

# DATA MINING B(2)

10-0. Answer for 1st quiz

# Q1

- Please calculate the probability of play=yes/play=no under the following condition.

Outlook	Temperature	Humidity	Windy	Play
Sunny	66	90	true	?

- Answer
  - Temperature=66 when play=yes: Average=73, deviation=6.2
    - $f(temp = 66|yes) = \frac{1}{\sqrt{2\pi} \times 6.2} e^{-\frac{(73-66)^2}{2 \times 6.2^2}} = 0.0340$
  - Temperature=66 when play=no: Average=74.6, deviation=7.9
    - $f(temp = 66|no) = \frac{1}{\sqrt{2\pi} \times 7.9} e^{-\frac{(74.6-66)^2}{2 \times 7.9^2}} = 0.279$
  - Humidity=66 when play=yes: Average=79.1, deviation=10.2
    - $f(hum = 90|yes) = \frac{1}{\sqrt{2\pi} \times 10.2} e^{-\frac{(79.1-90)^2}{2 \times 10.2^2}} = 0.0221$
  - humidity=66 when play=no: Average=86.2, deviation=9.7
    - $f(hum = 90|no) = \frac{1}{\sqrt{2\pi} \times 9.7} e^{-\frac{(86.2-90)^2}{2 \times 9.7^2}} = 0.0381$

# Q1

- Please calculate the probability of play=yes/play=no under the following condition.

Outlook	Temperature	Humidity	Windy	Play
Sunny	66	90	true	?

- Answer(cont.)
  - Yes cases are 9 of 14, No cases are 5 of 14.
  - $P(\text{outlook}=\text{sunny}|\text{yes})$ : “yes” cases are 9, and outlook=sunny is 2, so  $p=2/9$ .
  - $P(\text{outlook}=\text{sunny}|\text{no})$ : “no” cases are 5, and outlook=sunny is 3, so  $p=3/5$ .
  - $P(\text{windy}=\text{true}|\text{yes})$ : “yes” cases are 9, and outlook=sunny is 3, so  $p=3/9$ .
  - $P(\text{windy}=\text{true}|\text{no})$ : “no” cases are 5, and outlook=sunny is 3, so  $p=3/5$ .

# Q1

- Please calculate the probability of play=yes/play=no under the following condition.

Outlook	Temperature	Humidity	Windy	Play
Sunny	66	90	true	?

- Answer(cont.)

- Likelihood of yes =  $p(\text{sunny}|\text{yes}) * p(\text{temp}=66|\text{yes}) * p(\text{hum}=90|\text{yes}) * p(\text{windy}=\text{true}|\text{yes}) * p(\text{play}=\text{yes})$   
 $= 2/9 * 0.0340 * 0.221 * 3/9 * 9/14 = 0.000036$
- Likelihood of no =  $p(\text{sunny}|\text{no}) * p(\text{temp}=66|\text{no}) * p(\text{hum}=90|\text{no}) * p(\text{windy}=\text{true}|\text{no}) * p(\text{play}=\text{no})$   
 $= 3/5 * 0.0279 * 0.381 * 3/5 * 5/14 = 0.000137$

Prob of yes =  $0.000036 / (0.000036 + 0.000137) = 20.8\%$

Prob of no =  $0.0000137 / (0.000036 + 0.000137) = 79.2\%$

# Supplement: Naïve Bayes Document Classification

- Please calculate a probability of document {blue, yellow, blue,} for class H'.
- Answer
  - Document class H'
    - $\text{Pr}[\text{yellow}|\text{H}']=10\%, \text{Pr}[\text{blue}|\text{H}']=90\%$
  - The document we want to classify is {blue, yellow, blue}
  - $$P[\{\text{yellow, blue, blue}\}|\text{H}'] = 3! \cdot \frac{\left(\frac{1}{10}\right)^1}{1!} \cdot \frac{\left(\frac{9}{10}\right)^2}{2!} = \frac{3 \times 2 \times 1 \times 1 \times 9 \times 9}{2 \times 10 \times 10^2} = \frac{273}{1000} = 27.3\%$$

For class H.

$$P[\{\text{yellow, blue, blue}\}|\text{H}] = 14\%$$