

EECS 203A HW2.

1*

(a) for $r_k = 1, 2, \dots, 49$ $h(r_k) = 1 + r_k$

Total number of pixels N : $\sum_{k=0}^{49} (1+k) = 50 \cdot 0 + \frac{49 \cdot 50}{2} = 1225$

$$\text{CDF: } T(r_k) = \frac{1}{N} \sum_{i=0}^k h(r_i) = \frac{1}{1225} \sum_{i=0}^k (1+i) = \frac{1}{1225} \left(50(k+1) + \frac{k(k+1)}{2} \right)$$

$$= (k+1)(k+10) / 3450$$

(b) Transformation $M(r_k)$ for histogram equalization is

$$M(r_k) = \text{round}((L-1)T(r_k))$$

$$= \text{round} \left(49 \times \frac{(k+1)(k+10)}{3450} \right)$$

(c) histogram of transformed image $h_m(s_j)$ (s_j is new gray level)

$M(r_k)$ must be calculated manually ex) $M(1) = \text{round} \left(49 \times \frac{2 \times 11}{3450} \right) = 1$, $M(2) = 1$, ...

2*

$n_1(x,y) \sim \mathcal{N}(0, \sigma^2)$, $n_2(x,y) \sim \mathcal{N}(0, \sigma^2)$

$$(a) \mathbb{E}[g'(x,y)] = 0.5 \mathbb{E}[g_1(x,y)] + 0.25 \mathbb{E}[g_2(x,y)]$$

$$= 0.5 f(x,y) + (0.25)(2) f(x,y)$$

$$= f(x,y)$$

$$(b) \text{Var}(g'(x,y)) = (0.5)^2 \text{Var}(g_1(x,y)) + (0.25)^2 \text{Var}(g_2(x,y))$$

$$\text{Var}(g_1(x,y)) = \text{Var}(n_1) = \sigma^2 / \text{Var}(g_2(x,y)) = \text{Var}(n_2) = \sigma^2$$

$$\text{as } g_2 = 2n_2, \text{Var}(g'(x,y)) = 0.25\sigma^2 + 0.0625\sigma^2 = 0.3125\sigma^2$$