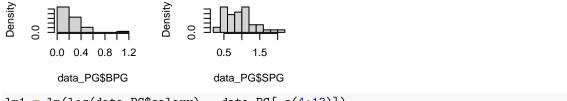
Histogram of data_PG\$/ Histogram of data_PG\$I Histogram of data_PG\$IHistogram of data_PG\$N



Histogram of data_PG\$FHistogram of data_PG\$AHistogram of data_PG\$TI



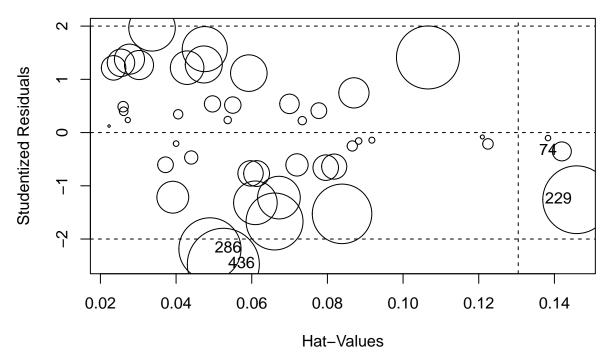
Histogram of data_PG\$E Histogram of data_PG\$S



lm1 = lm(log(data_PG\$salary)~.,data_PG[,c(4:13)])
summary(lm1)

```
##
## Call:
  lm(formula = log(data_PG$salary) ~ ., data = data_PG[, c(4:13)])
##
## Residuals:
##
        Min
                  1Q
                        Median
                                     3Q
                                              Max
   -1.39808 -0.44226 0.09293 0.43362
                                         0.96283
##
##
   Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
   (Intercept) 11.37528
                            2.35990
                                      4.820 2.76e-05 ***
##
                                             0.00673 **
## Age
                0.10002
                            0.03472
                                      2.881
## FG.
               -0.41153
                            3.22023
                                     -0.128
                                             0.89904
                                     -0.347
## FT.
               -0.69889
                            2.01503
                                             0.73079
                            0.03971
## MPG
                0.04783
                                      1.205
                                             0.23647
                0.08335
                            0.04592
                                      1.815
                                             0.07806 .
## PPG
                                     -0.917
## APG
               -0.10740
                            0.11712
                                             0.36538
## RPG
               -0.10879
                            0.13097
                                     -0.831
                                             0.41179
##
  TOPG
                0.29198
                            0.34866
                                      0.837
                                             0.40803
                            0.68483
                                             0.81175
## BPG
               -0.16434
                                     -0.240
## SPG
                0.28831
                            0.45191
                                      0.638
                                             0.52764
##
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.6838 on 35 degrees of freedom
```

```
## Multiple R-squared: 0.6561, Adjusted R-squared: 0.5578
## F-statistic: 6.677 on 10 and 35 DF, p-value: 1.065e-05
#step(lm1)
lm2 = lm(log(data_PG$salary)~Age + PPG,data_PG)
summary(lm2)
##
## Call:
## lm(formula = log(data_PG$salary) ~ Age + PPG, data = data_PG)
## Residuals:
               1Q Median
                               3Q
                                      Max
## -1.4695 -0.3951 -0.0248 0.3409 1.2085
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 11.42999
                          0.89312 12.798 2.93e-16 ***
               0.09529
                          0.02948
                                   3.233 0.00236 **
## Age
## PPG
               0.12242
                          0.01494
                                   8.192 2.54e-10 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.6454 on 43 degrees of freedom
## Multiple R-squared: 0.6236, Adjusted R-squared: 0.6061
## F-statistic: 35.62 on 2 and 43 DF, p-value: 7.537e-10
library(car)
## Loading required package: carData
which(dffits(lm2)>2*sqrt(2/46))
## 417
## 44
which (abs(covratio(lm2)-1)>(3*2/46))
## 61 74 107 142 179 212 250 270 286 359 376 386 395 410 436
            8 10 14 18 21 23 24 31 35 37 41 43 46
which(dfbetas(lm2)>(2/sqrt(46)))
## [1] 15 20 70 86 90
outlierTest(lm2)
## No Studentized residuals with Bonferroni p < 0.05
## Largest |rstudent|:
       rstudent unadjusted p-value Bonferroni p
                          0.017463
## 436 -2.474546
                                        0.80328
influencePlot(lm2)
```



```
## StudRes Hat CookD

## 74 -0.3536104 0.14195908 0.007039019

## 229 -1.2615690 0.14587631 0.089378045

## 286 -2.1852867 0.04895314 0.075322445

## 436 -2.4745462 0.05249088 0.101037513

#Same varaibles in the model as before

data_PG2 = data_PG[-c(74,229,286,436),]

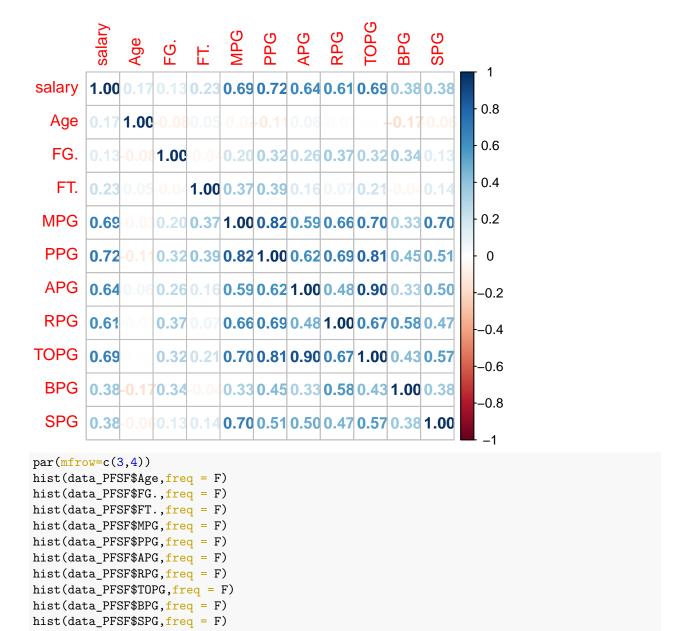
lm3 = lm(log(data_PG2$salary)~.,data_PG2[,c(4:13)])

#step(lm3)
```

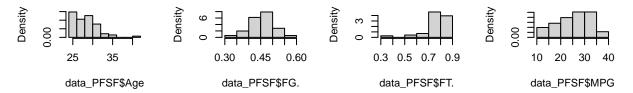
For the PF and SF players

```
data_PFSF = rbind(data_PF,data_SF)

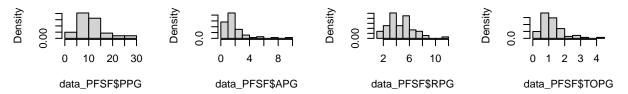
#corrplot(cor(data_PF[,-c(1,2)]), method = 'number')
#corrplot(cor(data_SF[,-c(1,2)]), method = 'number')
corrplot(cor(data_PFSF[,-c(1,2)]), method = 'number')
```



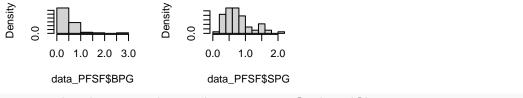
Histogram of data_PFSF\Histogram of data_PFSF\Histogram of data_PFSF\stagram of data_PFSF\



listogram of data_PFSF\$listogram of data_PFSF\$listogram of data_PFSF\$-



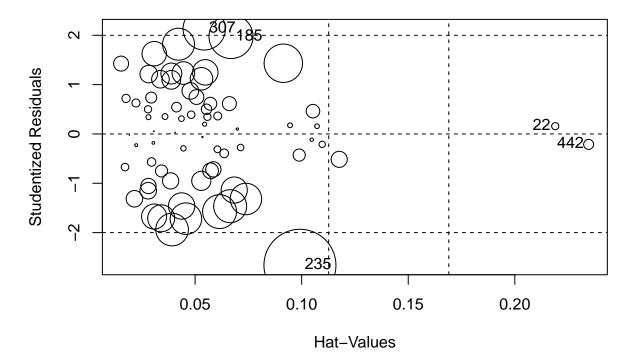
listogram of data_PFSF\$listogram of data_PFSF\$



```
lm5 = lm(log(data_PFSF$salary)~.,data_PFSF[,c(4:13)])
summary(lm5)
```

```
##
## Call:
   lm(formula = log(data_PFSF$salary) ~ ., data = data_PFSF[, c(4:13)])
##
##
## Residuals:
##
        Min
                   1Q
                        Median
                                     3Q
                                              Max
   -1.44059 -0.42070 -0.02365 0.40681
                                         1.52853
##
##
   Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
   (Intercept) 11.71233
                            1.27303
                                      9.200 4.55e-13 ***
##
##
  Age
                0.08528
                            0.02521
                                      3.383
                                             0.00127 **
## FG.
               -2.47504
                                     -1.428
                            1.73359
                                             0.15856
## FT.
                0.52665
                            0.94119
                                      0.560
                                             0.57787
                            0.02746
                                             0.02816 *
## MPG
                0.06178
                                      2.250
## PPG
                0.02888
                            0.03634
                                      0.795
                                             0.42993
                                      1.399
                                             0.16690
  APG
                0.18765
                            0.13411
  RPG
                0.14029
                            0.07419
                                      1.891
                                              0.06347
##
##
  TOPG
               -0.36571
                            0.39781
                                     -0.919
                                             0.36162
                            0.27159
                                             0.69825
## BPG
                0.10580
                                      0.390
## SPG
               -0.24347
                            0.30280
                                     -0.804
                                             0.42453
##
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.6604 on 60 degrees of freedom
```

```
## Multiple R-squared: 0.6077, Adjusted R-squared: 0.5423
## F-statistic: 9.293 on 10 and 60 DF, p-value: 4.441e-09
#step(lm5)
lm6 = lm(log(data_PFSF$salary)~Age + MPG + RPG,data_PFSF)
summary(lm6)
##
## Call:
## lm(formula = log(data_PFSF$salary) ~ Age + MPG + RPG, data = data_PFSF)
## Residuals:
                 1Q
                     Median
                                   3Q
## -1.58465 -0.44792 0.03487 0.39978 1.32275
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 10.75400
                          0.74875 14.363 < 2e-16 ***
               0.08876
                          0.02375
                                   3.737 0.000387 ***
## Age
## MPG
               0.07528
                          0.01501
                                   5.016 4.12e-06 ***
## RPG
                          0.05433
                                   2.109 0.038713 *
               0.11457
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.6549 on 67 degrees of freedom
## Multiple R-squared: 0.5691, Adjusted R-squared: 0.5498
## F-statistic: 29.5 on 3 and 67 DF, p-value: 2.838e-12
library(car)
which(dffits(lm6)>2*sqrt(3/46))
## 185
## 15
which (abs (covratio (lm6)-1)>(3*3/46))
## 22 235 442
##
   2 54 68
which(dfbetas(lm6)>(2/sqrt(46)))
## [1] 59 60 125 191 267
outlierTest(lm6)
## No Studentized residuals with Bonferroni p < 0.05
## Largest |rstudent|:
       rstudent unadjusted p-value Bonferroni p
## 235 -2.662551
                          0.009732
                                        0.69097
influencePlot(lm6)
```

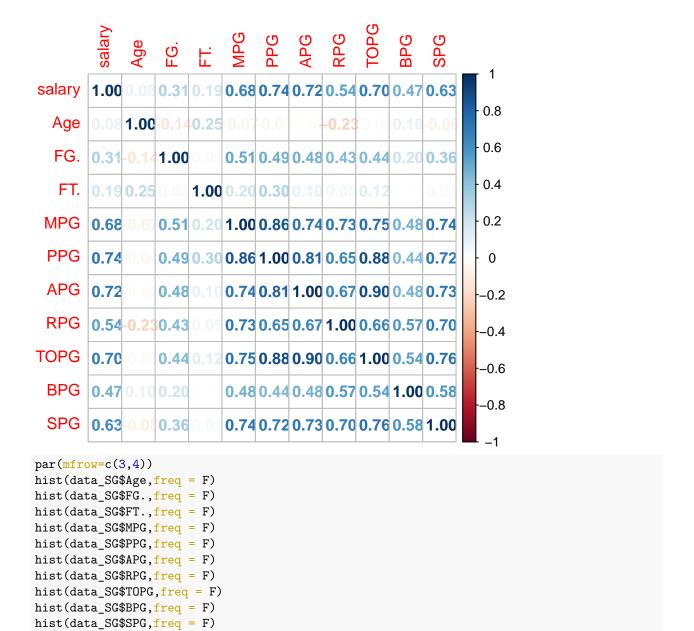


```
## StudRes Hat CookD
## 22  0.1575431  0.21896403  0.001765258
## 185  1.9755474  0.06685735  0.067003324
## 235 -2.6625512  0.09918723  0.178887044
## 307  2.1309564  0.05428110  0.061888371
## 442 -0.2115417  0.23462983  0.003479205

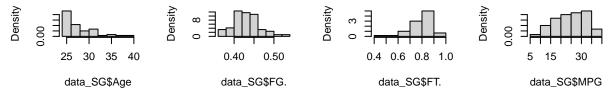
#Same varaibles in the model as before
data_PFSF2 = data_PFSF[-c(22,185,235,307,442),]
lm7 = lm(log(data_PFSF2$salary)~.,data_PFSF2[,c(4:13)])
#step(lm7)
```

For the SG players,

```
corrplot(cor(data_SG[,-c(1,2)]), method = 'number')
```



Histogram of data_SG\$/ Histogram of data_SG\$I Histogram of data_SG\$|Histogram of data_SG\$N

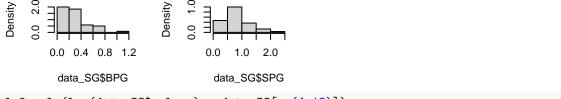


Histogram of data_SG\$FHistogram of data_SG\$AHistogram of data_SG\$RHistogram of data_SG\$T(



Histogram of data SG\$EHistogram of data SG\$S

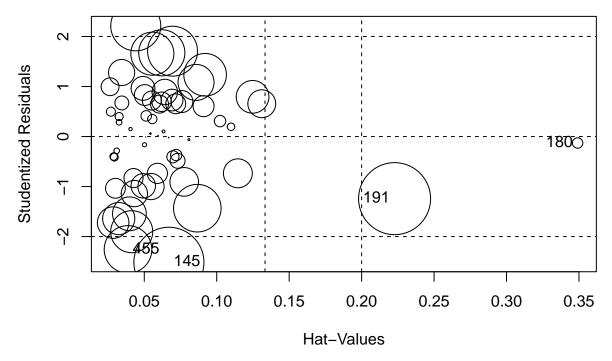
2.0



lm9 = lm(log(data_SG\$salary)~.,data_SG[,c(4:13)]) summary(lm9)

```
##
## Call:
  lm(formula = log(data_SG$salary) ~ ., data = data_SG[, c(4:13)])
##
## Residuals:
##
        Min
                  1Q
                       Median
                                     3Q
                                             Max
  -1.71901 -0.48090 0.07355 0.44723
                                         1.35337
##
##
  Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) 13.02057
                            1.82435
                                      7.137 4.07e-09 ***
## Age
                0.03361
                            0.02964
                                      1.134
                                              0.2623
## FG.
               -3.37909
                            3.37402
                                     -1.002
                                              0.3215
## FT.
                1.28263
                            1.19683
                                      1.072
                                              0.2891
                            0.03004
                                      2.006
## MPG
                0.06025
                                              0.0504 .
                0.01440
                            0.04865
                                      0.296
                                              0.7685
## PPG
                                      0.606
## APG
                0.08445
                            0.13942
                                              0.5475
## RPG
               -0.09169
                            0.12972
                                     -0.707
                                              0.4830
##
  TOPG
                0.09819
                            0.36982
                                      0.266
                                              0.7917
                0.32850
                            0.59001
                                      0.557
                                              0.5802
## BPG
## SPG
                0.30905
                            0.40284
                                      0.767
                                              0.4467
##
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.7243 on 49 degrees of freedom
```

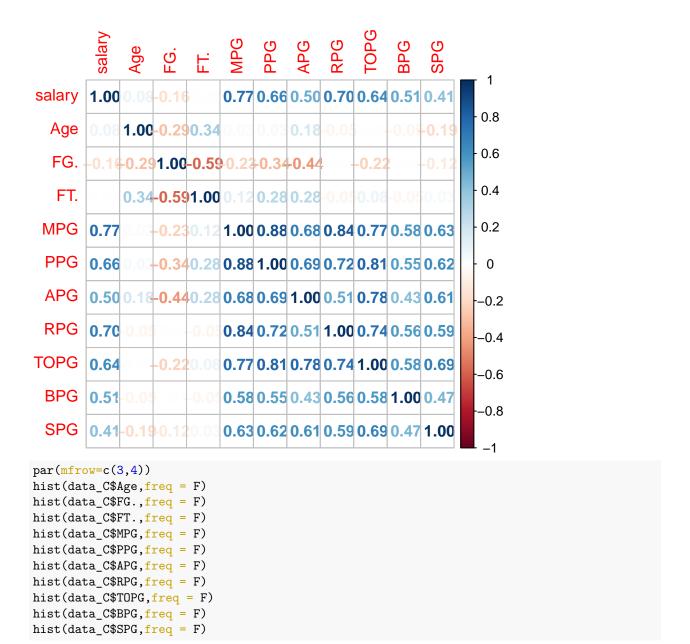
```
## Multiple R-squared: 0.5648, Adjusted R-squared: 0.4759
## F-statistic: 6.358 on 10 and 49 DF, p-value: 3.582e-06
#step(lm9)
lm10 = lm(log(data_SG$salary)~ Age + MPG + APG,data_SG)
summary(lm10)
##
## Call:
## lm(formula = log(data_SG$salary) ~ Age + MPG + APG, data = data_SG)
## Residuals:
                 1Q
                     Median
                                   3Q
                                           Max
## -1.65029 -0.49816 0.05603 0.48046 1.48764
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
                          0.81902 14.635 < 2e-16 ***
## (Intercept) 11.98625
               0.05364
                          0.02546
                                   2.107 0.039631 *
## Age
## MPG
               0.07172
                          0.01883
                                    3.810 0.000348 ***
## APG
               0.13763
                          0.08315
                                   1.655 0.103463
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.7111 on 56 degrees of freedom
## Multiple R-squared: 0.5206, Adjusted R-squared: 0.4949
## F-statistic: 20.27 on 3 and 56 DF, p-value: 5.089e-09
library(car)
which(dffits(lm10)>2*sqrt(3/60))
## 8 9
## 1 2
which (abs (covratio (lm10)-1)>(3*4/60))
##
    8 145 180 191 265 455
##
    1 23 28 29 41 60
which(dfbetas(lm10)>(2/sqrt(60)))
## [1]
            2 23 29 43 48 120 123 203
outlierTest(lm10)
## No Studentized residuals with Bonferroni p < 0.05
## Largest |rstudent|:
       rstudent unadjusted p-value Bonferroni p
## 145 -2.514169
                          0.014887
                                        0.89322
influencePlot(lm10)
```



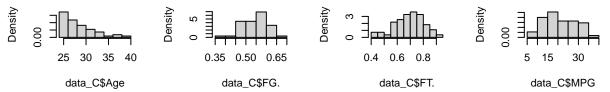
```
## StudRes Hat CookD
## 145 -2.5141691 0.06699268 0.103621478
## 180 -0.1296745 0.34909042 0.002294875
## 191 -1.2418908 0.22274911 0.109440020
## 455 -2.2574579 0.03877990 0.047896606
#Same varaibles in the model as before
data_SG2 = data_SG[-c(145,180,191,455),]
lm11 = lm(log(data_SG2$salary)~.,data_SG2[,c(4:13)])
#step(lm11)
```

```
For the C players
```

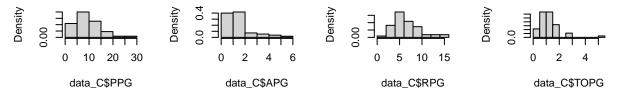
```
corrplot(cor(data_C[,-c(1,2)]), method = 'number')
```



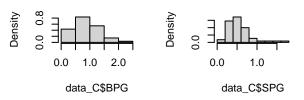
Histogram of data_C\$A Histogram of data_C\$F Histogram of data_C\$F Histogram of data_C\$M



Histogram of data_C\$P| Histogram of data_C\$A| Histogram of data_C\$R| Histogram of data_C\$TC



Histogram of data_C\$B| Histogram of data_C\$S|



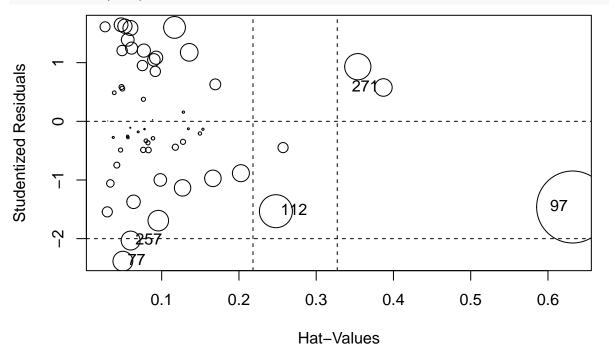
##

```
lm13 = lm(log(data_C$salary)~.,data_C[,c(4:13)])
summary(lm13)
```

```
## Call:
  lm(formula = log(data_C$salary) ~ ., data = data_C[, c(4:13)])
##
## Residuals:
##
        Min
                  1Q
                       Median
                                     3Q
                                             Max
  -1.45883 -0.41456 -0.06907 0.51299
                                         1.12229
##
##
  Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) 14.00575
                            1.90661
                                      7.346 3.57e-09 ***
## Age
                0.04307
                            0.03055
                                      1.410 0.165622
## FG.
               -1.90580
                                     -0.888 0.379155
                            2.14520
                                     -0.776 0.441821
## FT.
               -0.89904
                            1.15835
                                      3.612 0.000774 ***
## MPG
                0.13786
                            0.03816
               -0.07064
                            0.05031
                                     -1.404 0.167337
## PPG
               -0.23969
## APG
                            0.18699
                                     -1.282 0.206615
## RPG
               -0.01264
                            0.06734
                                     -0.188 0.851973
## TOPG
                0.45401
                            0.31038
                                      1.463 0.150643
               -0.06569
                            0.28204
                                     -0.233 0.816910
## BPG
## SPG
               -0.13963
                            0.49185
                                     -0.284 0.777827
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.7032 on 44 degrees of freedom
```

```
## Multiple R-squared: 0.6094, Adjusted R-squared: 0.5207
## F-statistic: 6.865 on 10 and 44 DF, p-value: 2.406e-06
#step(lm13)
lm14 = lm(log(data_C$salary)~Age + MPG + PPG+ APG + TOPG ,data_C)
summary(lm14)
##
## Call:
## lm(formula = log(data_C$salary) ~ Age + MPG + PPG + APG + TOPG,
##
      data = data_C)
##
## Residuals:
##
                                           Max
       Min
                 1Q Median
                                   3Q
## -1.50213 -0.32268 -0.08718 0.52865 1.06823
##
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 12.24263
                         0.81784 14.969 < 2e-16 ***
                          0.02664
              0.04483
                                  1.682 0.0988 .
## Age
## MPG
                                  4.938 9.56e-06 ***
              0.13213
                          0.02676
## PPG
              -0.07345
                          0.04255 - 1.726
                                           0.0906 .
                          0.15191 -1.354
## APG
              -0.20575
                                           0.1818
## TOPG
              0.40084
                          0.24666
                                  1.625
                                          0.1106
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.6765 on 49 degrees of freedom
## Multiple R-squared: 0.5975, Adjusted R-squared: 0.5564
## F-statistic: 14.55 on 5 and 49 DF, p-value: 9.817e-09
library(car)
which(dffits(lm14)>2*sqrt(5/55))
## 4
## 1
which (abs(covratio(lm14)-1)>(3*5/55))
    4 15 77 97 121 271 290 335 349 375 397 437
        4 10 13 17 33 35 42 43 46 48 52
##
which(dfbetas(lm14)>(2/sqrt(55)))
## [1] 16 52 65 79 85 108 123 172 194 198 217 221 291 299 328
outlierTest(lm14)
## No Studentized residuals with Bonferroni p < 0.05
## Largest |rstudent|:
     rstudent unadjusted p-value Bonferroni p
## 77 -2.38438
                        0.021108
```

influencePlot(lm14)



```
## StudRes Hat CookD
## 77 -2.384380 0.04976428 0.04529258
## 97 -1.460625 0.63193724 0.59668766
## 112 -1.532146 0.24783823 0.12546553
## 257 -2.032457 0.05981689 0.04117218
## 271 0.576530 0.38697584 0.03545329

#Same varaibles in the model as before
data_C2 = data_C[-c(77,97,112,257,271),]
lm15 = lm(log(data_C2$salary)~.,data_C2[,c(4:13)])
#step(lm15)
```

PF

```
lmod1 = lm(log(data_PF$salary)~.,data_PF[,c(4:13)])
summary(lmod1)
```

```
##
## Call:
## lm(formula = log(data_PF$salary) ~ ., data = data_PF[, c(4:13)])
##
## Residuals:
##
       Min
                1Q Median
                                        Max
## -1.1625 -0.3874 -0.1142 0.4695
                                    1.0095
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) 11.30427
                            1.59214
                                      7.100 6.77e-08 ***
## Age
                0.09409
                            0.04147
                                      2.269
                                              0.0306 *
                            2.21292
                                     -1.046
## FG.
               -2.31517
                                              0.3038
## FT.
                0.66553
                            1.02312
                                      0.650
                                              0.5203
## MPG
                0.05307
                            0.03808
                                      1.393
                                              0.1737
```

```
## PPG
               0.03248
                          0.04320
                                   0.752
                                            0.4579
## APG
                          0.16426 2.078 0.0463 *
               0.34137
                          0.11319
## RPG
               0.24499
                                   2.165
                                          0.0385 *
                          0.49761 -1.744
## TOPG
              -0.86796
                                            0.0914
## BPG
               0.01858
                          0.33985
                                    0.055
                                            0.9568
## SPG
                          0.46112 -0.555
              -0.25579
                                           0.5832
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.6283 on 30 degrees of freedom
## Multiple R-squared: 0.6936, Adjusted R-squared: 0.5915
## F-statistic: 6.792 on 10 and 30 DF, p-value: 1.975e-05
#step(lmod1)
lmod2 = lm(log(data_PF$salary)~ Age + MPG + APG + RPG + TOPG ,data_PF)
summary(lmod2)
##
## Call:
## lm(formula = log(data_PF$salary) ~ Age + MPG + APG + RPG + TOPG,
      data = data_PF)
##
## Residuals:
##
       Min
                 1Q
                     Median
                                   3Q
                                           Max
## -1.21872 -0.47668 -0.02955 0.42568 1.10189
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 10.91984
                          1.11232
                                   9.817 1.37e-11 ***
                          0.03706
                                    2.185 0.03564 *
## Age
               0.08100
## MPG
                          0.02647
                                    2.796 0.00835 **
               0.07401
## APG
              0.29177
                          0.15149
                                    1.926 0.06226 .
## RPG
               0.20414
                          0.09802
                                    2.083 0.04466 *
## TOPG
              -0.73215
                          0.42175 -1.736 0.09136 .
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.6126 on 35 degrees of freedom
## Multiple R-squared: 0.6602, Adjusted R-squared: 0.6117
## F-statistic: 13.6 on 5 and 35 DF, p-value: 2.136e-07
SF
lmod3 = lm(log(data_SF$salary)~.,data_SF[,c(4:13)])
summary(lmod3)
##
## Call:
## lm(formula = log(data_SF$salary) ~ ., data = data_SF[, c(4:13)])
## Residuals:
                 1Q
                     Median
                                   3Q
## -1.66711 -0.34751 -0.06671 0.29731 1.37242
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
```

```
## (Intercept) 10.82433
                          2.96840
                                    3.647 0.00172 **
                          0.04665
                                    2.525 0.02063 *
## Age
               0.11778
                          4.07044
## FG.
               0.20730
                                   0.051 0.95992
                          2.52128 -0.426 0.67478
## FT.
              -1.07448
## MPG
               0.08865
                          0.05711
                                    1.552 0.13709
## PPG
              -0.01268
                          0.08101 -0.157 0.87729
                          0.36463 -0.522 0.60738
## APG
              -0.19051
                                   -0.389 0.70193
## RPG
              -0.09161
                          0.23577
              0.88853
## TOPG
                          1.01848
                                    0.872 0.39388
## BPG
              0.12819
                          0.59110
                                   0.217 0.83062
## SPG
              -0.35881
                          0.54569 -0.658 0.51872
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.8075 on 19 degrees of freedom
## Multiple R-squared: 0.5542, Adjusted R-squared: 0.3196
## F-statistic: 2.362 on 10 and 19 DF, p-value: 0.05129
#step(lmod3)
lmod4 = lm(log(data_SF$salary)~ Age + MPG + TOPG ,data_SF)
summary(lmod4)
##
## Call:
## lm(formula = log(data_SF$salary) ~ Age + MPG + TOPG, data = data_SF)
## Residuals:
##
                 1Q
                    Median
## -1.63686 -0.49200 0.01551 0.29576 1.42490
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
                                    9.593
## (Intercept) 10.68042
                          1.11337
                                             5e-10 ***
               0.10649
                          0.03348
                                    3.181 0.00378 **
## Age
## MPG
               0.05701
                          0.02772
                                    2.057 0.04985 *
## TOPG
               0.41064
                          0.30520
                                    1.345 0.19008
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.7049 on 26 degrees of freedom
## Multiple R-squared: 0.5351, Adjusted R-squared: 0.4814
## F-statistic: 9.974 on 3 and 26 DF, p-value: 0.0001496
```