

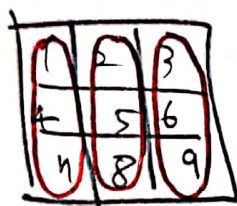
10/25

$$\begin{bmatrix} a_1 & a_2 \\ a_3 & a_4 \end{bmatrix} \begin{matrix} 32 \text{ bits} \times 4 \\ = 128 \text{ bits} \end{matrix}$$

$$\begin{bmatrix} a_1 & a_2 \\ a_3 & a_4 \end{bmatrix} \cdot \begin{bmatrix} b_1 & b_2 \\ b_3 & b_4 \end{bmatrix} =$$

2×2

$$\begin{bmatrix} a_1 \cdot b_1 + a_2 \cdot b_3 & a_1 \cdot b_2 + a_2 \cdot b_4 \\ a_3 \cdot b_1 + a_4 \cdot b_3 & a_3 \cdot b_2 + a_4 \cdot b_4 \end{bmatrix}$$



→

| | | | | | | | | |
|---|---|---|---|---|---|---|---|---|
| 1 | 4 | 7 | 2 | 5 | 8 | 3 | 6 | 9 |
|---|---|---|---|---|---|---|---|---|

column major

↳ If you ignore the sparsity, you may store the matrix in either row-major order or column-major order.

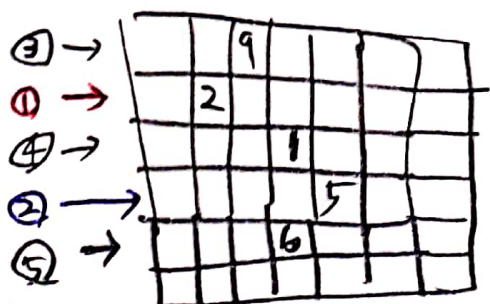
popular format = COO, CSR

Row =

| | | | | |
|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 |
| 1 | 3 | 0 | 2 | 4 |

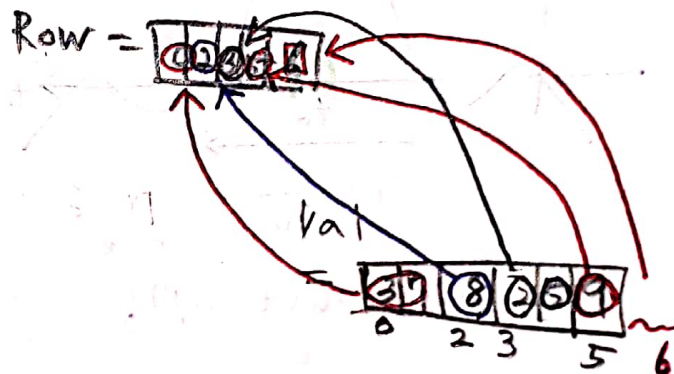
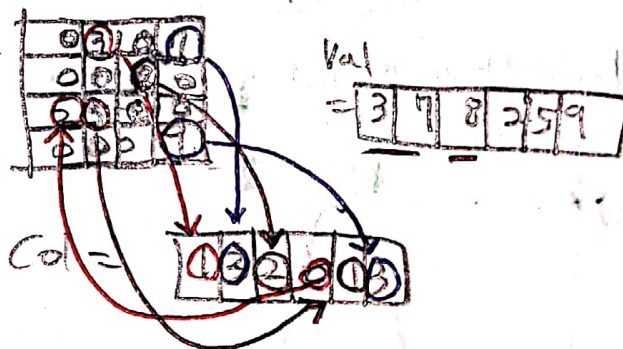
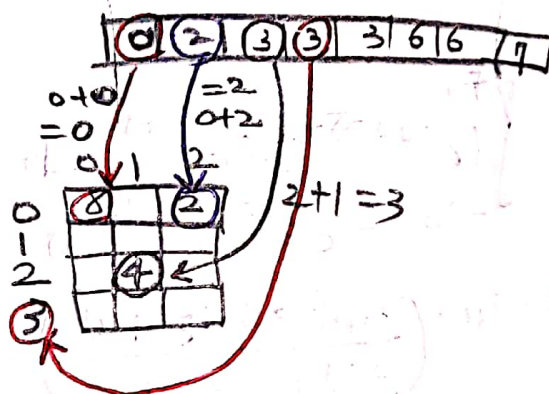
data =

| | | | | |
|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 |
| 2 | 5 | 9 | 1 | 6 |

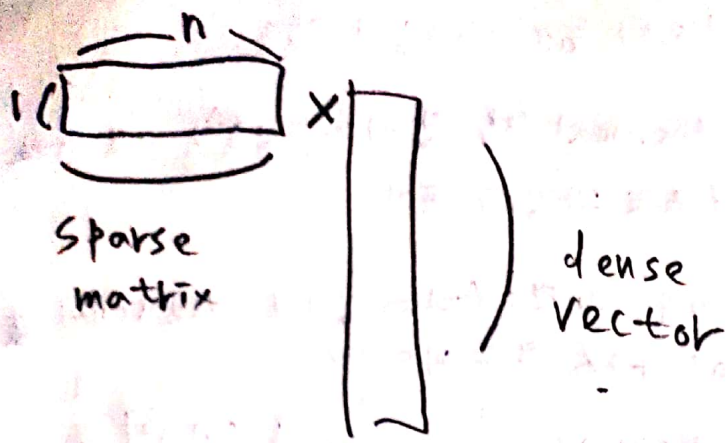


CSR = compressed sparse rows.

↳ store the column of each non-zero element, and which column indices belong to each row.

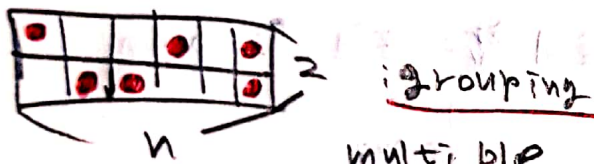


<1>



\Rightarrow vector-wise operation.

grouping multiple vectors
lead to more number of wasted
computation.



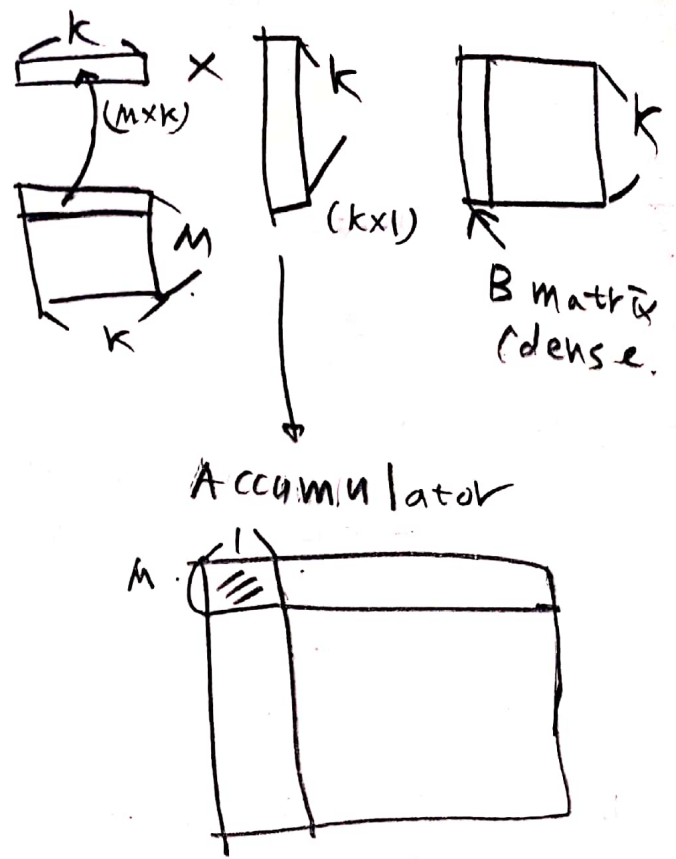
• 위키다스네가 dense vector가
이런보다 계산 양이 ↑.

meta data



<2>

2-bits
indices



<pruning initialization>

training \rightarrow **pruning** \rightarrow retraining

Folk knowledge

① Without an initial training
 \hookrightarrow The pruned model cannot be
optimized well

② final model does not
generalize well

Can prune at the initial
stage without performance
drop.

\hookrightarrow There are other methods
called Grasp / synFlow, but
SNIP perform best.

<3>

layerwise sparsity.

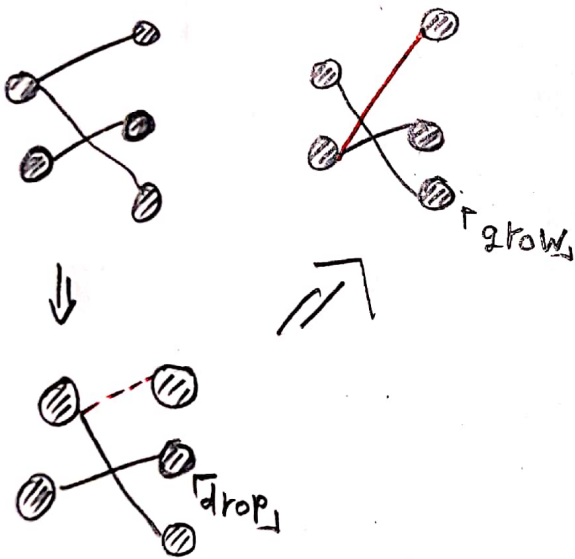
taylor approximation

$$L(\tilde{\theta}) \approx L(\theta) + (\tilde{\theta} - \theta)^T G_{\theta} + \frac{1}{2} (\tilde{\theta} - \theta)^T H_{\theta} (\tilde{\theta} - \theta)$$

$H_{\theta} \cdot (\tilde{\theta} - \theta)$

sparse training = Limitation

: Peak memory is still the same as dense.



Sparsity $\downarrow \Rightarrow$ test accuracy $\uparrow \uparrow$

Good layerwise sparsity & schedule

Pruning

① MINIMIZING the loss after pruning

② MAXIMIZING the re-trainability

$$CD = \frac{1}{n} \sum_{i=1}^n \frac{\partial L}{\partial \theta_i} \quad (4.12)$$

(2) is viewed as the most important decision criterion.