



Searching and Hash structure

Data Structures and Algorithms

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① Searching algorithms

Sequential Search

Interval Search

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Interval Search

② Hash table

Basic concepts

Direct-address tables

Hash tables

Hash functions

Open addressing

Hash table

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SEARCHING ALGORITHMS



Definition

Searching Algorithms are designed to check for an element or retrieve an element from any data structure where it is stored. Based on the type of search operation, these algorithms are generally classified into two categories:

- ① **Sequential Search:** In this, the list or array is traversed sequentially and every element is checked.
- ② **Interval Search:** These algorithms are specifically designed for searching in sorted data-structures.

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Approach

- ① Start from the leftmost element of list and one by one compare x with each element of list.
- ② If x matches with an element, return the index.
- ③ If x doesn't match with any of elements, return -1.



Approach

- ① Start from the leftmost element of list and one by one compare x with each element of list.
- ② If x matches with an element, return the index.
- ③ If x doesn't match with any of elements, return -1.

The **time complexity** of the above algorithm is $O(n)$.



Approach

Search a sorted array by repeatedly dividing the search interval in half. Begin with an interval covering the whole array.

- ① If the value of the search key is **less than** the item in the middle of the interval, narrow the interval to the lower half, otherwise narrow it to the upper half.
- ② Repeatedly check until the value is found or the interval is empty.



Approach

Search a sorted array by repeatedly dividing the search interval in half. Begin with an interval covering the whole array.

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Implementation:

- Recursive
- Iterative

Time complexity: $O(\log n)$

Approach

Jump Search is a searching algorithm for sorted arrays. The basic idea is to check **fewer elements** (than linear search) by jumping ahead by fixed steps or skipping some elements in place of searching all elements.





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Suppose that an array **arr** of size **n** divided to some blocks with fixed size **m** .

- 1 Find the block **k** such that the first element of block **k** is less than **key** and the first element of block **$k + 1$** is greater than or equals to **key**.
- 2 Perform the linear search on the block **k** .



Approach

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- 1 Find the block **k** such that the first element of block **k** is less than **key** and the first element of block **$k + 1$** is greater than or equals to **key**.
- 2 Perform the linear search on the block **k** .

Time complexity: \sqrt{n} .



Consider the following array:

[0, 1, 1, 2, 3, 5, 8, 13, 21, 34, 55, 89, 144, 233, 377, 610].

Length of the array is 16, block size is 4.

- ➊ Jump from index 0 to index 4.
- ➋ Jump from index 4 to index 8.
- ➌ Jump from index 8 to index 12.
- ➍ Since the element at index 12 is greater than 55 we will jump back a step to come to index 8.
- ➎ Do linear search from index 8 to get the element 55.

Approach

Interpolation Search is an improvement over Binary Search for instances, where the values in a sorted array are uniformly distributed.

- 1 Calculate the value of **pos** using the probe position formula.

$$\text{pos} = \text{lo} + \frac{(x - \text{arr}[\text{lo}]) \times (\text{hi} - \text{lo})}{\text{arr}[\text{hi}] - \text{arr}[\text{lo}]}$$

where

- **arr**: array where elements need to be searched.
- **x**: element to be searched.
- **lo**: starting index in **arr**.
- **hi**: ending index in **arr**.



Approach

Interpolation Search is an improvement over Binary Search for instances, where the values in a sorted array are uniformly distributed.

- 1 Calculate the value of **pos** using the probe position formula.
- 2 If it is a match, return the index of the item, and exit.

Time complexity:

- If elements are uniformly distributed, then $O(\log \log n)$.
- In worst case, it can take up to $O(n)$.



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- 3 If the item is **less than** $\text{arr}[\text{pos}]$, calculate the probe position of the left sub-array. Otherwise calculate the same in the right sub-array.

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- 1 Calculate the value of **pos** using the probe position formula.
- 2 If it is a match, return the index of the item, and exit.
- 3 If the item is **less than** `arr[pos]`, calculate the probe position of the left sub-array. Otherwise calculate the same in the right sub-array.
- 4 Repeat until a match is found or the sub-array reduces to zero.

Time complexity:

- If elements are uniformly distributed, then $O(\log \log n)$.
- In worst case, it can take up to $O(n)$.



Search the element 18 in array [10, 12, 13, 16, 18, 19, 20, 21, 22, 23, 24, 33, 35, 42, 47].

① Calculate the probe position:

$$\text{pos} = 0 + \frac{(18 - 10) \times (14 - 0)}{47 - 10} = 3$$



Interpolation Search

Search the element 18 in array [10, 12, 13, 16, 18, 19, 20, 21, 22, 23, 24, 33, 35, 42, 47].

- 1 Calculate the probe position:

$$\text{pos} = 0 + \frac{(18 - 10) \times (14 - 0)}{47 - 10} = 3$$

- 2 $\text{arr}[3] = 16 > 18 = x \Rightarrow$ Search from `index = 4` to the end `index = 14`.



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Interpolation Search

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Interpolation Search

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- ④ $\text{arr}[4] = 18 = x \Rightarrow$ End.





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HASH TABLE

- Sequential search: $O(n)$
- Binary search: $O(\log_2 n)$

→ Requiring several **key comparisons** before the target is found.





Search complexity:

Size	Binary	Sequential (Average)	Sequential (Worst Case)
16	4	8	16
50	6	25	50
256	8	128	256
1,000	10	500	1,000
10,000	14	5,000	10,000
100,000	17	50,000	100,000
1,000,000	20	500,000	1,000,000

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Is there a search algorithm whose complexity is $O(1)$?

Is there a search algorithm whose complexity is $O(1)$?

YES



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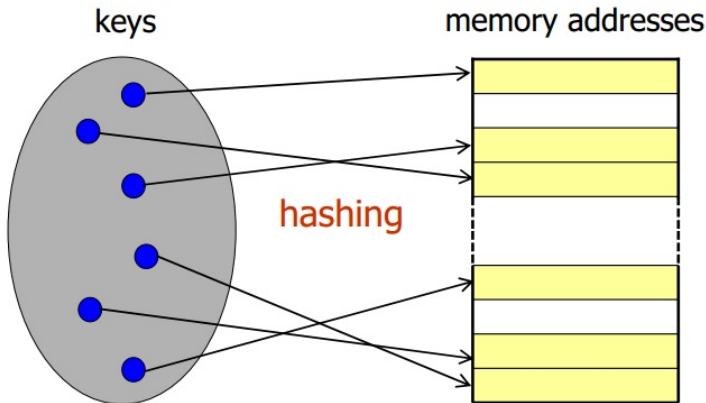
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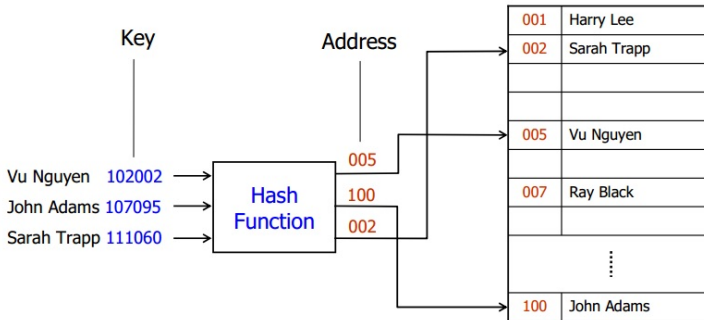
Hash tables

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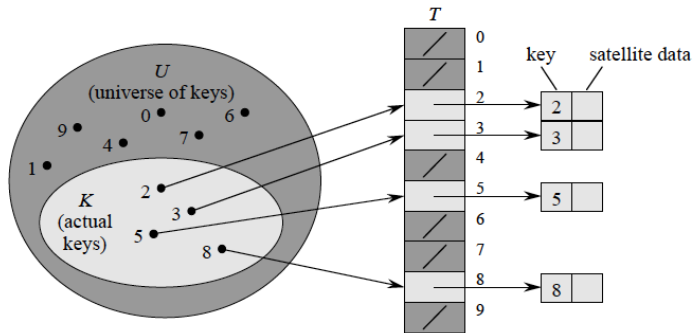
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Direct-address tables

Definition

Direct-address table is a structure using an array denoted by $T[0 \dots m - 1]$, in which each position, or **slot**, corresponds to a key in the universe U .



(Source: Introduction to algorithms - 3rd edition)



Direct-address tables

DIRECT-ADDRESS-SEARCH(T, k)

1 **return** $T[k]$

DIRECT-ADDRESS-INSERT(T, x)

1 $T[x.key] = x$

DIRECT-ADDRESS-DELETE(T, x)

1 $T[x.key] = \text{NIL}$



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Direct-address tables

DIRECT-ADDRESS-SEARCH(T, k)

1 **return** $T[k]$

DIRECT-ADDRESS-INSERT(T, x)

1 $T[x.key] = x$

DIRECT-ADDRESS-DELETE(T, x)

1 $T[x.key] = \text{NIL}$

Each of these operations takes only $O(1)$ time.



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- If the universe U is large, storing a table T of size $|U|$ may be impractical, or even impossible.
- The set K of keys *actually stored* may be so small relative to U that most of the space allocated for T would be wasted.





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- Sequential Search
- Interval Search

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Hash tables

- Hash functions
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Definition

Hash table is a dynamic set that supports only the dictionary operations INSERT, SEARCH, and DELETE with the average time to search for an element $O(1)$ but requires much less storage than the universe U of all possible keys.



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- With direct addressing, an element with key k is stored in slot k .
- With hashing, this element is stored in slot $h(k)$. **Hash function** h computes the slot from the key k that maps the universe keys U into the slots of a hash table $T[0 \dots m - 1]$:

$$h : U \rightarrow \{0, 1, \dots, m - 1\}$$

where $m \ll |U|$.



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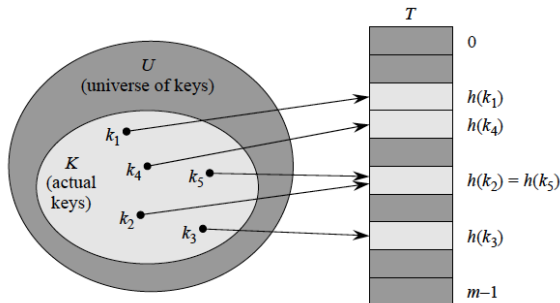
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Hash tables

Definition

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(Source: Introduction to algorithms - 3rd edition)



There is one hitch: two keys may hash to the same slot. We call this situation a **collision**. Fortunately, we have effective techniques for resolving the conflict created by collisions.



Searching algorithms

- Sequential Search
- Interval Search

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There is one hitch: two keys may hash to the same slot. We call this situation a **collision**. Fortunately, we have effective techniques for resolving the conflict created by collisions.

- Ideal solution: avoid collisions altogether, try to achieve this goal by choosing a suitable hash function h .



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There is one hitch: two keys may hash to the same slot. We call this situation a **collision**. Fortunately, we have effective techniques for resolving the conflict created by collisions.

- Ideal solution: avoid collisions altogether, try to achieve this goal by choosing a suitable hash function h .
- Simplest solution: collision resolution by chaining.



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Collision resolution by chaining



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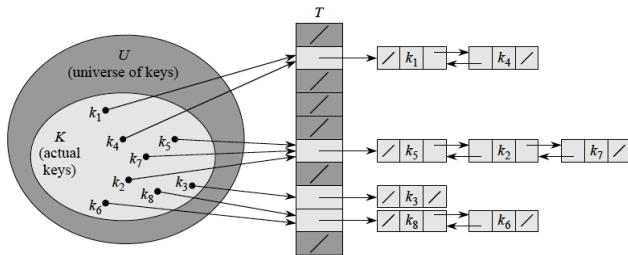
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Definition

In **chaining**, we place all the elements that hash to the same slot into the same linked list.



(Source: Introduction to algorithms - 3rd edition)



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Definition

In **chaining**, we place all the elements that hash to the same slot into the same linked list.

CHAINED-HASH-INSERT(T, x)

- 1 insert x at the head of list $T[h(x.key)]$

CHAINED-HASH-SEARCH(T, k)

- 1 search for an element with key k in list $T[h(k)]$

CHAINED-HASH-DELETE(T, x)

- 1 delete x from the list $T[h(x.key)]$



Definition

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1 delete x from the list $T[h(x.key)]$

The worst-case behavior of hashing with chaining is terrible: all n keys hash to the same slot, creating a list of length n .

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HASH FUNCTIONS

Interpreting keys as natural numbers

- Most hash functions assume that the universe of keys is the set $\mathbb{N} = \{0, 1, 2, \dots\}$.
- If the keys are not natural numbers, we find a way to interpret them as natural numbers.



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Interpreting keys as natural numbers

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- If the keys are not natural numbers, we find a way to interpret them as natural numbers.

Example

Interpret the key in string `pt` as natural number.



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Interpreting keys as natural numbers

- Most hash functions assume that the universe of keys is the set $\mathbb{N} = \{0, 1, 2, \dots\}$.
- If the keys are not natural numbers, we find a way to interpret them as natural numbers.

Example

Interpret the key in string `pt` as natural number.

Since `p` = 112, `t` = 116, express it as a radix-128 integer. It becomes $(112 \times 128) + 116 = 14452$



Searching algorithms

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A good hash function

A good hash function satisfies (approximately) the assumption of simple uniform hashing (SUHA): each key is equally likely to hash to any of the m slots, independently of where any other key has hashed to.



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- Division method
- Multiplication method
- Universal hashing
- Other methods



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Definition

In the **division method** for creating hash functions, we map a key k into one of m slots by taking the remainder of k divided by m . That is, the hash function is

$$h(k) = k \bmod m$$



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Example

If the hash table has size $m = 12$ and the key is $k = 100$, then $h(k) = 4$



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Example

If the hash table has size $m = 12$ and the key is $k = 100$, then $h(k) = 4$

Value of m :

- m should not be a power of 2.
- m should be a prime not too close to an exact power of 2.





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Definition

The multiplication method for creating hash functions operates in two steps:

- 1 Multiply the key k by a constant A in the range $(0, 1)$ and extract the fractional part of kA .
- 2 Multiply this value by m and take the floor of the result.

In short, the hash function is

$$h(k) = \lfloor m (kA \bmod 1) \rfloor$$

where $kA \bmod 1$ means $kA - \lfloor kA \rfloor$.

Address = selected digits from Key

Example:

379452 → 394

121267 → 112

378845 → 388

160252 → 102

045128 → 051



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Address = middle digits of Key^2

Example:

$$9452 * 9452 = 89340304 \rightarrow 3403$$

- **Disadvantage:** the size of the Key^2 is too large.
- **Variations:** use only a portion of the key.

Example:

379452: $379 * 379 = 143641 \rightarrow 364$ 121267:
 $121 * 121 = 014641 \rightarrow 464$ 045128: $045 * 045 = 002025 \rightarrow 202$



The key is divided into parts whose size matches the address size.

Example:

Key = 123||456||789

fold shift

$123 + 456 + 789 = 1368$

→ 368



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The key is divided into parts whose size matches the address size.

Example:

Key = 123||456||789

fold shift

$$123 + 456 + 789 = 1368$$

→ 368

fold boundary

$$321 + 456 + 987 = 1764$$

→ 764



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- Hashing keys that are identical except for the last character may create synonyms.
- The key is rotated before hashing.

original key	rotated key
--------------	-------------

600101	160010
--------	--------

600102	260010
--------	--------

600103	360010
--------	--------

600104	460010
--------	--------

600105	560010
--------	--------



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- Used in combination with fold shift.

original key	rotated key
600101 → 62	160010 → 26
600102 → 63	260010 → 36
600103 → 64	360010 → 46
600104 → 65	460010 → 56
600105 → 66	560010 → 66

Spreading the data more evenly across the address space.



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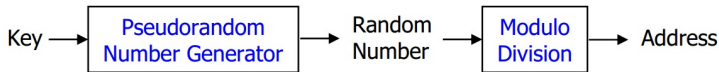
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$$y = ax + c$$

For maximum efficiency, a and c should be prime numbers.



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Example:

Key = 121267

$a = 17$

$c = 7$

listSize = 307

$$\begin{aligned}\text{Address} &= ((17 * 121267 + 7) \bmod 307) \\ &= (2061539 + 7) \bmod 307 \\ &= 2061546 \bmod 307 \\ &= 41\end{aligned}$$


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When a collision occurs, an **unoccupied element** is searched for placing the new element in (probing).

Hash function:

$$h : U \times \{0, 1, 2, \dots, m - 1\} \rightarrow \{0, 1, 2, \dots, m - 1\}$$

For every key k , the **probe sequence**:

$$\langle h(k, 0), h(k, 1), \dots, h(k, m - 1) \rangle$$



When a collision occurs, an **unoccupied element** is searched for placing the new element in (probing).

Hash function:

$$h : U \times \{0, 1, 2, \dots, m - 1\} \rightarrow \{0, 1, 2, \dots, m - 1\}$$

For every key k , the **probe sequence**:

$$\langle h(k, 0), h(k, 1), \dots, h(k, m - 1) \rangle$$

be a permutation of $\langle 0, 1, \dots, m - 1 \rangle$

Open Addressing

```
1 Algorithm hashInsert(ref T <array>, val k <key>)  
2 Inserts key k into table T.  
  
3 i = 0  
4 while i < m do  
5     j = h(k, i)  
6     if T[j] = nil then  
7         T[j] = k  
8         return j  
9     else  
10        i = i + 1  
11    end  
12 end  
13 return error: "hash table overflow"  
14 End hashInsert
```



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```
1 Algorithm hashSearch(val T <array>, val k <key>)
2 Searches for key k in table T.

3 i = 0
4 while i < m do
5     j = h(k, i)
6     if T[j] = k then
7         | return j
8     else if T[j] = nil then
9         | return nil
10    else
11        | i = i + 1
12    end
13 end
14 return nil
15 End hashSearch
```



Given an ordinary hash function $h' : U \rightarrow \{0, 1, 2, \dots, m-1\}$, which we refer to as an **auxiliary hash function**, the method of **linear probing** uses the hash function

$$h(k, i) = (h'(k) + ci) \mod m$$

where c is positive auxiliary constant.



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$$h(k, i) = (h'(k) + ci) \mod m$$

where c is positive auxiliary constant.

Example

$$h'(k) = k \mod 11$$

$$h(k, i) = (h'(k) + i) \mod m$$

Insert 10, 22, 31, 4, 15, 28, 17, 88, 59 into hash table.



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Linear Probing

Insert 10.

$$h(10, 0) = (h'(10) + 0) \bmod 11 = 10.$$

0	1	2	3	4	5	6	7	8	9	10
										10



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Insert 22.

$$h(22, 0) = (h'(22) + 0) \bmod 11 = 0.$$

0	1	2	3	4	5	6	7	8	9	10
22										10



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Insert 31.

$$h(31, 0) = (h'(31) + 0) \bmod 11 = 9.$$

0	1	2	3	4	5	6	7	8	9	10
22									31	10



Searching algorithms

Sequential Search

Interval Search

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Basic concepts

Direct-address tables

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Open addressing

Insert 4.

$$h(4, 0) = (h'(4) + 0) \bmod 11 = 4.$$

0	1	2	3	4	5	6	7	8	9	10
22				4					31	10

Linear Probing

Insert 15.

$$h(15, 0) = (h'(15) + 0) \bmod 11 = 4. \text{ Collision.}$$

0	1	2	3	4	5	6	7	8	9	10
22				4					31	10



Searching algorithms

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Open addressing

Insert 15.

$$h(15, 0) = (h'(15) + 0) \bmod 11 = 4. \text{ Collision.}$$

$$h(15, 1) = (h'(15) + 1) \bmod 11 = 5.$$

0	1	2	3	4	5	6	7	8	9	10
22				4	15				31	10

Linear Probing



Searching algorithms

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Insert 28.

$$h(28, 0) = (h'(28) + 0) \bmod 11 = 6.$$

0	1	2	3	4	5	6	7	8	9	10
22				4	15	28			31	10



Searching algorithms

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Open addressing

Insert 17.

$$h(17, 0) = (h'(17) + 0) \bmod 11 = 6. \text{ Collision.}$$

0	1	2	3	4	5	6	7	8	9	10
22				4	15	28			31	10



Searching algorithms

Sequential Search

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Open addressing

Insert 17.

$$h(17, 0) = (h'(17) + 0) \bmod 11 = 6. \text{ Collision.}$$

$$h(17, 1) = (h'(17) + 1) \bmod 11 = 7.$$

0	1	2	3	4	5	6	7	8	9	10
22				4	15	28	17		31	10



Searching algorithms

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Open addressing

Insert 88.

$$h(88, 0) = (h'(88) + 0) \bmod 11 = 0. \text{ Collision.}$$

0	1	2	3	4	5	6	7	8	9	10
22				4	15	28	17		31	10



Searching algorithms

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Open addressing

Insert 88.

$$h(88, 0) = (h'(88) + 0) \bmod 11 = 0. \text{ Collision.}$$

$$h(88, 1) = (h'(88) + 1) \bmod 11 = 1.$$

0	1	2	3	4	5	6	7	8	9	10
22	88			4	15	28	17		31	10



Searching algorithms

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Open addressing

Insert 59.

$$h(59, 0) = (h'(59) + 0) \bmod 11 = 4. \text{ Collision.}$$

0	1	2	3	4	5	6	7	8	9	10
22	88			4	15	28	17		31	10



Searching algorithms

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Open addressing

Insert 59.

$$h(59, 0) = (h'(59) + 0) \bmod 11 = 4. \text{ Collision.}$$

$$h(59, 1) = (h'(59) + 1) \bmod 11 = 5. \text{ Collision.}$$

0	1	2	3	4	5	6	7	8	9	10
22	88			4	15	28	17		31	10



Searching algorithms

Sequential Search

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Open addressing

Insert 59.

$$h(59, 0) = (h'(59) + 0) \bmod 11 = 4. \text{ Collision.}$$

$$h(59, 1) = (h'(59) + 1) \bmod 11 = 5. \text{ Collision.}$$

$$h(59, 2) = (h'(59) + 2) \bmod 11 = 6. \text{ Collision.}$$

0	1	2	3	4	5	6	7	8	9	10
22	88			4	15	28	17		31	10



Searching algorithms

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Open addressing

Insert 59.

$$h(59, 0) = (h'(59) + 0) \bmod 11 = 4. \text{ Collision.}$$

$$h(59, 1) = (h'(59) + 1) \bmod 11 = 5. \text{ Collision.}$$

$$h(59, 2) = (h'(59) + 2) \bmod 11 = 6. \text{ Collision.}$$

$$h(59, 3) = (h'(59) + 3) \bmod 11 = 7. \text{ Collision.}$$

0	1	2	3	4	5	6	7	8	9	10
22	88			4	15	28	17		31	10



Searching algorithms

Sequential Search

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Open addressing

Insert 59.

$$h(59, 0) = (h'(59) + 0) \bmod 11 = 4. \text{ Collision.}$$

$$h(59, 1) = (h'(59) + 1) \bmod 11 = 5. \text{ Collision.}$$

$$h(59, 2) = (h'(59) + 2) \bmod 11 = 6. \text{ Collision.}$$

$$h(59, 3) = (h'(59) + 3) \bmod 11 = 7. \text{ Collision.}$$

$$h(59, 4) = (h'(59) + 4) \bmod 11 = 8.$$

0	1	2	3	4	5	6	7	8	9	10
22	88			4	15	28	17	59	31	10

Linear probing: Evaluation

- Easy to implement.
- Suffers from a problem as **primary clustering**.



Searching algorithms

Sequential Search

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Searching algorithms

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Hash functions

Open addressing

Quadratic probing uses a hash function of the form

$$h(k, i) = (h'(k) + c_1i + c_2i^2) \mod m$$

where h' is an auxiliary hash function, c_1 and c_2 are positive auxiliary constants, and $i = 0, 1, \dots, m - 1$.



Searching algorithms

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Open addressing

Quadratic probing uses a hash function of the form

$$h(k, i) = (h'(k) + c_1i + c_2i^2) \mod m$$

where h' is an auxiliary hash function, c_1 and c_2 are positive auxiliary constants, and $i = 0, 1, \dots, m - 1$.

Example

$$h'(k) = k \mod 11$$

$$c_1 = 1, c_2 = 3 \Rightarrow h(k, i) = (h'(k) + i + 3i^2) \mod 11$$

Insert 10, 22, 31, 4, 15, 28, 17, 88, 59 into hash table.

Quadratic Probing

Insert 10.

$$h(10,0) = (h'(10) + 0) \bmod 11 = 10.$$

0	1	2	3	4	5	6	7	8	9	10
										10



Searching algorithms

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Quadratic Probing

Insert 22.

$$h(22, 0) = (h'(22) + 0) \bmod 11 = 0.$$

0	1	2	3	4	5	6	7	8	9	10
22										10



Searching algorithms

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Quadratic Probing

Insert 31.

$$h(31, 0) = (h'(31) + 0) \bmod 11 = 9.$$

0	1	2	3	4	5	6	7	8	9	10
22									31	10



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Quadratic Probing

Insert 4.

$$h(4, 0) = (h'(4) + 0) \bmod 11 = 4.$$

0	1	2	3	4	5	6	7	8	9	10
22				4					31	10



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Quadratic Probing

Insert 15.

$$h(15, 0) = (h'(15) + 0) \bmod 11 = 4. \text{ Collision.}$$

0	1	2	3	4	5	6	7	8	9	10
22				4					31	10



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Insert 15.

$$h(15, 0) = (h'(15) + 0) \bmod 11 = 4. \text{ Collision.}$$

$$h(15, 1) = (h'(15) + 1 + 3 \times 1^2) \bmod 11 = 8.$$

0	1	2	3	4	5	6	7	8	9	10
22				4				15	31	10

Quadratic Probing

Insert 28.

$$h(28, 0) = (h'(28) + 0) \bmod 11 = 6.$$

0	1	2	3	4	5	6	7	8	9	10
22				4		28		15	31	10



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Quadratic Probing

Insert 17.

$$h(17, 0) = (h'(17) + 0) \bmod 11 = 6. \text{ Collision.}$$

0	1	2	3	4	5	6	7	8	9	10
22				4		28		15	31	10



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Insert 17.

$$h(17, 0) = (h'(17) + 0) \bmod 11 = 6. \text{ Collision.}$$

$$h(17, 1) = (h'(17) + 1 + 3 \times 1^2) \bmod 11 = 10. \text{ Collision.}$$

0	1	2	3	4	5	6	7	8	9	10
22				4		28		15	31	10

Quadratic Probing



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Insert 17.

$$h(17,0) = (h'(17) + 0) \bmod 11 = 6. \text{ Collision.}$$

$$h(17,1) = (h'(17) + 1 + 3 \times 1^2) \bmod 11 = 10. \text{ Collision.}$$

$$h(17,2) = (h'(17) + 2 + 3 \times 2^2) \bmod 11 = 9. \text{ Collision.}$$

0	1	2	3	4	5	6	7	8	9	10
22				4		28		15	31	10

Quadratic Probing



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Insert 17.

$$h(17, 0) = (h'(17) + 0) \bmod 11 = 6. \text{ Collision.}$$

$$h(17, 1) = (h'(17) + 1 + 3 \times 1^2) \bmod 11 = 10. \text{ Collision.}$$

$$h(17, 2) = (h'(17) + 2 + 3 \times 2^2) \bmod 11 = 9. \text{ Collision.}$$

$$h(17, 3) = (h'(17) + 3 + 3 \times 3^2) \bmod 11 = 3.$$

0	1	2	3	4	5	6	7	8	9	10
22			17	4		28		15	31	10

Quadratic Probing



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Open addressing

Insert 88.

$$h(88, 0) = (h'(88) + 0) \bmod 11 = 0. \text{ Collision.}$$

0	1	2	3	4	5	6	7	8	9	10
22			17	4		28		15	31	10

Quadratic Probing



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Open addressing

Insert 88.

$$h(88, 0) = (h'(88) + 0) \bmod 11 = 0. \text{ Collision.}$$

$$h(88, 1) = (h'(88) + 1 + 3 \times 1^2) \bmod 11 = 4. \text{ Collision.}$$

0	1	2	3	4	5	6	7	8	9	10
22			17	4		28		15	31	10

Quadratic Probing



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Insert 88.

$$h(88, 0) = (h'(88) + 0) \bmod 11 = 0. \text{ Collision.}$$

$$h(88, 1) = (h'(88) + 1 + 3 \times 1^2) \bmod 11 = 4. \text{ Collision.}$$

$$h(88, 2) = (h'(88) + 2 + 3 \times 2^2) \bmod 11 = 3. \text{ Collision.}$$

0	1	2	3	4	5	6	7	8	9	10
22			17	4		28		15	31	10

Quadratic Probing



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Insert 88.

$$h(88, 0) = (h'(88) + 0) \bmod 11 = 0. \text{ Collision.}$$

$$h(88, 1) = (h'(88) + 1 + 3 \times 1^2) \bmod 11 = 4. \text{ Collision.}$$

$$h(88, 2) = (h'(88) + 2 + 3 \times 2^2) \bmod 11 = 3. \text{ Collision.}$$

$$h(88, 3) = (h'(88) + 3 + 3 \times 3^2) \bmod 11 = 8. \text{ Collision.}$$

0	1	2	3	4	5	6	7	8	9	10
22			17	4		28		15	31	10

Quadratic Probing

Insert 88.

$$h(88, 0) = (h'(88) + 0) \bmod 11 = 0. \text{ Collision.}$$

$$h(88, 1) = (h'(88) + 1 + 3 \times 1^2) \bmod 11 = 4. \text{ Collision.}$$

$$h(88, 2) = (h'(88) + 2 + 3 \times 2^2) \bmod 11 = 3. \text{ Collision.}$$

$$h(88, 3) = (h'(88) + 3 + 3 \times 3^2) \bmod 11 = 8. \text{ Collision.}$$

$$h(88, 4) = (h'(88) + 4 + 3 \times 4^2) \bmod 11 = 8. \text{ Collision.}$$

.
. .

0	1	2	3	4	5	6	7	8	9	10
22			17	4		28		15	31	10



Quadratic Probing

Insert 88.

$$h(88, 0) = (h'(88) + 0) \bmod 11 = 0. \text{ Collision.}$$

$$h(88, 1) = (h'(88) + 1 + 3 \times 1^2) \bmod 11 = 4. \text{ Collision.}$$

$$h(88, 2) = (h'(88) + 2 + 3 \times 2^2) \bmod 11 = 3. \text{ Collision.}$$

$$h(88, 3) = (h'(88) + 3 + 3 \times 3^2) \bmod 11 = 8. \text{ Collision.}$$

$$h(88, 4) = (h'(88) + 4 + 3 \times 4^2) \bmod 11 = 8. \text{ Collision.}$$

.
. .
.

$$h(88, 8) = (h'(88) + 8 + 3 \times 8^2) \bmod 11 = 2.$$

0	1	2	3	4	5	6	7	8	9	10
22		88	17	4		28		15	31	10



Searching algorithms

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Quadratic Probing

Insert 59.

⋮

$$h(59, 2) = (h'(59) + 2 + 3 \times 2^2) \bmod 11 = 7.$$

0	1	2	3	4	5	6	7	8	9	10
22		88	17	4		28	59	15	31	10



Searching algorithms

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Quadratic probing: Evaluation

- Easy to implement.
- Suffers from a problem as **secondary clustering**.



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Open addressing

Double hashing offers one of the best methods available for open addressing because the permutations produced have many of the characteristics of randomly chosen permutations. **Double hashing** uses a hash function of the form

$$h(k, i) = (h_1(k) + ih_2(k)) \mod m$$

where h_1 and h_2 are auxiliary hash functions.



Double hashing offers one of the best methods available for open addressing because the permutations produced have many of the characteristics of randomly chosen permutations. **Double hashing** uses a hash function of the form

$$h(k, i) = (h_1(k) + ih_2(k)) \mod m$$

where h_1 and h_2 are auxiliary hash functions.

Example

$$h_1(k) = k \mod 11$$

$$h_2(k) = 1 + (k \mod 10)$$

$$h(k, i) = (h_1(k) + ih_2(k)) \mod 11$$

Insert 10, 22, 31, 4, 15, 28, 17, 88, 59 into hash table.



Double hashing

Insert 10.

$$h(10, 0) = (h_1(10) + 0 \times h_2(10)) \bmod 11 = 10.$$

0	1	2	3	4	5	6	7	8	9	10
										10



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Double hashing

Insert 22.

$$h(22, 0) = (h_1(22) + 0 \times h_2(22)) \bmod 11 = 0.$$

0	1	2	3	4	5	6	7	8	9	10
22										10



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Double hashing

Insert 31.

$$h(31, 0) = (h_1(31) + 0 \times h_2(31)) \bmod 11 = 9.$$

0	1	2	3	4	5	6	7	8	9	10
22									31	10



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Insert 4.

$$h(4, 0) = (h_1(4) + 0 \times h_2(4)) \bmod 11 = 4.$$

0	1	2	3	4	5	6	7	8	9	10
22				4					31	10

Double hashing

Insert 15.

$$h(15, 0) = (h_1(15) + 0 \times h_2(15)) \bmod 11 = 4. \text{ Collision.}$$

0	1	2	3	4	5	6	7	8	9	10
22				4					31	10



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Insert 15.

$$h(15, 0) = (h_1(15) + 0 \times h_2(15)) \bmod 11 = 4. \text{ Collision.}$$

$$h(15, 1) = (h_1(10) + 1 \times h_2(10)) \bmod 11 = 10.$$

Collision.

0	1	2	3	4	5	6	7	8	9	10
22				4					31	10

Double hashing

Insert 15.

$$h(15, 0) = (h_1(15) + 0 \times h_2(15)) \bmod 11 = 4. \text{ Collision.}$$

$$h(15, 1) = (h_1(10) + 1 \times h_2(10)) \bmod 11 = 10.$$

Collision.

$$h(15, 2) = (h_1(10) + 2 \times h_2(10)) \bmod 11 = 5.$$

0	1	2	3	4	5	6	7	8	9	10
22				4	15				31	10



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Insert 28.

$$h(28, 0) = (h_1(28) + 0 \times h_2(28)) \bmod 11 = 6.$$

0	1	2	3	4	5	6	7	8	9	10
22				4	15	28			31	10

Double hashing



Searching algorithms

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Insert 17.

$$h(17, 0) = (h_1(17) + 0 \times h_2(17)) \bmod 11 = 6.$$

Collision.

0	1	2	3	4	5	6	7	8	9	10
22				4	15	28			31	10

Double hashing



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Insert 17.

$$h(17, 0) = (h_1(17) + 0 \times h_2(17)) \bmod 11 = 6.$$

Collision.

$$h(17, 1) = (h_1(17) + 1 \times h_2(17)) \bmod 11 = 2.$$

0	1	2	3	4	5	6	7	8	9	10
22		17		4	15	28			31	10

Double hashing



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Insert 88.

$$h(88, 0) = (h_1(88) + 0 \times h_2(88)) \bmod 11 = 0.$$

Collision.

0	1	2	3	4	5	6	7	8	9	10
22		17		4	15	28			31	10

Double hashing

Insert 88.

$$h(88, 0) = (h_1(88) + 0 \times h_2(88)) \bmod 11 = 0.$$

Collision.

$$h(88, 1) = (h_1(88) + 1 \times h_2(88)) \bmod 11 = 9.$$

Collision.

0	1	2	3	4	5	6	7	8	9	10
22		17		4	15	28			31	10



Double hashing

Insert 88.

$$h(88, 0) = (h_1(88) + 0 \times h_2(88)) \bmod 11 = 0.$$

Collision.

$$h(88, 1) = (h_1(88) + 1 \times h_2(88)) \bmod 11 = 9.$$

Collision.

$$h(88, 2) = (h_1(88) + 2 \times h_2(88)) \bmod 11 = 7.$$

0	1	2	3	4	5	6	7	8	9	10
22		17		4	15	28	88		31	10



Double hashing



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Insert 59.

$$h(59, 0) = (h_1(59) + 0 \times h_2(59)) \bmod 11 = 4.$$

Collision.

0	1	2	3	4	5	6	7	8	9	10
22		17		4	15	28	88		31	10

Double hashing

Insert 59.

$$h(59, 0) = (h_1(59) + 0 \times h_2(59)) \bmod 11 = 4.$$

Collision.

$$h(59, 1) = (h_1(59) + 1 \times h_2(59)) \bmod 11 = 3.$$

0	1	2	3	4	5	6	7	8	9	10
22		17	59	4	15	28	88		31	10



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Open addressing

- Hashing data to **buckets** that can hold multiple pieces of data.
- Each bucket has an address and **collisions are postponed** until the bucket is full.



Bucket hashing

001	Mary Dodd (379452)
002	Sarah Trapp (070918)
	Harry Eagle (166702)
	Ann Georgis (367173)
003	Bryan Devaux (121267)
	Chris Walljasper(572556)
⋮	
307	Shouli Feldman (045128)



linear probing



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THANK YOU.



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