

## DDA3020 Assignment 1

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1-1)

1-1

$$\frac{df(w)}{dw} = \begin{bmatrix} \frac{\partial f}{\partial w_1} & \dots & \frac{\partial f}{\partial w_n} \\ \vdots & \ddots & \vdots \\ \frac{\partial f}{\partial w_d} & \dots & \frac{\partial f}{\partial w_d} \end{bmatrix} = \frac{d(w)}{dw} \times \text{?}^T$$
$$\hookrightarrow \frac{d(X^T w)}{dw} = \frac{d(w)}{dw} \times (X^T)^T = 1 \times X = X$$

1-1

$$\frac{d(y^T X w)}{dw} = (y^T X)^T = X^T y$$

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$$\begin{aligned} \frac{d(w^T X w)}{dw} &= \frac{d(w^T)}{dw} X w + w^T \frac{d(X w)}{dw} \\ &= X w + w^T X \\ &= X w + X^T w \\ &= (X + X^T) w \end{aligned}$$

1-2)

1.2

$$\min_{W, b} \sum_{i=1}^N \alpha_i \|y_i - Wx_i - b\|^2$$

①  $\|(X^T X)^{-1} X^T y - B\|$

- ②
1. Start with a random input value  
(0 is convention)
  2. Calculate the Partial Derivative of the function  
with respect to the original output value / position
  3. Repeat until Convergence

1-3)

1-3

$$\textcircled{1} (\lambda x + (1-\lambda)y)^4 = ((\lambda x + (1-\lambda)y)^2)^2 \leq (\lambda x^2 + (1-\lambda)y^2)^2 \leq \lambda x^4 + (1-\lambda)y^4$$

$$\begin{aligned} & \lambda^2 x^4 + 2\lambda(1-\lambda)x^2y^2 + (1-\lambda)^2y^4 - \lambda x^4 - (1-\lambda)y^4 \\ & \hookrightarrow (\lambda-1)x^4 + (\lambda-1)y^4 - 2(\lambda-1)x^2y^2 \\ & = (\lambda-1)(x^4 + y^4 - 2x^2y^2) \\ & = (\lambda-1)(x^2 - y^2)^2 \leq 0 \end{aligned}$$

$$(\lambda \in [0, 1])$$

1-3

$$\textcircled{2} |\lambda x + (1-\lambda)y| \leq \lambda|x| + (1-\lambda)|y|$$

$$|x+y| \leq |x| + |y|$$

$$\hookrightarrow |\lambda x + (1-\lambda)y| \leq |\lambda x| + |(1-\lambda)y|$$

$$\hookrightarrow |\lambda x + (1-\lambda)y| \leq \lambda|x| + (1-\lambda)|y|$$

$$(\lambda \in [0, 1])$$

1-3)

1-3

$$\textcircled{3} \|A(x+y)\| \leq \|Ax\| + \|Ay\|$$

$$\|A(x+y)\|^2 \leq \|Ax\|^2 + \|Ay\|^2$$

$$\|A(x+y)-b\|^2 \leq \|Ax-b\|^2 + \|Ay-b\|^2$$

$$\begin{aligned} \|A(\lambda x + (1-\lambda)y) - b\|^2 &\leq \|A(\lambda x) - b\|^2 + \|A((1-\lambda)y) - b\|^2 \\ &\leq \lambda^2 \|Ax-b\|^2 + (1-\lambda)^2 \|Ay-b\|^2 \\ &\leq \lambda \|Ax-b\|^2 + (1-\lambda) \|Ay-b\|^2 \end{aligned}$$

$$(\lambda \in [0,1])$$

1-4)

갤러리



1-4

$$\sigma^2 = E(x_i - \mu)^2 = \frac{1}{N} \sum_{i=1}^N (x_i - \mu)^2$$

(Is the definition of Variance)

$$\hookrightarrow \sigma_{ML}^2 = \frac{1}{N} \sum_{i=1}^N (x_i - \mu_{ML})^2$$

2-1)

<p>Trial 1 (Next_Tmax)</p> <ul style="list-style-type: none"><li>- Training Error RMSE: 0.0291502407</li><li>- Test Error RMSE: 0.1204407047</li></ul> <p>Trial 2 (Next_Tmax)</p> <ul style="list-style-type: none"><li>- Training Error RMSE: 0.0306539907</li><li>- Test Error RMSE: 0.1546279789</li></ul> <p>Trial 3 (Next_Tmax)</p> <ul style="list-style-type: none"><li>- Training Error RMSE: 0.0459930015</li><li>- Test Error RMSE: 0.0293782999</li></ul> <p>Trial 4 (Next_Tmax)</p> <ul style="list-style-type: none"><li>- Training Error RMSE: 0.0205958059</li><li>- Test Error RMSE: 0.0851275653</li></ul> <p>Trial 5 (Next_Tmax)</p> <ul style="list-style-type: none"><li>- Training Error RMSE: 0.067856742</li><li>- Test Error RMSE: 0.1470456242</li></ul> <p>Trial 6 (Next_Tmax)</p> <ul style="list-style-type: none"><li>- Training Error RMSE: 0.0411286329</li><li>- Test Error RMSE: 0.0487073477</li></ul> <p>Trial 7 (Next_Tmax)</p> <ul style="list-style-type: none"><li>- Training Error RMSE: 0.0723820473</li><li>- Test Error RMSE: 0.1272343491</li></ul> <p>Trial 8 (Next_Tmax)</p> <ul style="list-style-type: none"><li>- Training Error RMSE: 0.0718629216</li><li>- Test Error RMSE: 0.0705387448</li></ul> <p>Trial 9 (Next_Tmax)</p> <ul style="list-style-type: none"><li>- Training Error RMSE: 0.0426002037</li><li>- Test Error RMSE: 0.0406797655</li></ul> <p>Trial 10 (Next_Tmax)</p> <ul style="list-style-type: none"><li>- Training Error RMSE: 0.0489320446</li><li>- Test Error RMSE: 0.1698338441</li></ul>	<p>Trial 1 (Next_Tmin)</p> <ul style="list-style-type: none"><li>- Training Error RMSE: 0.0092956914</li><li>- Test Error RMSE: 0.0834975961</li></ul> <p>Trial 2 (Next_Tmin)</p> <ul style="list-style-type: none"><li>- Training Error RMSE: 0.0292812932</li><li>- Test Error RMSE: 0.0561980276</li></ul> <p>Trial 3 (Next_Tmin)</p> <ul style="list-style-type: none"><li>- Training Error RMSE: 0.0353417875</li><li>- Test Error RMSE: 0.0155197476</li></ul> <p>Trial 4 (Next_Tmin)</p> <ul style="list-style-type: none"><li>- Training Error RMSE: 0.0338352823</li><li>- Test Error RMSE: 0.0002082216</li></ul> <p>Trial 5 (Next_Tmin)</p> <ul style="list-style-type: none"><li>- Training Error RMSE: 0.076820417</li><li>- Test Error RMSE: 0.0240910251</li></ul> <p>Trial 6 (Next_Tmin)</p> <ul style="list-style-type: none"><li>- Training Error RMSE: 0.0031703638</li><li>- Test Error RMSE: 0.023440943</li></ul> <p>Trial 7 (Next_Tmin)</p> <ul style="list-style-type: none"><li>- Training Error RMSE: 0.0307044456</li><li>- Test Error RMSE: 0.127550735</li></ul> <p>Trial 8 (Next_Tmin)</p> <ul style="list-style-type: none"><li>- Training Error RMSE: 0.0129012211</li><li>- Test Error RMSE: 0.0075642227</li></ul> <p>Trial 9 (Next_Tmin)</p> <ul style="list-style-type: none"><li>- Training Error RMSE: 0.0322146765</li><li>- Test Error RMSE: 0.0895942114</li></ul> <p>Trial 10 (Next_Tmin)</p> <ul style="list-style-type: none"><li>- Training Error RMSE: 0.0356269333</li><li>- Test Error RMSE: 0.1180644071</li></ul>
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## 2-2)

Iteration	10				
Sento	Versi	Virgi	Prediction	Guess	
0.0%	27.53%	96.1%	Iris-virginica	True - Iris-virginica	
0.01%	36.64%	99.45%	Iris-virginica	True - Iris-virginica	
99.97%	8.12%	0.0%	Iris-setosa	True - Iris-setosa	
0.0%	37.17%	99.86%	Iris-virginica	True - Iris-virginica	
0.0%	38.46%	99.91%	Iris-virginica	True - Iris-virginica	
0.47%	62.56%	0.08%	Iris-versicolor	True - Iris-versicolor	
99.8%	11.5%	0.0%	Iris-setosa	True - Iris-setosa	
0.04%	16.98%	36.67%	Iris-virginica	False - Iris-versicolor	
99.27%	30.18%	0.0%	Iris-setosa	True - Iris-setosa	
99.73%	17.72%	0.0%	Iris-setosa	True - Iris-setosa	
0.4%	90.1%	0.54%	Iris-versicolor	True - Iris-versicolor	
99.24%	14.0%	0.0%	Iris-setosa	True - Iris-setosa	
0.1%	64.11%	0.54%	Iris-versicolor	True - Iris-versicolor	
0.01%	43.98%	93.5%	Iris-virginica	True - Iris-virginica	
0.17%	54.96%	0.32%	Iris-versicolor	True - Iris-versicolor	
0.09%	72.85%	4.6%	Iris-versicolor	True - Iris-versicolor	
0.15%	27.76%	1.04%	Iris-versicolor	True - Iris-versicolor	
0.54%	55.22%	0.02%	Iris-versicolor	True - Iris-versicolor	
0.0%	90.19%	100.0%	Iris-virginica	True - Iris-virginica	
0.0%	56.81%	98.14%	Iris-virginica	True - Iris-virginica	
0.11%	53.37%	10.35%	Iris-versicolor	True - Iris-versicolor	
0.04%	82.86%	48.71%	Iris-versicolor	True - Iris-versicolor	
99.05%	21.43%	0.0%	Iris-setosa	True - Iris-setosa	
0.36%	28.56%	4.4%	Iris-versicolor	True - Iris-versicolor	
6.84%	36.99%	0.01%	Iris-versicolor	True - Iris-versicolor	
99.55%	15.77%	0.0%	Iris-setosa	True - Iris-setosa	
0.21%	72.61%	0.27%	Iris-versicolor	True - Iris-versicolor	
0.0%	85.65%	99.01%	Iris-virginica	True - Iris-virginica	
0.3%	37.2%	0.17%	Iris-versicolor	True - Iris-versicolor	

\*Accuracy: 96.55172413793103 %