# Subtyping:

$$\frac{C <: C}{C <: E}$$

$$\frac{\mathit{CT}(\mathtt{C}) = \mathtt{class} \ \mathtt{C} \ \mathtt{extends} \ \mathtt{D} \ \{\ldots\}}{\mathtt{C} \mathrel{<\!\!\!\!\cdot} \mathtt{D}}$$

#### Computation:

$$\frac{\mathit{fields}(\mathtt{C}) = \overline{\mathtt{C}} \ \overline{\mathtt{f}}}{(\mathtt{new} \ \mathtt{C}(\overline{\mathtt{e}})) . \mathtt{f}_i \longrightarrow \mathtt{e}_i} \tag{R-Field}$$

$$\frac{mbody(\mathtt{m},\mathtt{C}) = (\overline{\mathtt{x}},\mathtt{e}_0)}{(\mathtt{new}\ \mathtt{C}(\overline{\mathtt{e}})).\mathtt{m}(\overline{\mathtt{d}})}$$

$$\longrightarrow [\overline{\mathtt{d}}/\overline{\mathtt{x}},\mathtt{new}\ \mathtt{C}(\overline{\mathtt{e}})/\mathtt{this}]\mathtt{e}_0$$
(R-Invk)

$$\frac{\mathtt{C} \mathrel{<\!\!\!\cdot} \mathtt{D}}{(\mathtt{D}) \, (\mathtt{new} \, \, \mathtt{C}(\overline{\mathbf{e}})) \longrightarrow \mathtt{new} \, \, \mathtt{C}(\overline{\mathbf{e}})} \qquad (\mathtt{R-CAST})$$

#### Congruence:

$$\frac{e_0 \longrightarrow e_0'}{e_0 \cdot f \longrightarrow e_0' \cdot f}$$
 (RC-Field)

$$\frac{e_0 \longrightarrow e_0{'}}{e_0\centerdot m(\overline{e}) \longrightarrow e_0{'}\centerdot m(\overline{e})} \quad (\text{RC-Invk-Recv})$$

$$\frac{\mathbf{e}_{i} \longrightarrow \mathbf{e}_{i}'}{\mathbf{e}_{0} \cdot \mathbf{m}(\dots, \mathbf{e}_{i}, \dots)} \qquad (\text{RC-Invk-Arg})$$
$$\longrightarrow \mathbf{e}_{0} \cdot \mathbf{m}(\dots, \mathbf{e}_{i}', \dots)$$

$$\frac{\mathbf{e}_{i} \longrightarrow \mathbf{e}_{i}'}{\text{new C}(\dots, \mathbf{e}_{i}, \dots)} \quad (\text{RC-New-Arg})$$

$$\longrightarrow \text{new C}(\dots, \mathbf{e}_{i}', \dots)$$

$$\frac{e_0 \longrightarrow e_0'}{(C)e_0 \longrightarrow (C)e_0'} \tag{RC-CAST}$$

#### **Expression typing:**

$$\Gamma \vdash x \in \Gamma(x)$$
 (T-Var)

$$\frac{\Gamma \vdash e_0 \in C_0 \quad \textit{fields}(C_0) = \overline{C} \ \overline{f}}{\Gamma \vdash e_0 \cdot f_i \in C_i} \quad \text{(T-Field)}$$

$$\begin{array}{c} \Gamma \vdash \mathbf{e}_0 \in \mathsf{C}_0 \\ \mathit{mtype}(\mathsf{m},\mathsf{C}_0) = \overline{\mathsf{D}} \!\!\to\!\! \mathsf{C} \\ \underline{\Gamma \vdash \overline{\mathsf{e}} \in \overline{\mathsf{C}}} \quad \overline{\mathsf{C}} \mathrel{<\!\!\!\cdot} \overline{\mathsf{D}} \\ \overline{\Gamma \vdash \mathsf{e}_0 . \mathsf{m}(\overline{\mathsf{e}})} \in \mathsf{C} \end{array} \tag{T-Invk}$$

$$\frac{\Gamma \vdash e_0 \in D \quad D \iff C}{\Gamma \vdash (C)e_0 \in C}$$
 (T-UCAST)

$$\frac{\Gamma \vdash \mathbf{e}_0 \in D \qquad C <: \ D \qquad C \neq D}{\Gamma \vdash (C) \mathbf{e}_0 \in C} \qquad (\text{T-DCast})$$

$$\frac{\Gamma \vdash \mathsf{e}_0 \in \mathsf{D} \quad \mathsf{C} \not \approx \mathsf{D} \quad \mathsf{D} \not \approx \mathsf{C}}{\underset{\Gamma \vdash (\mathsf{C}) \, \mathsf{e}_0 \, \in \, \mathsf{C}}{\mathit{stupid warning}}} \qquad (\mathsf{T\text{-}SCAST})$$

## Method typing:

$$\begin{array}{c} \overline{\mathbf{x}}: \overline{\mathbf{C}}, \mathtt{this}: \mathbf{C} \vdash \mathbf{e}_0 \in \mathbf{E}_0 & \mathbf{E}_0 \leqslant \mathbf{C}_0 \\ CT(\mathbf{C}) = \mathtt{class} \ \mathbf{C} \ \mathtt{extends} \ \mathbf{D} \ \{\ldots\} \\ \hline override(\mathbf{m}, \mathbf{D}, \overline{\mathbf{C}} {\rightarrow} \mathbf{C}_0) \\ \hline \mathbf{C}_0 \ \mathbf{m} \ (\overline{\mathbf{C}} \ \overline{\mathbf{x}}) \ \{\mathtt{return} \ \mathbf{e}_0;\} \ \mathtt{OK} \ \mathtt{IN} \ \mathtt{C} \\ \hline \end{array}$$

#### Class typing:

$$\begin{array}{c} \texttt{K} = \texttt{C}(\overline{\texttt{D}}\ \overline{\texttt{g}},\ \overline{\texttt{C}}\ \overline{\texttt{f}}) \ \{\texttt{super}(\overline{\texttt{g}}); \ \texttt{this}.\overline{\texttt{f}} = \overline{\texttt{f}};\} \\ \underline{fields}(\texttt{D}) = \overline{\texttt{D}}\ \overline{\texttt{g}} & \overline{\texttt{M}}\ \texttt{OK}\ \texttt{IN}\ \texttt{C} \\ \hline \\ \texttt{class}\ \texttt{C}\ \texttt{extends}\ \texttt{D}\ \{\overline{\texttt{C}}\ \overline{\texttt{f}};\ \texttt{K}\ \overline{\texttt{M}}\}\ \texttt{OK} \\ & (\text{T-CLASS}) \end{array}$$

Figure 1: FJ: Main definitions

#### Field lookup:

$$\mathit{fields}(\mathtt{Object}) = ullet$$

$$\frac{CT(\mathtt{C}) = \mathtt{class} \ \mathtt{C} \ \mathtt{extends} \ \mathtt{D} \ \{\overline{\mathtt{C}} \ \overline{\mathtt{f}}; \ \mathtt{K} \ \overline{\mathtt{M}}\}}{\mathit{fields}(\mathtt{D}) = \overline{\mathtt{D}} \ \overline{\mathtt{g}}}$$
$$\frac{\mathit{fields}(\mathtt{C}) = \overline{\mathtt{D}} \ \overline{\mathtt{g}}, \overline{\mathtt{C}} \ \overline{\mathtt{f}}}$$

## Method type lookup:

$$\frac{CT(\mathtt{C}) = \mathtt{class} \ \mathtt{C} \ \mathtt{extends} \ \mathtt{D} \ \{\overline{\mathtt{C}} \ \overline{\mathtt{f}}; \ \mathtt{K} \ \overline{\mathtt{M}}\}}{B \ \mathtt{m} \ (\overline{\mathtt{B}} \ \overline{\mathtt{x}}) \ \{\mathtt{return} \ \mathtt{e};\} \in \overline{\mathtt{M}}}$$

$$\frac{mtype(\mathtt{m},\mathtt{C}) = \overline{\mathtt{B}} \rightarrow \mathtt{B}}{}$$

$$CT(C) = class C extends D \{\overline{C} \ \overline{f}; K \overline{M}\}$$
 m is not defined in  $\overline{M}$ 

$$mtype(m, C) = mtype(m, D)$$

## Method body lookup:

$$\frac{CT(\texttt{C}) = \texttt{class C extends D } \{\overline{\texttt{C}} \ \overline{\texttt{f}}; \ \texttt{K} \ \overline{\texttt{M}}\}}{\texttt{B m } (\overline{\texttt{B}} \ \overline{\texttt{x}}) \ \{\texttt{return e};\} \in \overline{\texttt{M}}}$$
$$\frac{mbody(\texttt{m},\texttt{C}) = (\overline{\texttt{x}},\texttt{e})}$$

$$\frac{CT(\mathtt{C}) = \mathtt{class} \ \mathtt{C} \ \mathtt{extends} \ \mathtt{D} \ \{\overline{\mathtt{C}} \ \overline{\mathtt{f}}; \ \mathtt{K} \ \overline{\mathtt{M}}\}}{\mathtt{m} \ \mathtt{is} \ \mathtt{not} \ \mathtt{defined} \ \mathtt{in} \ \overline{\mathtt{M}}}$$
$$\frac{mbody(\mathtt{m},\mathtt{C}) = mbody(\mathtt{m},\mathtt{D})}{}$$

#### Valid method overriding:

$$\frac{\mathit{mtype}(\mathtt{m},\mathtt{D}) = \overline{\mathtt{D}} \rightarrow \mathtt{D}_0, \mathrm{implies} \ \overline{\mathtt{C}} = \overline{\mathtt{D}} \ \mathrm{and} \ \mathtt{C}_0 = \mathtt{D}_0}{\mathit{override}(\mathtt{m},\mathtt{D},\overline{\mathtt{C}} \rightarrow \mathtt{C}_0)}$$

Figure 2: FJ: Auxiliary definitions